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## EC3353-ELECTRONIC DEVICES AND CIRCUITS <br> UNIT-I PN.JUNCTION DEVICES <br> PART - B <br> PN junction diode: structure, operation \& V-I characteristics

1. With a neat diagram explain the working of a PN junction diode in forward bias

And reverse bias and show the effects of temperature on its VI characteristics (NOV/DEC 2012), (May / June 2016), (Nov / Dec 2015)
(OR)
Outline the charge carrier diffusion phenomenon across a PN junction. Explain the effect of forward and reverse biasing on the depletion region. (Nov/Dec 2018 R-13) (April / May 2019-R17)

A PN junction is formed from a piece of semiconductor ( Ge or Si ) by diffusing p-type material (Acceptor impurity Atoms) to one half side and N type material to (Donar Impurity Atoms) other half side. The plane dividing the two zones is known as 'Junction'.

The P-region of the semiconductor contains a large number of holes and N region, contains a large number of electrons. A PN junction just immediately formed is shown in Fig.


When PN junction is formed, there is a tendency for the electrons in the N -region to diffuse into the p region, and holes from P-region to N -region. This process is called diffusion. While crossing the junction, the electrons and holes recombines with each other, leaving the immobile ions in the neighborhood of the junction neutralized as shown in Fig.


These immobile + ve and -ve ions, set up a potential across the junction. This potential is called potential barrier or junction barrier. Due to the potential barrier no further diffusion of electrons and holes takes place across the junction. Potential barrier is defined as a potential difference built up across the PN junction which restricts further movement of charge carriers across the junction. The potential barrier for a silicon PN junction is about 0.7 volt, whereas for Germanium PN junction is approximately 0.3 volt.

## Symbol of Diode:

The symbol of PN junction diode is shown in Fig. The P-type and N-type regions are referred to as Anode and Cathode respectively. The arrowhead shows the conventional direction of current flow when the diode is forward biased.


## Working of PN Junction Diode:

## Forward Bias:

When the positive terminal of the external battery is connected to the P-region and negative terminal to the N -region, the PN junction is said to be forward biased as shown in Fig.


When the junction is forward biased, the holes in the p-region are repelled by the positive terminal of the battery and are forced to move towards the junction. similarly, the electrons in the N -region are repelled by the negative terminal of the battery and are forced to move towards the-junction.

This reduces the width of the depletion layer and barrier potential. If the applied voltage is greater than the potential barrier $\mathrm{v}_{\mathrm{r}}$, then the majority carriers namely holes in P-region and electrons in N-region, cross the barrier. During crossing some of the charges get neutralized the remaining charges after crossing, reach the other side and constitute current in the forward direction. The PN junction offers very low resistance under forward biased condition.

Since the barrier potential is very small (nearly 0.7 V for silicon and 0.3 V for Germanium junction), a small forward voltage is enough to completely eliminate the barrier. once the potential barrier is eliminated by the forward voltage, a large current start flowing through the PN junction.

## Reverse Bias:



When the positive terminal of the external battery is connected to the N -region and negative terminal to the p-region, the PN junction is said to be reverse biased. When the junction is reverse biased, the holes in the P-region are attracted by the negative terminal of the battery. Similarly, the electrons in the N-region

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are attracted by the positive terminal of the external battery. This increases the width of the depletion layer and barrier potential (Vs).

The increased barrier potential makes it very difficult for the majority carriers to diffuse across the junction. Thus, there is no current due to majority carriers in a reverse biased PN junction. In other words, the PN junction offers very high resistance under reverse biased condition.

In a reverse biased PN junction, a small amount of current (in $\mu \mathrm{A}$ ) flows through the junction because of minority carriers. (i.e., electrons in the P-region and holes in the N region).The reverse current is small because the number of majority carrier in both regions is small.

## V-I characteristics of PN-Junction Diode:



A graph between the voltage applied across the PN junction and the current flowing through the junction is called the V-I characteristics of PN junction diode. Fig. shows the V-I characteristics of PN junction diode.

## Forward Characteristics:

Fig. (a) shows the circuit arrangement for drawing the forward V-I characteristics of PN junction diode. To apply a forward bias, the +ve terminal of the battery is connected to Anode (A) and the negative terminal of the battery is connected to Cathode (K). Now, when supply voltage is increased the circuit current increases very slowly and the curve is nonlinear (region-OA).

The slow rise in current in this region is because the external applied voltage is used to overcome the barrier potential ( 0.7 V for $\mathrm{Si} ; 0.3 \mathrm{~V}$ for Ge ) of the PN junction' However once the potential barrier is eliminated and the external supply voltage is increased further, the current flowing through the PN junction diode increases rapidly (region AB ). This region of the curve is almost linear. The applied voltage should not be increased beyond a certain safe limit, otherwise the diode will burnout.

The forward voltage at which the current through the PN junction starts increasing rapidly is called by knee voltage. It is denoted by the letter $\mathrm{V}_{\mathrm{B}}$.

## Reverse Characteristics:

Fig (b) shows the circuit arrangement for drawing the reverse V-I characteristics of PN junction diode. To apply a reverse bias, the +ve terminal of the battery is connected to cathode (K) and - ve terminal of the battery is connected to anode (A).

Under this condition the potential buried at the junction is increased. Therefore, the junction resistance becomes very high and practically no. current flows through the circuit. However, in actual practice, a very small current (of the order of $\mu \mathrm{A}$ ) flows in the circuit. This current is called reverse current and is due to minority carriers. It is also called as reverse saturation current (I). The reverse current increases slightly with the increase in reverse bias supply voltage.

If the reverse voltage is increased continuously at one state (marked by point C on the reverse characteristics) breakdown of junction occurs and the resistance of the barrier regions falls suddenly. Consequently, the reverse current increases rapidly (as shown by the curve CD in the current) to a large value. This may destroy the junction permanently. The reverse voltage at which the PN junction breaks is called as break down voltage.

## Temperature effects

The cut in voltage decreases as the temperature increases. The reverse saturation current increases.
$I_{02}=2^{(\Delta T / 10)} I_{01}$
$I_{01,} I_{02}$ are the reverse current at $\mathrm{T}_{1}{ }^{\circ} \mathrm{C}, \mathrm{T}_{2}{ }^{\circ} \mathrm{C}$
$\Delta T=\mathrm{T}_{2}-\mathrm{T}_{1}$.
The voltage equivalent of temperature $V_{T}$ also increases. The reverse breakdown voltage increases.

## 2. Derive the PN diode current equation.

The applied voltage and current though diode are related by the equation

$$
I=I_{0}\left(e^{V / y V_{T}}-1\right)
$$

Where,
Io $=$ Reverse saturation current
$\mathrm{V}=$ Applied voltage
I = Diode current
$\mathrm{VT}=$ Volt equivalent temperature

$$
V_{T}=\frac{\bar{F}}{q}
$$

$-k=1.38 * 10^{-23} \mathrm{~J} / \mathrm{K}$
$\mathrm{T}=$ temperature of the diode junction
I = diode current
$\mathrm{Q}=$ change of electron $1.602 * 10^{-19} \mathrm{C}$
At any temperature

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$$
V_{T}=\frac{{ }^{6}}{q}=\frac{1.38 \times 10^{-23}}{1.602 \times 10^{-19}}=\frac{T}{11600}
$$

At room temperature

$$
V_{T}=\frac{300}{11600}=26 \mathrm{mV}
$$

The value of $\eta=1$ for germanium and 2 for silicon.
For forward bias voltage the current equation reduces to

$$
I=I_{0}\left(e^{V / y V_{T}}\right)
$$

At room temperature for germanium transistor

$$
I=I_{0}\left(e^{40}\right)
$$

When the diode is reverse biased

$$
\begin{gathered}
I=I_{0}\left(e^{V / y V_{T}}-1\right) \\
I \cong I_{0}
\end{gathered}
$$

## Diffusion and transient capacitance

## 3. Explain diffusion and transition capacitance of diode

Depletion layer capacitance (or) transition capacitance (or) space charge capacitance (May / June 2016)(Nov/Dec 2016)(May 2017)

- When a PN junction is reverse biased, a layer of positive and negative immobile ions, called depletion layer, is formed on either side of the junction. It is also known as depletion-region, space-charge region or transition region. The depletion-layer acts as a dielectric (i.e., non-conductive) medium between P-region and N -region. We know that the P-region and N-region on either side of the junction, has a low resistance. Therefore, these regions act as two plates of a capacitor, separated by a dielectric (i.e., depletion layer) as shown in Fig.


The capacitance formed in a junction area is called depletion layer capacitance. It is also called depletion region-capacitance, space charge capacitance, transition region capacitance or simply junction capacitance.

- Since the depletion layer width $(d)$ increases with the increase in reverse bias voltage, the resulting depletion layer capacitance will decrease with the increased reverse bias.
- The depletion layer capacitance depends upon the nature of a PN junction, semiconductor material and magnitude of the applied reverse voltage. It is given by the relation,


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$$
C_{T}=\frac{K}{\left(V_{B}-V\right)^{n}}
$$

Where
$\mathrm{K}=\mathrm{A}$ constant, depending upon the nature of semiconductor material
$\mathrm{VB}=$ barrier voltage. 0.6 V for silicon and 0.3 V for germanium
$\mathrm{V}=$ applied reverse voltage
n a constant depending upon the nature of junction.
The value of the K is

$$
K=A \times \frac{\epsilon \cdot q}{2}\left(\frac{N_{A} \cdot N_{D}}{N_{A}+N_{D}}\right)
$$

- The value of ' $n$ ' is taken as $1 / 2$ for step or abrupt junction, $1 / 3$ for linearly graded junction.
- It is the evident from the above relation that the value of depletion layer capacitance (CT) can be controlled by varying the applied reverse voltage. This property of variable capacitance, possessed by reverse biased PN junction, is used in the concentration of a device called varactor.
Reverse biased.


## Derivation:



Connection P side is less
Doping less in P side $\left(\mathrm{N}_{\mathrm{A}}\right)$
N side $\left(\mathrm{N}_{\mathrm{D}}\right)$
Potential \& change density Relation

$$
N_{A}<N_{D} \frac{d^{2} V}{d^{2}}------------1
$$

$$
\mathrm{X} \text { - distance measured from junction }
$$

$$
\mathrm{N}_{\mathrm{A}}<\mathrm{N}_{\mathrm{D}} \frac{\mathrm{~d} 2 V}{\mathrm{E} \mathrm{~V}^{2}}=\frac{\mathrm{qND}}{\mathrm{~s}}
$$

Integrating 2

$$
\begin{aligned}
& \int \frac{\mathrm{d}^{2} \mathrm{~V}}{\mathrm{dx}^{2}}=\int \frac{\mathrm{qN} \mathrm{~N}_{\mathrm{D}}}{\mathrm{~d}^{\varepsilon}} \\
& \frac{\mathrm{dv}}{\mathrm{dx}}=\frac{\mathrm{qN}_{\mathrm{A}} \mathrm{~S}^{2}}{\varepsilon}
\end{aligned}
$$

To get potential from 0 to w

$$
\int_{o}^{\mathrm{V}_{\mathrm{B}}} \frac{\mathrm{dv}}{\mathrm{dx}}=\int_{\mathrm{o}}^{\mathrm{w}} \frac{\mathrm{qN}_{\mathrm{A}} \mathrm{X}}{\varepsilon} \mathrm{dx}
$$

Where $\mathrm{V}=\mathrm{V}_{\mathrm{B}}$

$$
\mathrm{X}=\mathrm{w}
$$

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$$
\begin{array}{r}
\mathrm{V}_{\mathrm{B}}=\frac{\mathrm{qN}_{\mathrm{A}}}{\mathrm{~s}} \times \frac{\mathrm{w}^{2}}{2} \\
\mathrm{~W}=\sqrt{\mathrm{V}_{\mathrm{B}}}
\end{array}
$$

$\mathrm{Q}=$ No of change particle $\times$ change on each particle

$$
\begin{aligned}
&=\left(\mathrm{N}_{\mathrm{A}} \times \text { volume }\right) \times \mathrm{q} \\
& \mathrm{Q}=\mathrm{qN}_{\mathrm{A}} A W_{\ldots} . . . . . . . . . . . . . . . . . . . . ~
\end{aligned} 2
$$

Diff 3 w.r.to V

$$
\mathrm{V}_{\mathrm{B}}=\frac{\mathrm{q} \mathrm{~N}_{\mathrm{A}}}{\varepsilon} \times \frac{\mathrm{w}^{2}}{2}
$$

$1=\frac{\mathrm{qN}_{\mathrm{A}}}{\mathrm{s}} \times \frac{1}{2} \frac{\mathrm{dw}}{\mathrm{dv}} 2 \mathrm{w}$

$$
\frac{\mathrm{dw}}{\mathrm{dv}}=\frac{\varepsilon}{\mathrm{qN} \mathrm{~N}_{\mathrm{AW}}}
$$

Diff 2


Ex: Varactor diode (or) Tuning diode
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## Diffusion capacitance $\mathrm{C}_{\mathrm{d}}$ :(May 2017)

The junction behaves like a capacitor. The capacitance, which exists in a forward-biased junction is called a diffusion or storage capacitance. It is different from the transition or depletion layer capacitance, which exists in a reverse-biased junction. The diffusion capacitance arises due to the arrangement of minority carrier density. And its value is much larger than the depletion layer capacitance.
Width of depletion region $\downarrow$ As applied voltage $\uparrow$, the concentration of injected charged particle also increases. This rate of change of injected change with applied voltage is capacitance.
$r=$ mean lifetime of the carrier
$\mathrm{I}=$ value of forward current
$\eta=\mathrm{A}$ constant ( 1 for Ge and 2 for Si )
$\mathrm{V}_{\mathrm{T}}=$ volt equivalent of temperature.
$C_{D}=\frac{d Q}{d v}$


C is $>\mathrm{C}_{\mathrm{T}}$
$\mathrm{I}=\mathrm{I}_{\mathrm{pn}(0)}+\mathrm{I}_{\mathrm{np}(0)}$
$\mathrm{Imn}_{\mathrm{p}(0)} \rightarrow$ hole diffusion current n region
$\mathrm{I}_{\mathrm{np}}(0) \rightarrow$ electron diffusion current in p region

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$$
\mathrm{I}_{\mathrm{np}(0)} \simeq 0
$$

$P$ side heavily doped

$$
\begin{gathered}
\mathrm{Jp}_{\mathrm{p}(\mathrm{x})}=-\mathrm{qD} \mathrm{D} \frac{\mathrm{dp} \mathrm{n}}{\mathrm{dx}} \\
\mathrm{~J}=\frac{\mathrm{I}}{\mathrm{~A}}
\end{gathered}
$$

$I_{p}(X)=-q A D_{p} \frac{d p_{n}}{d x}--\quad-\quad-\quad-\quad-\quad 1$
$\mathrm{P}_{\mathrm{n}}(\mathrm{X})=\mathrm{P}_{\mathrm{n}(0)} \mathrm{e}^{-\mathrm{X} / \mathrm{LP}-\ldots}-2$
Hole concentration in the right side of p material $\mathrm{P}_{\mathrm{n}(0)}$ ie junction Diff 2

$$
\frac{d p_{n}(x)}{d x}=P_{n(0)} e^{e-x / L^{P}}\left(\frac{1}{L P}\right)
$$

$\mathrm{I}_{\mathrm{p}}(\mathrm{X})=-\mathrm{qAD}_{\mathrm{p}} \mathrm{P}_{\mathrm{n}(0)} \mathrm{e}^{-\mathrm{X} / \mathrm{LP}} \cdot-1 / \mathrm{LP}_{\mathrm{p}}$
At $\mathrm{x}=0 \mathrm{I}_{\mathrm{p}}(\mathrm{X})=\mathrm{I}_{\mathrm{pn}(0)}=\mathrm{I}$

$$
\mathrm{I}=\frac{\mathrm{QAD}_{\mathrm{P}}}{\mathrm{LP}_{P}} \operatorname{Pn}(0)
$$

$\operatorname{Pn}(0)=\frac{L_{p}}{\text { QAD }_{P}}$
A
Now the excess minority charge exists only on n side and given by
$\mathrm{Q}=\int_{0}^{\infty} \mathrm{Aq} \operatorname{Pn}(0) \mathrm{e}^{-\mathrm{X} / \mathrm{LP}} \mathrm{dx}$
$=\operatorname{AqPn}(0)\left[\frac{\mathrm{e}^{-\mathrm{x} / L_{\mathrm{P}}}}{\frac{-1}{L_{\mathrm{p}}}}\right]_{0}^{\infty}$
$=\operatorname{AqLpPn}(0)\left[\mathrm{e}^{-\infty}-\mathrm{e}^{-0}\right]$
$\mathrm{Q}=-\operatorname{AqLpPn}(0)$
Q=AqLpPn(0)------------------B
Put A in B
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$\mathrm{Q}=\frac{\mathrm{AqLpILp}}{\mathrm{qADp}}=\frac{\mathrm{Lp}{ }^{2}}{\mathrm{Dp}} . \mathrm{I}$
Assume
$\frac{\mathrm{L}_{\mathrm{p}}{ }^{2}}{\mathrm{Dp}}=r$
$\mathrm{Q}=r \mathrm{I} \Rightarrow \frac{\mathrm{dQ}}{\mathrm{dl}}=r$
W.K.T

$$
\begin{gathered}
\mathrm{C}_{\mathrm{D}}=\frac{\mathrm{dQ}}{\mathrm{dI}} \cdot \frac{\mathrm{dI}}{\mathrm{dV}} \\
\mathrm{C}_{\mathrm{D}}=r \cdot \frac{\mathrm{dI}}{\mathrm{dV}} \\
\mathrm{I}=\mathrm{I}_{\mathrm{o}}\left(\mathrm{e}^{\mathrm{VDVT}}\right) \\
\frac{\mathrm{dI}}{\mathrm{dV}}=\mathrm{I} \cdot \frac{1}{\eta V_{\mathrm{T}}} \\
\mathrm{C}_{\mathrm{D}}=r \cdot \frac{\mathrm{I}}{\eta V_{\mathrm{T}}}
\end{gathered}
$$

It is evident from the above relation, that diffusion capacitance is directly proportional to the forward current (I).

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## Rectifiers - Half Wave and Full Wave

## Half Wave

4. What is halfwave rectifier? Explain the working principle with neat sketch? (Nov / Dec 2015) (Nov/Dec 2016)

Rectifiers are a class of circuits whose purpose is to convert ac waveforms (usually sinusoidal and with zero average value) into a waveform that has a significant non-zero average value (dc component). Simply stated, rectifiers are ac-to-dc energy converter circuits. Most rectifier circuits employ diodes as the principal elements in the energy conversion process; thus, the almost inseparable notions of diodes and rectifiers.

Uncontrolled rectifier: uncontrolled refers to the absence of any control signal necessary to operate the primary switching elements (diodes) in the rectifier circuit. (The discussion of controlled rectifier circuits, and the controlled switches themselves, is more appropriate in the context of power electronics applications). Rectifiers are the fundamental building block in dc power supplies of all types and in dc power transmission used by some electric utilities.

There are two types of rectifiers:
(a) Half Wave (HW) rectifier
(b) Full Wave (FW) rectifier

## Half -wave Rectifier:

It consists of a single diode in series with a load resistor. The input to half wave rectifier is supplied from the 50 Hz a.c supply. The circuit diagram for halfwave rectifier is shown in fig.


## Positive half cycle:

During the positive half cycle of the input signal the anode of the diode becomes positive with respect to the cathode and hence the diode D conducts. For an ideal to the cathode and hence the diode D conducts. For an ideal diode, the forward voltage drop is zero. So the whole-input voltage will appear across load resistance $\mathrm{R}_{\mathrm{L}}$.

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## Negative half cycle:

During negative half cycle of the input signal, the anode of the diode becomes negative with respective to the cathode and hence the diode D does not contact. For an ideal diode the impedance by the diode is infinity. So the whole input voltage appears across the diode D . hence the voltage drop across R , is zero.

## Analysis of Half wave rectifier:

Let Vi be the input voltage to the rectifier

$$
V_{i}=V_{m} \sin \omega t
$$

Where,
$V_{m}=$ Maximum value of the input voltage.
Let I be the current flowing though the circuit when the diode is conducting.

$$
i=\left\{\begin{array}{cc}
\operatorname{Im} \sin \omega t & \text { For } 0 \leq \omega t \leq \pi \\
0 & \text { For } \pi \leq \omega t \leq 2 \pi
\end{array}\right\}
$$

Where

$$
\begin{aligned}
& I_{m}=\text { Maximum value of the current } \\
& \qquad I_{m}=\frac{V_{m}}{R_{F}+R_{L}}
\end{aligned}
$$

Where
$R_{F}$-Forward dynamic resistance of diode.
$R_{L}$-Load resistance.
(a) Average or DC value of output current ( $\mathrm{I}_{\mathrm{dc}}$ ):

From Fig., it is seen that the output current is not steady but contains fluctuations even though it is DC current. The average value of this fluctuating current is called DC current ( $\mathrm{I}_{\mathrm{dc}}$ ). It can be calculated as follows.

Average value $=($ Area under the curve $/$ Period $)$

$$
\begin{gathered}
\mathrm{Idc}=\frac{1}{2 \pi} \int_{0}^{2 \pi} \mathrm{id}(\omega \mathrm{t}) \\
\mathrm{I}_{\mathrm{dc}}=\frac{1}{2 \pi}\left[\int_{0}^{\pi} \mathrm{I}_{\mathrm{m}} * \sin \omega \mathrm{t}(\omega \mathrm{t})\right] \\
\mathrm{I}=\frac{1}{2 \pi}[-\cos \omega \mathrm{t}]^{\pi}=\frac{\mathrm{I}_{\mathrm{m}}}{2 \pi}[-\cos \pi-(-\cos 0)]=\frac{\mathrm{I}_{\mathrm{m}}}{2 \pi}[-(-1)-(-1)]=\frac{\mathrm{I}_{\mathrm{m}}}{\pi} \\
\mathrm{I}_{\mathrm{dc}}=\frac{\mathrm{V}_{\mathrm{m}}}{\pi\left(\mathrm{R}_{\mathrm{F}}+\mathrm{R}_{\mathrm{L}}\right)}
\end{gathered}
$$

(b) Average or DC output voltage ( $\mathrm{V}_{\mathrm{o}}$ ):

$$
\mathrm{V}_{\mathrm{dc}}=\frac{\mathrm{Im}}{\pi} \times \mathrm{R}_{\mathrm{L}}=\frac{\mathrm{V}_{\mathrm{m}}}{\pi}
$$

(c) RMS value of output current ( $\mathrm{I}_{\mathrm{rms}}$ ):

$$
\boldsymbol{I}_{r m s}=\sqrt{\frac{1}{2 \pi} \int_{0}^{\pi} \mathrm{i}^{2} \mathrm{~d}(\omega \mathrm{t})}=\sqrt{\frac{1}{2 \pi} \int_{0}^{\pi} \mathrm{I}_{\mathrm{m}}{ }^{2} \sin ^{2} \omega \mathrm{t} * \mathrm{~d}(\omega \mathrm{t})}=\sqrt{\frac{\mathrm{I}_{\mathrm{m}}^{2}}{2 \pi} \int_{0}^{\pi}\left(\frac{1-\cos 2 \omega \mathrm{t}}{2}\right) * \mathrm{~d}(\omega \mathrm{t})}
$$

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$$
\left.\begin{array}{rl} 
& =\sqrt{\frac{\mathrm{I}_{\mathrm{m}}^{2}}{4 \pi} \int_{0}^{\pi} \mathrm{d}(\omega \mathrm{t})-\int_{0}^{\pi} \cos 2(\omega \mathrm{t})} * \mathrm{~d}(\omega \mathrm{t})
\end{array}=\sqrt{\left.\frac{\sqrt{\mathrm{I}_{\mathrm{m}}^{2}\left[\omega \mathrm{t}^{\pi}\right.}-\left(\frac{\sin 2 \omega \mathrm{t}}{}{ }^{\pi}\right.}{4 \pi}\right)_{0}^{2}}\right]
$$

(d) Rectification Efficiency ( $\boldsymbol{\eta}$ ):

(e) Ripple Factor ( $\gamma$ ):

$$
y=\frac{I_{\mathrm{rms}}^{\prime}}{\mathrm{I}_{\mathrm{dc}}}=\sqrt{\frac{\overline{I_{\mathrm{rms}}^{2}-\mathrm{I}_{\mathrm{dc}}^{2}}}{\mathrm{I}_{\mathrm{dc}}^{2}}}=\sqrt{\left(\frac{\mathrm{I}_{\mathrm{rms}}}{\mathrm{I}_{\mathrm{dc}}}\right)^{2}-1}=\sqrt{\left(\frac{\left.\mathrm{I}_{\mathrm{rms}} / 2\right)^{2}}{\mathrm{I}_{\mathrm{m}} / \pi}\right)^{-1}}=\sqrt{\overline{\pi^{2}}-1}=\mathbf{1 . 2 1}
$$

(f) Peak inverse Voltage (PIV):

Peak inverse voltage is defined as the maximum voltage that is applied across the Diode when the diode is reverse biased. [ $n$ case of half wave rectifier, maximum Voltage across the diode when it is not conducting is equal to $\mathrm{V}_{\mathrm{m}}$.

$$
P I V=V_{m}
$$

(g) From factor:

$$
F F=\frac{r m s ~ v a l u e}{\text { average value }}=\frac{\pi}{2}=1.57
$$

(h) Peak factor:

$$
P F=\frac{V_{m}}{\left(\frac{V_{m}}{2}\right)}=2
$$

(i) Transformer utilization factor:

$$
T U F=\frac{P_{d c}}{P_{a c}}(\text { Transformer secondary rated })=0.287
$$

## Disadvantages of HWR:

$>$ Low output because one half cycle only delivers output
$>$ A.C. component more in the output
$>$ Requires heavy filter circuits to smooth out the output Peak inverse Voltage.

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## Rectifiers - Full Wave using center tap Transformer

5. Explain the operation of full wave rectifier with center tap transformer. Also derive the following for this rectifier. (Apr/May 2018)

## i) DC output voltage (average value) output voltage.

ii) DC output current (average value) iii) RMS

In FWR, current flows through the load during both half cycles of the input a.c. supply. Like the half wave circuit, a full wave rectifier circuit produces an output voltage or current which is purely DC or has some specified DC component. Full wave rectifiers have some fundamental advantages over their half wave rectifier counterparts. The average (DC) output voltage is higher than for half wave, the output of the full wave rectifier has much less ripple than that of the half wave rectifier producing a smoother output waveform.

## Full Wave Rectifier:

A full wave rectifier is an electronic circuit which converts AC voltage into a pulsating DC voltage using both half cycles of the applied AC voltage. A full wave rectifier is a circuit which allows a unidirectional current to flow through the load during the entire input cycle as shown in fig. The result of full wave rectification is a d.c. output voltage that pulsates every half-cycle of the input. On the other hand a half wave rectifier allows the current to flow through the load during positive half-cycle only.


## Positive half cycle:

The circuit uses two diodes which are connected to secondary winding of the transformer. The input signal is applied to the primary winding of the transformer. During the positive input half cycle, the polarities of the secondary voltage is shown in fig. This forward bias the diode D , and reverse biases the diode $\mathrm{D}_{1}$. As a result of this, the diode D , conducts some current whereas the diode D , is off.

The current through load R1 is as indicated in through $D_{1}$, and the voltage Drop across $\mathrm{R}_{\mathrm{L}}$ will the fig. The load current flows be equal to the input voltage.


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## Negative half cycle:

During the negative input half cycle, the polarities of the secondary voltage are interchanged. The reverse-bias the diode D , and forward Biases the diode $\mathrm{D}_{2}$. As a result of this, the diode $\mathrm{D}_{1}$ is OFF and the diode $\mathrm{D}_{2}$ conducts some current. The current through the load R , is an indicated in the fig. The load current flows through $\mathrm{D}_{2}$ and the voltage drop across $\mathrm{R}_{1}$ will be equal to the input voltage. The maximum efficiency of a fall-wave rectifier is $81,2 \%$ Vo and ripple factor is 0.48 .


## Analysis of Full Wave Rectifier:

Let Vi be the input voltage to the rectifier, $\quad V_{i}=V_{m} \sin \omega t$
Where, $\quad V_{m}=$ Maximum value of the input voltage.
Let I be the current flowing though the circuit when the diode is conducting.

$$
i=\left\{\begin{array}{cc}
I_{m} \operatorname{Sin} \omega t & \text { For } 0 \leq \omega t \leq \pi \\
0 & \text { For } \pi \leq \omega t \leq 2 \pi
\end{array}\right\}
$$

Where, $I_{n}=$ Maximum value of the current; $\quad=\frac{V_{m}}{R_{F}+R_{L}}$
Where, $R_{F}$-Forward dynamic resistance of diode; $R_{L}$-Load resistance.

## Input and output waveforms:



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(a) Average or DC value of output current ( $I_{d c}$ ):

Average value $=($ Area under the curve $/$ Period $)$

$$
\begin{gathered}
\mathrm{Idc}=\frac{1}{\pi} \int_{0}^{\pi} \mathrm{id}(\omega \mathrm{t}) \\
\mathrm{I}_{\mathrm{dc}}={\underset{\sim}{\pi}}_{1}^{\pi}[-\cos \omega \mathrm{t}]_{0}^{\pi}=\frac{1}{\mathrm{I}_{\mathrm{m}}}=\frac{1}{\pi}\left[\int_{0}^{\pi}[-\cos \pi-(-\cos 0)]=\frac{\mathrm{I}_{\mathrm{m}}}{\pi}[-(-1)-(-1)]=\frac{2 \mathrm{I}_{\mathrm{m}}}{\pi}\right. \\
\mathrm{I}_{\mathrm{dc}}=\frac{2 \mathrm{~V}_{\mathrm{m}}}{\pi\left(\mathrm{R}_{\mathrm{F}}+\mathrm{R}_{\mathrm{L}}\right)}
\end{gathered}
$$

(b) Average or DC value of output voltage ( $\mathbf{V}_{\mathrm{dc}}$ ) :

$$
\mathrm{V}_{\mathrm{dc}}=\frac{2 \mathrm{Im}}{\pi} \times \mathrm{R}_{\mathrm{L}}=\frac{2 \mathrm{~V}_{\mathrm{m}}}{\pi}
$$

(c) RMS value of output current (Irms):

$$
\begin{aligned}
& =\sqrt{\frac{\mathrm{I}_{\mathrm{m}}{ }^{2}}{2 \pi} \int_{0}^{\pi} \mathrm{d}(\omega \mathrm{t})-\int_{0}^{\pi} \cos 2(\omega \mathrm{t}) * \mathrm{~d}(\omega \mathrm{t})}=\sqrt{\left.\frac{\mathrm{I}_{\mathrm{m}}{ }^{2}\left[\omega \mathrm{t}^{\pi}-\left(\left(_{2 \pi}^{\sin 2 \omega \mathrm{t}}\right)^{\pi}\right.\right.}{2}{ }_{0}\right]} \\
& =\sqrt{\frac{\sqrt{\mathrm{I}_{\mathrm{m}}{ }^{2}}\left[(\pi-0)-\left(\frac{\sin 2 \pi}{2 \pi}-\frac{\sin 0}{2}\right)\right]}{2}=\frac{\sqrt{\mathrm{I}_{\mathrm{m}}^{2}}[(\pi-0)-0]}{2 \pi}=\sqrt{\frac{\sqrt{\mathrm{Im}^{2}}}{2}}=\frac{\mathrm{Im}}{\sqrt{2}}, ~(\pi)}
\end{aligned}
$$

(d) Rectification Efficiency ( $\boldsymbol{\eta}$ ):

(e) Ripple Factor ( $\gamma$ ):

$$
y=\frac{\text { RMS value of Ac component }}{\text { Dc value of wave }}=\sqrt{\left(\frac{\mathrm{rms}^{2}}{\mathrm{I}_{\mathrm{dc}}}\right)^{2}-1}=\sqrt{\left(\frac{{ }_{\mathrm{m}} / \sqrt{Z}{ }^{2}}{2 \mathrm{I}_{\mathrm{m}} / \pi}\right)^{-1}-1}=\sqrt{\frac{\pi^{2}}{8}-1}=\mathbf{0 . 4 8}
$$

## (f) Peak inverse Voltage (PIV):

Peak inverse voltage is the maximum possible voltage across a diode when it is not conducting. During positive half cycle of the AC input voltage Diode D1, is conducting and Diode D, is not conducting. In this case a voltage V , is developed across the load resistor $\mathrm{R}_{1}$. Now the voltage across the non-conducting Diode D, is the sum of the voltage across R1 and voltage across the lower half of transformer secondary $\mathrm{V}_{\mathrm{m}}$.
Hence, PIV of Diode D2 $=\mathrm{V}_{\mathrm{m}}+\mathrm{V}_{\mathrm{m}}=2 \mathrm{~V}_{\mathrm{m}}$ Similary, PIV of Diode D1 $=\mathrm{V}_{\mathrm{m}}+\mathrm{V}_{\mathrm{m}}=2 \mathrm{~V}_{\mathrm{m}}$

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## Advantages:

1. The D.c load voltage and current are more than halfwave.
2. No D.c current thro transformer windings hence no possibility of saturation.
3. TUF is better.
4. Efficiency is higher.
5. Ripple factor less.

## Disadvantages:

1. PIV rating of diode is higher
2. Higher PIV diodes are larger in size ad costlier.
3. Cost of transformer is high.

## Rectifiers - Full Wave Bridge type

6. (a) Draw the circuit diagram and explain the working of full wave bridge rectifier $\&$ derive the expansion for average amount current \& rectification efficiency. (May 2017) (Nov/Dec 2017) (Nov/Dec 2018)

## Bridge rectifier (Full Wave Bridge rectifier):

Another type of circuit that produces the same output waveform as the full wave rectifier circuit above is that of the Full Wave Bridge Rectifier. This type of single-phase rectifier uses four individual rectifying diodes connected in a closed loop "bridge" configuration to produce the desired output. The main advantage of this bridge circuit is that it does not require a special center tapped transformer, thereby reducing its size and cost. The single secondary winding is connected to one side of the diode bridge network and the load to the other side as shown below.


The four diodes labeled D1 to D4 are arranged in "series pairs" with only two diodes conducting current during each half cycle. During the positive half cycle of the supply, diodes D1 and D2 conduct in series while diodes D3 and D4 are reverse biased and the current flows through the load as shown below.

During the negative half cycle of the supply, diodes D3 and D4 conduct in series, but diodes D1 and D 2 switch of as they are now reverse biased. The current flowing through the load is the same direction as before. As the current flowing through the load is unidirectional, so the voltage developed across the load is also unidirectional the same as for the previous two diode full-wave rectifier.

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Positive half cycle


Negative half cycle

## Waveform:



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## Analysis of Full Wave Rectifier:

Let Vi be the input voltage to the rectifier,

$$
V_{i}=V_{m} \sin \omega t
$$

Where,
$V_{m}=$ Maximum value of the input voltage.
Let I be the current flowing though the circuit when the diode is conducting.

$$
i=\left\{\begin{array}{cc}
I_{m} \sin \omega t & \text { For } 0 \leq \omega t \leq \pi \\
0 & \text { For } \pi \leq \omega t \leq 2 \pi
\end{array}\right\}
$$

Where

$$
\begin{aligned}
& I_{m}=\text { Maximum value of the current } \\
& \qquad I_{m}=\frac{V_{m}}{R_{F}+R_{L}}
\end{aligned}
$$

Where, $R_{F}$-Forward dynamic resistance of diode; $R_{L}$-Load resistance.
(a) Average or DC value of output current ( $\mathrm{I}_{\mathrm{dc}}$ ):

Average value $=($ Area under the curve $/$ Period $)$

$$
\begin{gathered}
\mathrm{I}_{\mathrm{dc}}=\frac{1}{\pi} \int_{0}^{\pi} \mathrm{id}(\omega \mathrm{t}) \quad \quad \mathrm{I}_{\mathrm{dc}}=\frac{1}{\pi}\left[\int_{0}^{\pi} \mathrm{I}_{\mathrm{m}} * \sin \omega \mathrm{t} \mathrm{~d}(\omega \mathrm{t})\right] \\
\mathrm{I}_{\mathrm{dc}}=\frac{1}{\pi}[-\cos \omega \mathrm{t}]_{0}^{\pi}=\frac{\mathrm{I}_{\mathrm{m}}}{\pi}[-\cos \pi-(-\cos 0)]=\frac{\mathrm{I}_{\mathrm{m}}}{\pi}[-(-1)-(-1)]=\frac{2 \mathrm{I}_{\mathrm{m}}}{\pi} \\
\mathrm{I}_{\mathrm{dc}}=\frac{2 \mathrm{~V}_{\mathrm{m}}}{\pi\left(\mathrm{R}_{\mathrm{F}}+\mathrm{R}_{\mathrm{L}}\right)}
\end{gathered}
$$

(b) Average or DC value of output voltage ( $\mathbf{V}_{\mathrm{dc}}$ ): $\quad \mathrm{V}_{\mathrm{dc}}=\frac{2 \mathrm{I}_{\mathrm{m}}}{\pi} \times \mathrm{R}_{\mathrm{L}}=\frac{2 \mathrm{~V}_{\mathrm{m}}}{\pi}$
(c) RMS value of output current ( $\mathrm{I}_{\mathrm{rms}}$ ):

$$
\begin{aligned}
& \boldsymbol{I}_{r m s}=\sqrt{\frac{1}{\pi} \int_{0}^{\pi} \mathrm{i}^{2} \mathrm{~d}(\omega \mathrm{t})}=\sqrt{\frac{1}{\pi} \int_{0}^{\pi} \mathrm{Im}^{2} \sin ^{2} \omega \mathrm{t} * \mathrm{~d}(\omega \mathrm{t})}=\sqrt{\frac{\mathrm{I}_{\mathrm{m}}{ }^{2}}{\pi} \int_{0}^{\pi}\left(\frac{1-\cos 2 \omega \mathrm{t}}{2}\right) * \mathrm{~d}(\omega \mathrm{t})} \\
& =\sqrt{\frac{\mathrm{I}_{\mathrm{m}}^{2}}{2 \pi} \int_{0}^{\pi} \mathrm{d}(\omega \mathrm{t})-\int_{0}^{\pi} \cos 2(\omega \mathrm{t}) * \mathrm{~d}(\omega \mathrm{t})}=\sqrt{\left.\left.\frac{\mathrm{I}_{\mathrm{m}}^{2}\left[\omega \mathrm{t}^{\pi}-\left(\mathrm{c}_{0}^{\sin 2 \omega \mathrm{t}^{\pi}}\right.\right.}{2 \pi}\right)_{0}^{\pi}\right]} \\
& =\sqrt{\frac{\sqrt{\mathrm{I}_{\mathrm{m}}{ }^{2}}}{2 \pi}\left[(\pi-0)-\left(\frac{\sin 2 \pi}{2}-\frac{\sin 0}{2}\right)\right]}=\frac{\sqrt{\mathrm{I}_{\mathrm{m}}{ }^{2}}[(\pi-0)-0]}{2 \pi}=\sqrt{\frac{\sqrt{\mathrm{Im}^{2}}}{2}}=\frac{\mathrm{I}_{\mathrm{m}}}{\sqrt{2}}
\end{aligned}
$$

## (d) Rectification Efficiency ( $\boldsymbol{\eta}$ ):


(e) Ripple Factor ( $\gamma$ ):

$$
y=\frac{\text { RMS value of Ac component }}{\text { Dc value of wave }}=\sqrt{\left(\frac{\mathrm{rms}}{\mathrm{I}_{\mathrm{dc}}}\right)^{2}-1}=\sqrt{\left(\frac{\mathrm{I}_{\mathrm{m}} / \sqrt{Z}{ }^{2}}{2 \mathrm{I}_{\mathrm{m}} / \pi}\right)^{-1}}=\sqrt{\frac{\pi^{2}}{8}-1}=\mathbf{0 . 4 8}
$$

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(f) Peak inverse Voltage (PIV):

Peak inverse voltage is the maximum possible voltage across a diode when it is not
Conducting. During positive half cycle of the AC input voltage Diode D1, is conducting and Diode D, is not conducting. In this case a voltage V , is developed across the load resistor $\mathrm{R}_{1}$. Now the voltage across the non-conducting Diode D , is the sum of the voltage across R1 and voltage across the lower half of transformer secondary $\mathrm{V}_{\mathrm{m}}$.
Hence, PIV of Diode $\mathrm{D} 2=\mathrm{V}_{\mathrm{m}}+\mathrm{V}_{\mathrm{m}}=2 \mathrm{~V}_{\mathrm{m}}$
Similary, PIV of Diode D1 $=\mathrm{V}_{\mathrm{m}}+\mathrm{V}_{\mathrm{m}}=2 \mathrm{~V}_{\mathrm{m}}$

## Advantages:

1. The D.c load voltage and current are more than half wave.
2. No D.c current thro transformer windings hence no possibility of saturation.
3. TUF is better.
4. Efficiency is higher.
5. Ripple factor less.
6. No centre tapped is required.

## Disadvantages:

4 diodes are used therefore voltage drop across the diode is increased. This reduces output voltage.

## Applications:

1. In power supply circuits.
2. Used as rectifier in power circuits to convert A.C to D.C
(b) In a bridge rectifier circuit, input supply is $230 \mathrm{~V}, 50 \mathrm{~Hz}$. Primary to secondary turns ratio is $4: 1$, load resistance is $200 \Omega$. The diodes are ideal. Find DC output voltage, PIV and output signal frequency. (Nov / Dec 2018-R17)
Solution: $\quad E_{p y}(r m s)=230 V,{ }_{N_{1}}^{\frac{N_{2}}{1}}=\underset{-}{1}, R_{L}=200 \Omega \quad R_{f}=R_{s}=0 \Omega$ as ideal
$\frac{E_{p y}(r m s)}{E_{s y}(r m s)}=\frac{N_{1}}{N_{2}}, E_{s y}(r m s)=\frac{N_{1}}{N_{2}} X \underset{p y}{E}(r m s)=\frac{1}{4} X 230=57.5 \mathrm{~V}$,

$I_{m}=\frac{E_{s m}}{R_{s}+2 R_{f}+R_{L}}=\frac{81.31}{200}=0.4065 A_{D C}=\frac{2 I_{m}}{\pi}=\frac{2 X 0.4065}{\pi}=0.2587 \mathrm{~A}$
$E_{D C}=I_{D C} R_{L}=0.2587 \times 200=51.74 V$
PIV $=E_{s m}=81.31 \mathrm{~V} \quad$ (for full wave rectifier)
Output signal frequency $=2 \mathrm{f}_{\mathrm{s}}=2 \times 50=100 \mathrm{~Hz}$
Ripple Factor (for Full Bridge Rectifier) $=\mathbf{0 . 4 8 2}$,

$$
\text { Ripple Factor }=\frac{\text { AC rms output }}{D C \text { output }}=\frac{\text { Ripple Voltage }}{E_{D C}} \quad 0.482=\frac{\text { Ripple Voltage }}{51.74}
$$

i.e. Ripple voltage $=\mathbf{5 1 . 7 4} \mathbf{X} \mathbf{0 . 4 8 2}=\mathbf{2 4 . 9 4} \mathrm{V}$

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## 7. Compare different types of rectifiers?

| Type | HW | CT FW | FW BR |
| :--- | :---: | :---: | :---: |
| No of diodes used | 1 | 2 | 4 |
| Need of transformer | Not necessary | Necessary | Not necessary |
| Ripple factor | 1.21 | 0.48 | 0.48 |
| Efficiency | $40.6 \%$ | $81.2 \%$ | $81.2 \%$ |
| PIV | $\mathrm{V}_{\mathrm{m}}$ | $2 \mathrm{~V}_{\mathrm{m}}$ | $\mathrm{V}_{\mathrm{m}}$ |
| TUF | 0.287 | 0.812 | 0.693 |
| From factor | 1.57 | 1.11 | 1.11 |
| Peak factor | 2 | $\sqrt{2}$ | $\sqrt{2}$ |
| Ripple frequency | f | 2 f | 2 f |

## Display devices- LED

8. Discuss the working principle, characteristics and application of LED in detail. (NOV/DEC 2012) (Apr/May 2018)
Explain the principle and operation of light emitting diode (LED) with necessary expressions for current densities and efficiency of light generation. (April / May 2019-R17)

A light-emitting diode(LED) is a semiconductor light source LEDs are used as indicator lamps in many devices and are increasingly used for other lighting. Introduced as a practical electronic component in 1962, early LEDs emitted low-intensity red light, but modern versions are available across the visible, ultraviolet, and infrared wavelengths, with very high brightness.

When a light-emitting diode is forward-biased (switched on), electrons are able to recombine with electron holes within the device, releasing energy in the form of photons. This effect is called electroluminescence and the color of the light (corresponding to the energy of the photon) is determined by the energy gap of the semiconductor.

LEDs are often small in area (less than $1 \mathrm{~mm}^{2}$ ), and integrated optical components may be used to shape its radiation pattern. ${ }^{[5]}$ LEDs present many advantages over incandescent light sources including lower energy consumption, longer lifetime, improved robustness, smaller size, and faster switching. LEDs powerful enough for room lighting are relatively expensive and require more precise current and heat management than compact fluorescent lamp sources of comparable output.

Light Emitting Diodes are made from exotic semiconductor compounds such as Gallium Arsenide (GaAs), Gallium Phosphide (GaP), Gallium Arsenide Phosphide (GaAsP), Silicon Carbide ( SiC ) or Gallium Indium Nitride (GaInN) all mixed together at different ratios to produce a distinct wavelength of colour.

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Different LED compounds emit light in specific regions of the visible light spectrum and therefore produce different intensity levels.

- Gallium Arsenide Phosphide (GaAsP) - red to infra-red, orange
- Aluminium Gallium Arsenide Phosphide (AlGaAsP) - high-brightness red, orange-red, orange, and yellow
- Gallium Phosphide (GaP) - red, yellow and green
- Aluminium Gallium Phosphide (AlGaP) - green
- Gallium Nitride ( GaN ) - green, emerald green
- Gallium Indium Nitride (GaInN) - near ultraviolet, bluish-green and blue
- Silicon Carbide (SiC) - blue as a substrate
- Zinc Selenide (ZnSe) - blue
- Aluminium Gallium Nitride (AlGaN) - ultraviolet


Light-emitting diodes are used in applications as diverse as aviation lighting, automotive lighting, advertising, general lighting, and traffic signals. LEDs have allowed new text, video displays, live video, and sensors to be developed, while their high switching rates are also useful in advanced communications technology. Infrared LEDs are also used in the remote control units of many commercial products including televisions, DVD players, and other domestic appliances.

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## Laser diodes

## 9. Explain in detail about LASER DIODE? (May / June 2016) (April/May 2018)

The term laser comes from the acronym for light amplification for stimulated emission of radiation. The laser medium can be a gas, liquid, amorphous solid or semiconductor.

## Laser Action

The light travelling through a semiconductor, then a single photon is able to generate an identical second photon. This photon multiplication is the key physical mechanism of lasing. The carrier inversion is the first requirement of lasing. It is achieved at the PN junction by providing the conduction bandwith electrons from the N -doped side and the valence band with holes from the P -doped side as shown in Fig. The photon energy is given by the band gap, which depends on the semiconductor material. The optical feedback and the confinement of photon in an optical resonator are the second basic requirement of lasing.


## PN Homojunction Laser

It has the material GaAs on both sides of the junction. A pair of parallel planes perpendicular to the plane of the junction are cleared and polished under appropriate biasing in off condition, laser light is emitted from these planes. The other two sides are deliberately roughened to prevent lasing in those directions. Such a cavity is called a Fabryperot resonant cavity with a typical cavity length of $300 \mid$ J.m. It is a thin layer of material with a narrow band gap. GaAs is sandwiched between layers of a material with band gap. This is usually realized by epitaxy. In such a structure the carrier are better confined in the active region due to the heterojunction barriers. Optical confinement is also better in $\boldsymbol{D H}$ laser. The propagation of the electromagnetic radiation is confined in a direction parallel to the


Fig. 4.28
layer interface. The current density required for lasing in lower for $\boldsymbol{D H}$ lasers compared to homojunction lasers. The double preferred for continuous operation at room temperature.

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Double Hetrostructure Laser


## Characteristics of Laser Diode

The Ideal light output against current characteristics for semiconductor laser is shown in Fig.4.28. The solid line represents the laser characteristics. It may be observed that the device gives low light output in the region, the threshold with corresponds to spontaneous emission only within the structure. After the threshold current value the light output increases substantially for small increases in current through the device.

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## ZENER DIODE

10. Explain the construction \& working principle of Zener diode.

Explain the Break down mechanisms in semiconductor devices. (May/June 2016), (Nov / Dec 2015) (OR) Explain the Concept of Zener Breakdown and its VI characteristics. (Nov/Dec 2018-R-13)

## ZENER DIODE:

The Zener Diode is a PN junction semiconductor device.
It is fabricated with precise breakdown voltages, by controlling the doping level during manufacturing. Practically, Zener Diodes are operated in reverse biased mode.


Fig. 20 Zener Diode
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## CHARACTERISITCS OF ZENER DIODE:

## FORWARD CHARACTERISITCS:

In forward biased condition, the normal rectifier diode and the Zener diode operate in similar fashion.
(Refer: PN diode forward characteristics)

## Zener reverse characteristics

## REVERSE CHARACTERISITCS:

Zener diode is designed to operate in the reverse biased condition.
In reverse biased condition, the diode carries reverse saturation current till the reverse voltage applied is less than the reverse breakdown voltage.

When the reverse voltage exceeds reverse breakdown voltage, the current through it changes drastically but the voltage across it remains almost constant.

Such a breakdown region is a normal operating region for a Zener diode.
The normal operating regions for both diode and Zener are shown in below Fig.

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(a) Operating regions shown shaded for normal diode

(b) Operating region shown shaded for zener diode

Fig. The normal operating region for a rectifier diode and Zener diode
When the applied reverse voltage is increased then, the current through it is very small (few $\mu \mathrm{A}$ ) and it is called Reverse Leakage Current ( $\mathrm{I}_{\mathbf{0}}$ )
At certain reverse voltage, the current will increase rapidly. The breakdown occurs and the current at this point (knee or Zener knee) is called Zener knee current ( $I_{Z K}$ or $I_{Z \text { min }}$ ).
Zener knee current is the minimum Zener current which is must to carry out the operate in Reverse Breakdown Region.
The reverse voltage at which the breakdown occurs is called Zener Breakdown Voltage or Zener Voltage ( $V_{Z}$ ). The $V_{Z}$ is set by controlling the doping level during manufacturing process.

Below the knee, the reverse breakdown voltage increases slightly as Zener current ( $\mathrm{I}_{z}$ ) increases but, remains almost CONSTANT.
The current at which the nominal Zener breakdown voltage is specified is called Zener Test Current ( $\boldsymbol{I}_{Z T}$ ).
As the current increases, the power dissipation $\left(\mathrm{P}_{\mathrm{Z}}=\mathrm{V}_{\mathrm{Z}} \mathrm{I}_{\mathrm{Z}}\right)$ will be increased and if this power dissipation is increased beyond a certain current value, the Zener diode may get damaged. So, there is a maximum current that a Zener diode can carry safely is called Zener Maximum Current ( $\boldsymbol{I}_{\text {Zм }}$ or $\boldsymbol{I}_{\text {Zmax }}$ ).

In practical circuits, a current limiting resistor is used in series with Zener diode in order to limit the current between $\mathrm{I}_{\mathrm{Zmin}}$ to $\mathrm{I}_{\mathrm{Zmax}}$.

The complete VI characteristics of Zener Diode is shown in Fig.


Fig. VI characteristics of Zener Diode

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## EQUIVALENT CIRCUIT OF ZENER DIODE:

When the breakdown occurs then Iz may increase from $I_{Z \min }$ to $I_{Z m a x}$ but voltage across Zener remains almost constant. The internal impedance decreases as current increases in Zener region. But this impedance is very small and hence ideally Zener diode is indicated by a battery of voltage $\mathrm{V}_{\mathrm{Z}}$. This $\mathrm{V}_{\mathrm{Z}}$ remains almost constant in the Zener region which is shown in Fig.


Fig. Ideal equivalent circuit of Zener diode
In practical circuit, the Zener internal resistance is to be considered (even though it is very small) and called as Zener Dynamic Resistance $\boldsymbol{Z}_{\mathbf{Z}}$. Due to this resistance the Zener region is not exactly vertical, i.e., for the small change in the Zener current $\Delta \mathrm{I}_{\mathrm{z}}$ produces a small change in Zener voltage $\Delta \mathrm{V}_{\mathrm{z}}$. The ratio of $\mathrm{V}_{\mathrm{Z}}$ to $\mathrm{I}_{\mathrm{Z}}$ is called Zener resistance $\mathbf{Z}_{\mathrm{Z}}$.
Hence, the practical Zener diode equivalent circuit should be indicated with a battery of $\mathrm{V}_{\mathrm{Z}}$ along with series resistance $\mathrm{Z}_{\mathrm{z}}$ as shown in Fig.

Dynamic Resistance, $Z_{Z}=\frac{\Delta V_{Z}}{\Delta I_{Z}}=\frac{1}{\left[\frac{\Delta I_{Z}}{\Delta V_{Z}}\right]}$

$$
Z_{Z}=\frac{1}{[\text { slope of the reverse characteristics in zener region }]}
$$


(a) Dynamic resistance

(b) A.C. equivalent circuit

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## BREAKDOWN MECHANISM IN ZENER DIODE:

Two distinct breakdown mechanism:
$\checkmark$ Zener Breakdown
$\checkmark$ Avalanche Breakdown
For devices with breakdown voltage less than 5V-Zener Breakdown
For devices with breakdown voltage between 5V and 8V - Zener Breakdown and Avalanche Breakdown
For devices with breakdown voltage above $8 V$ - Avalanche Breakdown

## ZENER BREAKDOWN:

Zener breakdown occurs at Reverse biased condition because of heavy doping;
Practically, Zener breakdown is observed in the Zener diodes with breakdown voltage less than 6 V .
In Zener breakdown, the value of the breakdown voltage decreases as PN junction temperature increases, i.e. Negative Temperature Coefficient (NTC)

For applied reverse biased voltage of less than 6 V causes a high magnitude electric field ( $3 \times 10^{5} \mathrm{~V} / \mathrm{cm}$ ) across the depletion region, at the PN junction.
This electric field applies a large force on the valence electron of the atom, tending it to separate them from their respective nuclei. Electron-hole pairs are generated in large numbers and there will be a sudden increase in current. (To limit this current, a current limiting resistor is used in order to protect the Zener diode from being destroyed because of excessive heating at the junction)


## AVALANCHE BREAKDOWN:

Avalanche Breakdown occurs at Reverse biased condition due to ionization of electron and hole pairs Practically, Avalanche breakdown is observed in the Zener diodes with breakdown voltage greater than 6 V . In avalanche breakdown, the value of the breakdown voltage increases as $P N$ junction temperature increases, i.e. Positive Temperature Coefficient (PTC)

For applied reverse biased voltage of greater than 6 V causes increased acceleration of minority charge particles. Thus, collision between accelerated charge particles with high velocity and kinetic energy with adjacent atom is involved in breaking the covalent bonds of the crystal structure. This process is called Carrier Multiplication.


At this stage, junction is said to be in breakdown and current starts increasing rapidly. To limit this current below $I_{\text {Zmax }}$, a current limiting resistor is necessary.


Fig. Breakdown Mechanism in Zener Diode

## ZENER AS REGULATOR

11. (a) Explain the working of a Zener diode as a regulator? (May 2017) (Nov/Dec 2017) (Nov/Dec 2018-R17)

The Zener Diode is used to regulate the Load Voltage. Here, the Zener is used in reverse biased condition.


Fig. Zener Diode as a shunt regulator
\{Under reverse biased condition, the current through the zener diode is very small of the order of few $\mu \mathrm{A}$, up to certain limit. When enough reverse bias voltage is applied, electrical breakdown occurs and large current flows through the zener diode. The voltage at which the breakdown occurs is called Zener Voltage ( $\mathrm{V}_{\mathrm{z}}$ ).


Fig. VI characteristics of Zener Diode

Under this condition, whatever may be the current, the voltage across the Zener is constant and equal to Vz \}

Since, voltage across the Zener Diode is CONSTANT \& equal to $V_{z}$, it is connected across the load. $\therefore$ The Load Voltage (Vo) is equal to Zener Voltage ( $V_{z}$ ).
i.e. The Zener Diode acts as an ideal voltage source which maintains a constant load voltage, independent of the current.

## REGULATION WITH VARYING input voltage (Line Regulation)

Zener Regulator under varying input voltage condition is shown in Fig.

$$
\begin{aligned}
& \\
& \\
& \\
& \\
& \mathrm{I}_{\mathrm{L}}=\frac{V_{O}}{R_{L}}=\frac{V_{Z} \text { is constant }}{R_{Z}}=\text { constant } \\
& \text { And } I \\
& I=I_{Z}+I_{L}
\end{aligned}
$$



Fig. Varying input condition


As long $I_{z}$ is between $I_{z \min }$ and $I_{z \max }$, the $V_{z}$ i.e. output voltage $V_{0}$ is constant. Thus, the changes in the input voltage is get compensated and output is maintained constant.
The maximum power dissipation for the zener diode is fixed, $\quad \boldsymbol{P}_{\boldsymbol{D}}=\boldsymbol{V}_{\boldsymbol{Z}} \boldsymbol{I}_{\boldsymbol{Z m a x}}$

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## REGULATION WITH VARYING LOAD (Load Regulation)

Zener Regulator under varying load condition ( $\mathrm{R}_{\mathrm{L}}$ is variable) and constant input voltage ( $\mathrm{V}_{\text {in }}$ is constant) is shown in Fig.


Fig. Varying load condition
$\mathbf{V}_{\mathbf{o}}=\mathbf{V}_{\mathbf{z}}$ is constant and $\mathbf{V}_{\text {in }}$ is Constant, then for constant R, the current (I) is constant.

$$
\underline{\underline{V}}_{\underline{i n}-V_{\underline{Z}}}^{=} \quad \text { (constant); } \quad \mathrm{I}=\ell+I_{Z}
$$

| $\mathrm{R}_{\mathrm{L}}$ increases <br> $\mathrm{I}_{\mathrm{L}}$ decreases | $\Rightarrow$ | $\begin{aligned} & I=\frac{V_{\text {in }}-V_{z}}{R} \\ & \text { constant } \end{aligned}$ | $\Rightarrow$ | ${ }_{\text {increases }}^{\mathrm{I}_{\mathrm{L}}}$ | $\Rightarrow$ | As long $\mathrm{I}_{\mathrm{Z}}<\mathrm{I}_{\mathrm{Zmax}}$ $V_{Z}$ is constant i.e. output voltage is constant |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{R}_{\mathrm{L}}$ decreases $\mathrm{I}_{\mathrm{L}}$ increases |  | $\begin{aligned} & I=\frac{R}{R} \\ & \text { constant } \end{aligned}$ | $\Rightarrow$ | $\begin{aligned} & \mathrm{I}_{\text {decreases }}=\mathrm{I}-\mathrm{I}_{\mathrm{L}} \end{aligned}$ | $\Rightarrow$ | As long $\mathrm{I}_{\mathrm{z}}>\mathrm{I}_{\mathrm{zmin}}, \mathrm{V}_{\mathrm{z}}$ is coltage is constant |

As long $I_{z}$ is between $I_{\text {min }}$ and $I_{z \max }$, the $\mathrm{V}_{\text {zi.e. }}$ output voltage $\mathrm{V}_{0}$ is constant. Thus, the changes in the load is get compensated and output is maintained constant.
(b) For the following circuit, find the maximum and minimum values of Zener diode current. (Nov/Dec 2018 -R17)


Solution: $V_{\text {in }(\text { min })}=80 \mathrm{~V}, V_{\text {in }(\max )}=120 \mathrm{~V}, V_{Z}=50 \mathrm{~V}, R_{L}=10 \mathrm{~K} \Omega, \quad R=5 \mathrm{~K} \Omega$
$I_{L}=\frac{V_{Z}}{R_{\mathrm{L}}}=\frac{50}{10 \times 10^{3}}=5 \times 10^{-3}=5 \mathrm{~mA}$
$V_{\text {in }(\text { min })}=V_{Z}+I R V_{\text {in }(\max )}=V_{Z}+I R$
$I=\frac{V_{i n(\min )}-V_{Z}}{R} I=\frac{V_{i n(\max )}-V_{Z}}{R}$
$I_{(\text {min })}=\frac{80-50}{5 \times 10^{3}}=6 m A I_{(\max )}=\frac{120-50}{5 \times 10^{3}}=14 m A$
$I_{Z(\text { min })}=I_{(\text {min })}-I_{L}$
$I_{Z(\text { min })}=6 \times 10^{-3}-5 \times 10^{-3}=1 m A$
$\therefore$ Minimum zener current, $I_{(\text {min })}=1 m A$
$I_{Z(\max )}=I_{(\max )}-I_{L}$
$I_{Z_{(\max )}}=14 \times 10^{-3}-5 \times 10^{-3}=9 m A$
$\therefore$ Maximum zener current, $I_{z(\max )}=\mathbf{9 m A}$

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## Problems: (Anna University Exam - Solved Problems)

1. For the zener regulator shown in Fig. 5, calculate the range of input voltage for which output will remain constant.

$$
I_{Z(\min )}=2.5 m A, \quad I_{Z(\max )}=25 m A, \quad V_{Z}=6.1 V, \quad r_{Z}=0 K \Omega
$$



## Solution:

$$
\begin{aligned}
& I_{Z(\min )}=2.5 \mathrm{~mA}, I_{Z(\min )}=25 \mathrm{~mA}, \quad V_{Z}=6.1 \mathrm{~V}, \quad r_{Z}=0 \mathrm{~K} \Omega, \quad R=2.2 \mathrm{~K} \Omega, \quad R_{L}=1 \mathrm{~K} \Omega \\
& I_{L}=\frac{V_{Z}}{R_{\mathrm{L}}}=\frac{6.1}{1 \times 10^{3}}=6.1 \times 10^{-3}=6.1 \mathrm{~mA} \quad(\text { CONSTANT }) \\
& \text { For } V_{\text {in }(\min )} ; \quad I_{(\min )}=I_{Z(\min )}+I_{L} \quad \text { For } V_{\text {in }(\operatorname{mzx})} ; \quad I_{(\max )}=I_{Z(\max )}+I_{L} \\
& I=2.5 \times 10^{-3}+6.1 \times 10^{-3}=8.6 \mathrm{~mA} \quad I=25 \times 10^{-3}+6.1 \times 10^{-3}=31.1 \mathrm{~mA} \\
& V_{\text {in }(\text { min })}=V_{Z}+I R V_{\text {in }(\max )}=V_{Z}+I R \\
& V_{\text {in }(\text { min })}=6.1+8.6 \times 10^{-3} \times 2.2 \times 10^{-3}=25.02 \mathrm{~V} \quad V_{\text {in }(\text { min })}=6.1+31.1 \times 10^{-3} \times 2.2 \times 10^{-3}=74.52 \mathrm{~V} \\
& \therefore V_{\text {in (min) }}=25.02 V \quad \therefore V_{\text {in }}^{(\max )}=74.52 V
\end{aligned}
$$

2. A silicon diode has a saturation current $7.5 \mu$ A at room temperature 300 K .Find the saturation current at 400k. $\mathrm{I}_{01}=7.5 \times 10-6$ A at $\mathrm{T}_{1}=300^{\circ} \mathrm{K}=27^{\circ} \mathrm{C}$ and $\mathrm{T}_{2}=400^{\circ} \mathrm{K}=127^{\circ} \mathrm{C}$. (Nov/Dec 2016-R13) Solution: The saturation current at $400^{\circ} \mathrm{K}$ is
$I_{02}=I_{01} \times 2^{\frac{\Delta T}{10}}=7.5 \times 10^{-6} \times 2^{(127-27) / 10}=7.68 \mathrm{~mA}$
3. Find the current $I$ in the following circuit. (Nov/Dec 2017 - R13)


Assume the diodes to be of silicon and forward resistance of diodes to be zero.
$\mathrm{I}=(\mathrm{E} 1-\mathrm{E} 2) / \mathrm{R}$
$\mathrm{I}=(24-4) / 2000$
$\mathrm{I}=1 \mathrm{~mA}$

## Current I is 1 mA .

4. An AC voltage of peak value 20 V is connected in series with a silicon diode and load resistance of $500 \Omega$. If the forward resistance of diode is $10 \Omega$ find the peak current through the diode. (Nov/Dec 2018-R17)
Solution: $E_{m}=20 \mathrm{~V}, \quad R_{L}=500 \Omega, \quad R_{f}=10 \Omega$

$$
\begin{aligned}
I_{m} & =\frac{E_{m}}{R_{f}+R} \quad I_{m}=\frac{20}{500+10} \\
& \therefore I_{m}=39.22 m A
\end{aligned}
$$

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5. (a) Determine the peak output voltage of a half wave rectifier, if the diode has $\mathrm{V}_{\mathrm{F}}=$ 0.7 V and the AC input is 22V. (April / May 2019-R17)

Solution: $V_{p o}=V_{p i}-V_{F}$
$V_{F}=0.7 V$,
$V_{p i}=\sqrt{2} V_{i}=\sqrt{2} \times 22$,
$V_{p o}=31.1-0.7$,
$V_{p o}=30.4 \mathrm{~V}$

$$
V_{p i}=31.1 V
$$

(b) If load resistance is given as $500 \Omega$, calculate peak output current of the above given half wave rectifier.
Solution: $R_{L}=500 \Omega$

$$
I_{p}=\frac{V_{p o}}{R_{L}}=\frac{30.4}{500}
$$

$$
I_{p}=60.8 m A
$$

(c) Determine the diode peak reverse voltage (PIV).
$\mathrm{PIV}=V_{p i}=31.1 \mathrm{~V}$
6. What value of series resistor is required to limit the current through a LED to 20 mA with a forward voltage drop of 1.6 V when connected to a 10 V supply? (Nov/Dec 2017)
Series resistor, $R_{S}=\frac{V_{S}-V_{D}}{I_{F}}$

$$
V_{S}=10 \mathrm{~V} ; \quad V_{D}=1.6 \mathrm{~V} ; \quad I_{F}=20 \mathrm{~mA}=20 \times 10^{-3} \mathrm{~A}
$$

$$
\therefore \quad R_{S}=\frac{10-1.6}{20 \times 10^{-3}}=420 \Omega
$$

7. In a semiconductor at room temperature $\left(300^{\circ} \mathrm{K}\right)$, the intrinsic carrier concentration and resistivity are1.5 $* 10^{16} / \mathrm{cm}^{3}$ and $2 * 10^{3} \Omega$-mrespectively. It is to an extrinsic semiconductor with a doping concentration of $10^{20} / \mathrm{cm}^{3}$ for the extrinsic semiconductor.
Calculate (a) Majority carrier concentration, (b) Shift in fermilevel due to doping (c) Minority carrier concentration when its temperature is increased to a value at which the intrinsic concentration ' $n_{i}$ ' doubles. (NOV/DEC 2012)

Assume the mobility of majority and minority carriers are same and $\mathbf{K T = 2 6} \mathbf{~ m e T}$ at room temperature.
a) Minority carrier concentration= $\qquad$

$$
=\frac{\left(1.5 \times 10^{16}\right)}{10^{20}}=2.25 \times 10^{12} \frac{\text { atoms }}{\mathrm{m}^{3}}
$$

$$
\begin{gathered}
\text { We know } \sigma=\mathrm{nq}\left(\mu_{\mathrm{n}}+\mu_{\mathrm{p}}\right) \\
\operatorname{or}\left(\mu_{\mathrm{n}}+\mu_{\mathrm{p}}\right)=\frac{\sigma}{\mathrm{nq}}=\frac{1}{\rho \mathrm{nq}} \\
=\frac{1}{\left(2 \times 10^{3}\right)\left(1.5 \times 10^{16}\right)\left(1.6 \times 10^{-19}\right)}=\frac{1}{4.8}
\end{gathered}
$$

In this case the concentration of majority and minority carriers are same, thus

$$
\mu_{\mathrm{n}}+\mu_{\mathrm{p}}=2 \mu_{\mathrm{n}}=\frac{1}{4.8} \text { or } \mu_{\mathrm{n}}=\mathrm{o} .1042 \frac{\mathrm{~m}^{2}}{\text { Volt }-\mathrm{sec}}
$$

b) Because of doping concentration $\gg$ minority concentration conductivity.
$\sigma=\mathrm{qn} \mu_{\mathrm{n}}=\left(1.6 \times 10^{-19}\right)\left(10^{20}\right)(0.10242)=1.6672$
Thus resistivity $\mathrm{R}=\frac{1}{\sigma}=0.599 \Omega \mathrm{~cm}$
Shift interm level $\mathrm{E}_{\mathrm{F}}$ computed as follows
C) $E_{A}-E_{i}=K T \log e \frac{n_{0}}{n_{i}}=0.026 \log _{e}\left(\frac{10^{20}}{10^{16} \times 15}\right)$

$$
=0.229_{\mathrm{e}} \mathrm{~V}
$$



## Additional Questions: PART-A

1. Define valence electron.

Electrons that are in shells close to nucleus are tightly bounced to the atom and have low energy. Whereas electrons that are in shells farther from the nucleus have large energy and less tightly bound to the atom. Electrons with highest energy level exist in the outermost shell of an atom. These electrons determine the electrical and chemical characteristic of each particular type of atom. These electrons are known as valence electrons.

## 2. What is meant by energy band?

In a single isolated atom, the electron in any orbit possesses define energy. Due to an interaction between atoms the electrons in a particular orbit of one atom have slightly different energy levels from electrons in the same orbit of an adjoining atom. This is due to the fact that no two electrons see exactly the same pattern of surrounding charges. Since there are billions of electrons in any orbit, slightly different energy levels form a cluster or band known as energy band.
3. Define conduction band $\&$ valence band.

- The conduction band is defined as the range of energies possessed by conduction electrons.
- Valence band is defined as the range of energies possessed by valence electros.

4. What are conductors, Insulators and semiconductors?

- A conductor is a material, which easily allows the flow of electric current. The best conductors are copper, silver, gold and aluminum.
- An Insulator is a material that does not conduct electric current. In these materials valence electrons are tightly bound to the atoms.
- A semiconductor is a material that has an electrical conductivity that lies between conductors and insulators. A semiconductor in it's pure state is neither a good conductor not a good insulator. The most common semiconductors are silicon, Germanium, and carbon.

5. What are the classifications of semiconductors?

Semiconductors are classified as intrinsic and extrinsic semiconductors. A pure semiconductor is called intrinsic semiconductor. A doped semiconductor is called extrinsic semiconductor.
6. What is meant by doping? How the extrinsic semiconductors are classified?

The process of adding impurities to a semiconductor is known as doping.

- n-type semiconductor
- p-type semiconductor

7. How a $\boldsymbol{n}$-type semiconductor \& p-type semiconductor can be obtained?

- A n-type semiconductor can be obtained by adding pentavalent impurities to an intrinsic semiconductor. These are atoms with five valence electrons. Typical examples for pentavalent atoms are Arsenic. Phosphorous, Bismuth and Antimony.
- A p-type semiconductor can be obtained by adding trivalent impurities to an intrinsic semiconductor. These are atoms with three valence electrons. Typical examples for trivalent atoms are boron(B), indium (In) and gallium (Ga).

8. Define Fermi level.

Fermi level is the energy at which the probability of occupation by an electron is exactly 0.5 .
9. What is the energy band gap of silicon and Germanium at $300^{\circ} \mathrm{K}$ ?

For Germanium: $0.66_{\mathrm{e}}$ and for Silicon: $1.12_{\mathrm{e} v}$
10. What are the different types of voltage regulators?

Based on how regulating element is connected to the load, voltage regulators are classified as

- Series regulator
- Shunt regulator
- Switch-mode regulators or switched mode power supply (SMPS)


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## Additional Questions (PART-B)

1. Draw and explain the energy band diagram for the following
(i) conductors
(ii) Insulators
(iii) semiconductors

## Insulators:

The materials in which the condition band and valence bands are seperated by a wide energy gap ( $\approx 15 \mathrm{eV}$ ) as shown in figure.
A wide energy gap means that a large amount of energy is required, to free the electrons, by moving them from the valence band into the condition band ;
Since at room temperature, the valence electrons of an insulator do not have enough energy to jump in to the condition, therefore insulator do not have an ability to conduct current. Thus insulators have very high resistively (or extremely low conductivity) at room temperatures.
However if the temperature is raised, some of the valence electrons may acquire energy and jump in to the conduction band. It causes the resistively of insulators to decrease.Therefore an insulator have negative temperature co-efficient of resistance.

(a) Insulators

(b) Conductors

(c) Semiconductors

## Conductors :-

The materials in which conduction and valence bands overlap as shown in figure are called conductors. The overlapping indicates a large number of electrons available for conduction. Hence the application of a small amount of voltage results a large amount of current.

## Semiconductors :-

The materials, in which the conduction and valence bands are separeated by a small energy gap ( 1 eV ) as shown in figure are called semiconductors.
Silicon and germanium are the commonly used semiconductors.
A small energy gap means that a small amount of energy is required to free the elctrons by moving them from the valence band in to the conduction band.
The semiconductors behave 4 like insulators at 0 K , because no electrons are available in the conduction band.
If the temperature is further increased, more valence elctrons will acquire energy to jump into the conduction band.Thus like insulators, semiconductors also have negative temperature co-efficient of resistance. It means that conductivity of semiconductors increases with the increases tempertature.

## 2. Explain the classification of semi-conducteurs.

Classification of semi-conducteurs :-
Semiconductors are classified in to two types

- Intrinsic Semiconductors
- Exterinsic semi-conducteurs
$>$ n-type semi-conductor
$>$ p-type semi-conductor


## - Intrinsic seiconductor

A semiconductor in an extremely pure form is known as an intrinic semiconductor. An Intrinsic semiconductor, even at room temperature, hole-electron pairs all created. When electric field is applied across an semiconductor intrinisic semiconductor, the current conduction takes place by two process, namely by free electrons and holes.

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Free electrons are produced due to the breeding up of fome co-valent bonds by thermal energy. At the same time holes are created in the co-valent bond itself. When electric field is applied across the semi-conducteurs material electrons will move towards the positive terminal of supply, holes will move towards negative terminal of the supply.
Thus current conduction inside this intrinisic semiconductor material is due to movement of holes \& electrons.
But the current in the external wire is only because of electrons. Since while applying electric field, holes are attracted towards negative terminal. There one new electron is introduced. This electron will combine with the hole, thus cancelling them.

At the same time electrons are moving towards positive terminal, while leacing from this intrinisic material it leaves a hole. Again this holes are attracted towards negative terminal.

## - Extrinisic semiconductor :

The current conduction capability of intrinisic semiconductor is very low at rom temperature. So we can not use it in electric devices.
Hence the current conduction capability must be increased. This can be achieved by adding impurities to the intrinisic semiconductor. So that it become impurity semiconductor (or) Extrinisic semiconductor.The process of adding impurity is known as doping.

The amount \& type of impurities have to be closely controlled during the preparation of extrinisic semiconductor. Generally, for $10^{8}$ atoms of semiconductor, one impurity atom is added.
The purpose of adding impurity is to increase either the number of free electrons or holes in the semiconductor crystal. If the pentavalent impurity is adding to the semiconductor, a large number of free electrons are produced in the semiconductor.
On the other hand if the trivalent impurtiy is added it introdued large number of holes. Depending upon the type of impurity added, extrisic semiconductors are classified into
$>\mathrm{n}$ - type Semiconductor
$>\mathrm{p}$ - type Semiconductor
n-type Semiconductor :

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The number of free electrons in an instrinsic silicon can be increased by adding a pentavalent atom to it. These are atoms with five valence electrons. Typical example for pentavalent atoms are Arsenic, Phosphorous, Bismuth and Antimony.

Four of the pentavalent atoms valence electrons form covalent bond with the valence electrons of Silicon atom, leaving an extra electron. Since valence orbit cannot hold no more than eight electrons the extra electron becomes a conduction electron.


Crystal lattice of a Si atom displaced by arsenic atom


Fig. 1.12 Energy band diagram d a $n$-type semiconductor

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Since the pentavalent atom donnates this extra conduction electron it is often called as a donor atom. For each pentavalent atom added, one free electron exists in a silicon crystal. A small amount of pentavalent impurity is enough to get more number of free electrons is greater than the nuumber of holes this extrinsic semiconductor is known as an $n$ type semiconductor.

When a pentavalent atom is added a number of conduction band electrons are produced. Only a few holes exist in the valence band, created by thermal energy. Therefore in an n-type semiconductor, electrons are majority carriers and holes are minority carriers.

## p-type semiconductor




Fig. 1.14 Energy band diagram of
a p-type semiconductor

A p-type semiconductor ( p for Positive) is obtained by carrying out a process of doping by adding a certain type of atoms (acceptors) to the semiconductor in order to increase the number of free charge carriers (in this case positive holes).

When the doping material is added, it takes away (accepts) weakly bound outer electrons from the semiconductor atoms. This type of doping agent is also known as an acceptor material and the vacancy left behind by the electron is known as a hole.

The purpose of p-type doping is to create an abundance of holes. In the case of silicon, a trivalent atom (typically from Group 13 of the periodic table, such as boron or aluminium) is substituted into the crystal lattice. The result is that one electron is missing from one of the four covalent bonds normal for the silicon lattice. Thus the dopant atom can accept an electron from a neighboring atom's covalent bond to complete the fourth bond. This is why such dopants are called acceptors.

The dopant atom accepts an electron, causing the loss of half of one bond from the neighboring atom and resulting in the formation of a "hole". Each hole is associated with a nearby negatively charged dopant ion, and the semiconductor remains electrically neutral as a whole. However, once each hole has wandered away into the lattice, one proton in the atom at the hole's location will be "exposed" and no longer cancelled by an electron.

This atom will have 3 electrons and 1 hole surrounding a particular nucleus with 4 protons. For this reason a hole behaves as a positive charge. When a sufficiently large number of acceptor atoms are added, the holes greatly outnumber thermal excited electrons. Thus, holes are the majority carriers, while electrons become minority carriers in p-type materials.

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## UNIT-II TRANSISTORS \& THYRISTORS <br> PART - A

## BJTT (Bipolar Junction Transistor)

1. What is transistor (BJT)? What are the types of circuit connections known as configurations, for operating a transistor?
Transistor (BJT) is a three-terminal device: Base (B), Emitter (E) \& Collector (C).
Transistor can be operated in three configurations Common Base (CB), Common Emitter (CE) \& Common Collector (CC).
According to configuration it can be used for voltage as well as current amplification.
2. Brief the types of transistors?
3. UJT (Unipolar Junction Transistor): In unipolar transistor, the current conduction is only due to one type of charge carriers (majority carriers).
4. BJT (Bipolar Junction Transistor): In bipolar transistor, the current conduction is only due to both the types of charge carriers (Holes and Electrons).
5. Why an ordinary transistor is called bipolar?

Because the transistor operation is carried out by two types charge carriers (both majority and minority carriers).
4. What are the types of BJT?

Types of BJT:

1. NPN
2. PNP
3. Brief the construction of BJT. Draw the symbol and structure and of BJT.

BJT is a three- layer semiconductor device consisting of two PN junctions.
If a layer of P-type material is sandwiched between two layers of N-type the transistor is known as NPN transistor.


Fig. Symbol of BJT (NPN type)

(a) $n-p-n$

Fig. Structure of BJT (NPN type)

On the other hand, if a layer of N-type material is sandwiched between two layers of P-type, the transistor is known as PNP transistor.


Fig. Symbol of BJT (PNP type)

(b) p-n-p

Fig. Structure of BJT (PNP type)
6. Why collector is made larger than emitter and base?

Collector is made physically larger than emitter and base because collector is to dissipate much power.
7. Why the width of the base region of a transistor is kept very Small as compared to other regions?

Base region of a transistor is kept very small and lightly doped so as to pass most of the injected charge carriers to the collector.

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8. How transistor is used as an amplifier? (OR) Explain the word transistor.

The amplification in the transistor is achieved by passing input current signal from a region of low resistance to a region of high resistance.
\{This concept of transfer of resistance has given the TRANSfer-resISTOR (TRANSISTOR)\}
9. Why silicon is preferred to germanium while manufacturing semiconductor devices?

As the knee voltage of silicon is higher $(0.7 \mathrm{~V})$ than the knee voltage of germanium $(0.3 \mathrm{~V})$, silicon will be more stable for temperature variation than germanium.
10. Why transistor (BJT) is called current controlled device?

The output voltage, current or power is controlled by the input current in a transistor. So, it is called the Current Controlled device.
11. State the advantages of a transistor.

1. Low operating voltage
2. Higher efficiency
3. Small size and ruggedness
4. 4. Does not require any filament power
1. Compare the performance of a transistor in three different configurations. (Nov/Dec 2012) (OR) Compare the input resistance, output resistance and voltage gain of $\mathrm{CB}, \mathrm{CC}$ and CE configuration. (OR) Compare the performance of CE and CC configuration. (May 2017)

| Property | CB | CE | CC |
| :--- | :--- | :--- | :--- |
| Input resistance | Low (about $100 \Omega$ ) | Moderate (about $750 \Omega$ ) | High (about 750 k $\Omega$ ) |
| Output resistance | High (about $450 \Omega$ ) | Moderate (about $45 \Omega$ ) | Low (about 25ת) |
| Current gain | 1 | High | High |
| Voltage gain | About 150 | About 500 | Less than 1 |
| Phase shift | 0 or $360^{\circ}$ | 0 or $360^{\circ}$ |  |
| Between input \& output <br> voltages Applications | For high frequency <br> circuits | For audio frequency <br> circuits | For impedance matching |

13. Define Early effect? (Nov/Dec 2016)

As the collector voltage $\mathrm{V}_{\mathrm{CC}}$ is made to increase the reverse bias, the space charge width between collector and base tends to increase, with the result that the effective width of the base decreases. This known as early effect or base width modulation.
14. What is peak point Voltage?

When $V_{\text {EE }}$ exceeds the value $\left(V_{D}+\eta V_{B B}\right)$, the diode is forward biased and starts to conduct. The value of emitter voltage which makes diode to conduct is called Peak Point Voltage.

$$
\mathrm{V}_{\mathrm{p}}=\left(\mathrm{V}_{\mathrm{D}}+\mathrm{n} \mathrm{~V}_{\mathrm{BB}}\right)
$$

## JFET (Junction Field EffectnTransistor)

15. What are the different types of FET?

Types of FET:

1. Junction Field Effect Transistor (JFET)
2. Metal Oxide Semiconductor Field Effect Transistor (MOSFET)
3. Draw the symbol and structure of JFET.


Fig. Structure and for n-channel JFET


Fig. Structure and for p-channel JFET

## 17. What are the features of JFET?

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a) The operation of JFET depends upon the flow of majority carriers only.
b) The input impedance of JFET is very high, in the order of $\mathrm{M} \Omega$.
c) The JFET is less noisy than BJT.
d) It exhibits no offset voltage at zero drain current.
e) It is simple to fabricate.
F) It occupies less space in an integrated circuit.

## 18. Draw the transfer and drain characteristics curves of JFET? (May / June 2016)

## Drain Characteristics:



Fig. Drain VI characteristics of n-channel JFET

Transfer Characteristics:


Fig. Transfer characteristics of n-channel JFET

## Drain Characteristics:



Fig. Drain VI characteristics of p-channel JFET

Transfer Characteristics:


Fig. Transfer characteristics of p-channel JFET
19. Define pinch-off voltage of a FET? (Nov/Dec-2012, May/June-2013)

Pinch-off voltage $\left(\mathrm{V}_{\mathrm{P}}\right)$ is defined as the drain to source voltage above which drain current becomes almost constant.
20. Mention the disadvantages of FET compared to BJT. (Nov/Dec-2012)

Gain bandwidth product of FET is relatively small as compared to BJT.

## 21. Define drain resistance.

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The drain resistance or output $\left(\mathrm{r}_{\mathrm{d}}\right)$ is defined as the ratio between change in drain-source voltage $\left(\mathrm{V}_{\mathrm{DS}}\right)$ and change in drain current $\left(\mathrm{I}_{\mathrm{D}}\right)$ at constant gate-source voltage $\left(\mathrm{V}_{\mathrm{GS}}\right)$.

$$
\mathrm{r}_{\mathrm{d}}=\frac{\partial V D S}{\partial i_{D}} V G S
$$

## 22. Differentiate FET and BJT (Nov/Dec 2018)

| S.No | FET | BJT |
| :---: | :--- | :--- |
| 1 | Unipolar device (that is current conduction by only one <br> type of either electron or hole). | Bipolar device (current conduction by both <br> electron and hole). |
| 2 | High input impedance due to reverse bias. | Low input impedance due to forward bias. |
| 3 | Gain is characterized by trans conductance | Gain is characterized by voltage <br> gain. |
| 4 | Low noise level | High noise level |

## 23. What are the applications of JFET?

a) JFET is used as a buffer in measuring instruments since it has high input impedance and low output impedance.
b) JFET is used in RF amplifier in FM tuners and communication equipment.
c) JFET is used in digital circuit's ii computers and memory circuits because of its small size.
d) It is used oscillators because the frequency drift is low.

## 24. FET has lower thermal noise than BJT - Justify. (April/May 2019-R17)

The FET has high gate-to-main current resistance, on the order of $100 \mathrm{M} \Omega$ or more providing a high degree of isolation between control and flow. Because base current noise will increase with shaping time, a FET typically produces less noise than a Bipolar Junction Transistor (BJT).
Thus, found in noise-sensitive electronics such as tuners and low noise amplifiers for VHF and satellite receivers. It is relatively immune to radiation.
25. What is the difference between BJT and JFET? (Nov/Dec 2017) (Apr/May 2018) (Nov/Dec 2018-R17)

| S. <br> No. | Bipolar junction transistor (BJT) | Junction field effect transistor (JFET) |
| :---: | :--- | :--- |
| 1 | Bipolar device (current conduction is by <br> both electrons and holes) | Unipolar device (current is by only one type of <br> carrier-either electrons or holes) |
| 2 | Low input impedance due to forward bias | High input impedance due to reverse bias |
| 3 | Current control device | Voltage control device |
| 4 | Gain is characterized by voltage gain | Gain is characterized by Tran conductance. |
| 5 | High noise level | Low noise level |

## MOSFET

26. What are the different types of MOSFET? (May/June-2012, 2013)

The modes of operation of the MOSFET are divided into two types.
a) Depletion mode MOSFET
b) Enhancement mode MOSFET
27. What is the other name for MOSFET? (May/June-2012, 2013)

Metal Oxide Semiconductor Field Effect Transistor (MOSFET) is also called as Insulated Gate Field Effect Transistor (IGFET)

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28. If the gate-to-source voltage in an Enhancement MOSFET is zero, what is the current from drain to source? In an Enhancement MOSFET if the gate-to-source voltage is zero, then the current from drain to source is also zero.
29. What is the major difference in construction of the D-MOSFET and the E-MOSFET?

The depletion MOSFET has a structural channel, whereas the enhancement-MOSFET does not.
30. If the gate-to-source voltage in depletion MOSFET is zero, what is the current from drain to source?

When gate -source voltage is zero for depletion MOSFET, the drain-source current is equal to $I_{D S S}$. ( $I_{D} \_I_{D S S}$ )
31. What are the precautions to be taken when handling MOSFET?
a) MOSFET should be shipped and stored in a conduction foam rubber.
b) Prior to soldering, the technician should use a shorting strap to discharge his static electricity.
c) The soldering iron tip to be grounded. d) MOSFETs should never be inserted into or removed from a circuit with the power on.
e) The assembler should wear antistatic clothes and ground wrist beads.
f) All the instruments and metal benches used to test the MOS devices should be connected to ground.
g) Always avoid touching the device terminals and pick up the transistor by its casing.
32. What are the applications of MOSFET?
a) It can be used as input amplifiers in oscilloscope, electric voltmeters etc.
b) It is used in logic circuits.
c) It is used in computer memories.
d) It is used in phase shift oscillators.
e) It is used in FM and TV receivers.

## 33. Depletion MOSFET is commonly known as "Normally-ON" MOSFET why?

The depletion MOSFET can conduct even if the gate to source voltage ( $\mathrm{V}_{\mathrm{GS}}$ ) is zero. Because of this reason depletion MOSFET is community known as "Normally-ON" MOSFET.
34. What is the difference between JFET and MOSFET? (May / Jun 2016)

| S. No. | JFET | MOSFET |
| :---: | :--- | :--- |
| 1 | Reverse bias for gate | Positive or negative gate voltage |
| 2 | Gate is formed as a diode | Gate is formed as a capacitor |
| 3 | Operation only depletion mode | Can be operated either in depletion mode or in enhancement mode. |
| 4 | High input impedance | Very high input impedance due to capacitive effect. |

## $\underline{\underline{U S T}}$

35. Draw the structure of UJT. (Nov/Dec 2017)

36. What is UJT?

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Uni junction transistor is a three terminal semiconductor device consisting of only one PN junction. It differs from ordinary PN diode in the sense that it has three terminals namely Emitter, Base 1 and Base 2.

## 37. Describe the construction of UJT?

UJT consists of lightly doped TV type is semiconductor bar with a heavily doped $\boldsymbol{P}$ type material.
$\boldsymbol{N}$ type bar is called base and $\boldsymbol{P}$ type region is called emitter. Hence $\boldsymbol{P N}$ junction is formed between emitter and base region.
Since base is lightly doped the resistivity of the base material is very high.
The direction of arrowhead in the UJT symbol represents the conventional direction of current flow when UJT is in conduction state.
38. State two applications of UJT. (Nov/Dec 2018)

1. UJT is used to trigger other devices like SCR.
2. Also used in sawtooth wave generators and some timing circuits.
3. It is used as relaxation oscillator to obtain short pulses for triggering of SCR.
4. What is intrinsic stand OFF ratio of UJT and its equivalent circuit? (May 2017)

The intrinsic stand OFF radio $(\mathrm{r} \mid)$ is defined as the ratio between the internal dynamic resistance $\left(\boldsymbol{R}_{\boldsymbol{B}}\right)$ and the inter base resistance $\left(\boldsymbol{R}_{\boldsymbol{B}}\right)$ -
$\boldsymbol{\eta}=\frac{R_{B 1}}{R_{B 2}}$
Where,
$\mathrm{R}_{\mathrm{BB}}=\mathrm{R}_{\mathrm{B} 1}+\mathrm{R}_{\mathrm{B} 2}$
$\mathrm{R}_{\mathrm{B} 1}$ - internal dynamic resistance
$\mathrm{R}_{\mathrm{B} 2}$ - inter base resistance

40. What are the different regions in characteristics of UJT?

- Cut off Region
- Negative Resistance Region
- Saturation Region


## THYRISTOR

41. Describe the basic structure of SCR?

SCR consist of four semiconductor layers forming a PNPN structure. It has three PN junctions namely $\mathrm{J}_{1}, \mathrm{~J}_{2}$ anode (A), cathode ( $\boldsymbol{K}$ ) and the gate (G).
42. What are the different methods used to turn ON SCR?

1. Gate triggering
2. Forward break over voltage
3. Light triggering
4. Rate - effect (or) triggering
5. What is forward break over voltage? (Apr/May 2018)

SCR is forward bias with a small voltage, it is in 'OFF' and no current flows through the SCR. The applied forward voltage is increased, a certain critical voltage called forward break over voltage ( $\boldsymbol{V}_{\boldsymbol{B} \boldsymbol{O}}$ ).
44. Define holding current? What is the latching current in SCR? (April / May 2019-R17)

Holding current is the current below which the SCR switches from the conduction state (ON state) to the forward blocking state.
Latching Current is the minimum current required to trigger the device from its OFF state to ON state.

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45. What is the forward blocking region?

This region corresponding to the OFF condition of the SCR when anode is positives.
46. What is the turn OFF mechanism used for SCR?

To turn OFF a SCR, the following methods are applied.
(i) Reversing polarity of anode-to-cathode voltage called as Gate turn OFF switch (GTO).
(ii)The second method is anode current interruption. Changing anode current by means of momentarily series or parallel switching arrangement.
(iii)Third method is forced commutation. In this, the current through SCR is reduced below the holding current
47. Give the applications of SCR.

Main applications of an SCR are as a power control device. Common areas of applications include
(a). As over light detector
(f). Battery charges
(b). Relay control
(g). Heater controls
(c). Regulated power supplies
(h). Phase controls
(d). Static switches
(i). For speed control of DC shunts motor.
(e). Motor control
48. What are the advantages of SCR?
$>$ SCR controls large current in the load by means of a small gate current.
$>$ SCR size is very compact.
> Switching speed is high.
49. Show how an SCR can be triggered on by the application of a pulse to the gate terminal. (Nov / Dec 2015)

SCR is forward bias with a small voltage, it is in 'OFF' and no current flows through the SCR. The applied forward voltage is increased, a certain critical voltage called forward break over voltage $\left(V_{B o}\right)$. The forward break over voltage is reduced by application of gate pulses.


## IGBT, DIAC \& TRIAC

50. IGBT is a voltage controlled device. Why?

Because the controlling parameter is gate-emitter voltage.
51. Why IGBT is very popular nowadays? MAY/JUNE-2012

1. Lower gate requirements 2. Lower switching losses
2. Smaller snubbed circuit requirements

## 52. What is DIAC?

A DIAC is two terminal semiconductor device and three-layer bidirectional device, which can be switched from of its OFF to ON state for either negative or positive polarity of applied voltage.

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## 53. What are the applications of DIAC?

The DIAC is used as a triggering device; it is not a control device. It is used in.

- Temperature control
- Triggering of TRIAC
- Light diming circuits
- Motor speed control

54. What is TRIAC?

TRIAC is a three terminal semiconductor switching device which can conduct in either forward or reverse direction. The TRIAC is the combination of two SCR's connected in parallel but in opposite direction.

## 55. What are the applications of TRIAC?

- Heater control
- Phase control
- Light dimming control
- Static switch to turn A.C power ON and OFF.
- Speed control of motor.


## PART-B

## BJT-Structure, Operation \& Characteristics

1. Explain about the transistor (BJT) operation.

Structure:

(a) $n-p-n$

(b) $p-n-p$

## Symbol:


(a) $n-p-n$

(b) p-n-p

## Two-diode transistor analogy


(a) n-p-n transistor

(b) p-n-p transistor

Applying external voltage to a transistor is called biasing. In order to operate transistor properly as an amplifier, it is necessary to correctly bias the two PN junctions with external voltages. Depending upon external bias voltage polarities used, the transistor works in one of the three regions.

1. Active region
2. Cut-off region
3. Saturation region

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| S. No. | Region | Emitter Base | Collector Base | Operation of a transistor |
| :---: | :--- | :---: | :---: | :--- |
| 1 | Active | Forward biased | Reverse biased | Acts as an amplifier |
| 2 | Cut off | Reverse biased | Reverse biased | Acts as an open switch |
| 3 | Saturation | Forward biased | Forward biased | Acts as a closed switch |

To bias the transistor in its active region the emitter base junction is forward biased, while the collectorbase junction in reverse-biased as shown in Fig. The Fig. shows the circuit connections for active region for both NPN and PNP transistors.


## Operation of NPN transistor:

As shown in fig. the forward bias applied to the emitter base junction of an NPN transistor causes a lot of electrons from the emitter region to cross over to the base region. As the base is lightly doped with P-type impurity, the number of holes in the base region is very small and hence the number of electrons that combine with holes in the P - type base region is also very small. Hence a few electrons combine with holes to constitute a base current $\mathrm{I}_{\mathrm{B}}$. The remaining electrons (more than $95 \%$ ) crossover into the collector region to constitute a collector current $\mathrm{I}_{\mathrm{C}}$. Thus the base and collector current summed up give the emitter current i.e. $\mathrm{I}_{\mathrm{E}}=-\left(\mathrm{I}_{\mathrm{C}}+\mathrm{I}_{\mathrm{B}}\right)$.


Fig. Current in NPN transistor
In the external circuit of the NPN bipolar junction transistor, the magnitudes of the emitter current $\mathrm{I}_{\mathrm{E}}$, the base current $\mathrm{I}_{\mathrm{B}}$ and the collector current $\mathrm{I}_{\mathrm{C}}$ are related by $\mathrm{I}_{\mathrm{E}}=\mathrm{I}_{\mathrm{C}}+\mathrm{I}_{\mathrm{B}}$.

## Operation of PNP transistor:

As shown in fig. the forward bias applied to the emitter - base junction of a PNP transistor causes a lot of hoses from the emitter regions to cross over to the base region as the base is lightly doped with N type impurity. The number of electrons in the base regions is very small and hence the number of holes combined with electrons in the N - type base region is also very small. Hence a few holes combined with electrons to constitute a base current $\mathrm{I}_{\mathrm{B}}$.


Fig. Current in PNP transistor
The remaining holes (more than 95\%) cross over into the collector region to constitute a collector current Ic. Thus, the collector and base current when summed up gives the emitter current.
i.e. $\mathrm{I}_{\mathrm{E}}=-\left(\mathrm{I}_{\mathrm{C}}+\mathrm{I}_{\mathrm{B}}\right)$.

In the external circuit of the PNP bipolar junction transistor, the magnitudes of the emitter current $\mathrm{I}_{\mathrm{E}}$, the base current $\mathrm{I}_{\mathrm{B}}$ and the collector current $\mathrm{I}_{\mathrm{C}}$ are related by

$$
\mathrm{I}_{\mathrm{E}}=\mathrm{I}_{\mathrm{C}}+\mathrm{I}_{\mathrm{B}}
$$

The equation gives the fundamental relationship between the currents in a bipolar transistor circuit. Also, this fundamental equation shows that there are current amplification factors $\alpha$ and $\beta$ in common base transistor configuration and common emitter transistor configuration respectively for the static (d.c) currents, and for small changes in the currents.

Large - signal current gain $(\alpha)$. The large signal current gain of a common base transistor is defined as the ratio of the negative of the collector - current increment to the emitter - current change from cut off ( $\mathrm{I}_{\mathrm{E}}=0$ ) to $\mathrm{I}_{\mathrm{E}}$,i.e.

$$
\alpha=-\frac{\left(I_{\mathrm{C}}-I_{\text {CBO }}\right)}{I_{\mathrm{E}}-0}
$$

where $\mathrm{I}_{\text {CBo }}$ ( or $\mathrm{I}_{\mathrm{Co}}$ ) is the reverse saturation current flowing through the reverse biased collector base junction. i.e. the collector to base leakage current with emitter open. As the magnitude of $\mathrm{I}_{\text {Cbo }}$ is negligible when compared to $\mathrm{I}_{\mathrm{E}}$, the above expression can be written as

$$
\alpha=\frac{I_{C}}{I_{E}}
$$

Since $\mathrm{I}_{\mathrm{C}}$ and $\mathrm{I}_{\mathrm{E}}$ are flowing in opposite directions, $\alpha$ is always positive. Typical value of $\alpha$ ranges from 0.90 to 0.995 . Also, $\alpha$ is not a constant but varies with emitter current $\mathrm{I}_{\mathrm{E}}$, collector voltage $\mathrm{V}_{\mathrm{CB}}$ and the temperature.

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## 2. (a) Explain various characteristics of BJT in Common Base configuration with neat diagram.

## Common Base Configuration (CB configuration):

This configuration is also called the grounded base configuration. In this case the input is connected between emitter and base while the output is taken across the collector and base. Thus the base of the transistor is common to both input and output circuits and hence the name, common base configuration. The common base circuit arrangement for NPN transistors is shown in Fig.

## Current Amplification Factor ( $\alpha$ ):

The current amplification factor is defined as the ratio of changes in Collector current ( $\Delta \mathrm{I}_{\mathrm{C}}$ ) to the change in emitter current $\left(\Delta \mathrm{I}_{\mathrm{E}}\right)$ when the collector to base voltage $\left(\mathrm{V}_{\mathrm{CB}}\right)$ is maintained at a constant value.

$$
\alpha=\left(\Delta \mathrm{I}_{\mathrm{C}}\right) /\left(\Delta \mathrm{I}_{\mathrm{E}}\right)\left(\text { at constant } \mathrm{V}_{\mathrm{CB}}\right)
$$

The value of $\alpha$ is always less than unity. The practical value of transistors lie between 0.95 and 0.99 .

## Characteristics of Common Base Configuration:

The circuit arrangement for determining the characteristics of a common base NPN transistors is shown in Fig.In this circuit, the collector to base voltage ( $\mathrm{V}_{\mathrm{CB}}$ ) can be varied by adjusting the potentiometer $\mathrm{R}_{2}$. The emitter to base voltage ( $\mathrm{V}_{\mathrm{EB}}$ ) can be varied by adjusting the potentiometer $\mathrm{R}_{1}$. The DC voltmeters and DC milliammeters are connected in the emitter and collector circuits to measure the voltages and currents.


## a). Input Characteristics:

The curve plotted between the emitter current ( $\mathrm{I}_{\mathrm{E}}$ ) and the emitter to base voltage $\left(\mathrm{V}_{\mathrm{EB}}\right)$ at constant collector to base voltage $\left(\mathrm{V}_{\mathrm{CB}}\right)$ are known as input characteristics of a transistor in common base configuration.


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## Input Resistance ( $\mathbf{R}_{\mathbf{i}}$ ):

It is the ratio of change in emitter to base voltage ( $\Delta \mathrm{V}_{\mathrm{EB}}$ ) to the corresponding change in emitter current ( $\Delta \mathrm{I}_{\mathrm{E}}$ ) for a constant collector to base voltage ( $\mathrm{V}_{\mathrm{CB}}$ ).

$$
\mathrm{R}_{i}=\frac{\Delta \mathrm{V}_{\mathrm{EB}}}{\Delta \mathrm{I}_{\mathrm{E}}} \text { (at constant } \mathrm{V}_{\mathrm{CB}} \text { ) }
$$

## b). Output Characteristics:

The curve plotted between the collector current ( $\mathrm{I}_{\mathrm{C}}$ ) and the collector to base voltage
$\left(\mathrm{V}_{\mathrm{CB}}\right)$ at constant emitter current $\left(\mathrm{I}_{\mathrm{E}}\right)$ are known as output characteristics of a transistor is common base configuration.


The output characteristics are as shown in Fig. and it can be divided into three important regions namely (i) Saturation region (ii) Active region (iii) Cut-off region.

## (i). Saturation Region:

In this region, collector to base voltage $\left(\mathrm{V}_{\mathrm{CB}}\right)$ is negative for a NPN transistor. A small change in collector to base voltage $\left(\mathrm{V}_{\mathrm{CB}}\right)$ results in a large valve of collector current.

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## (ii). Active Region:

In this region the collector current ( $\mathrm{I}_{\mathrm{C}}$ ) is almost equal to the emitter current ( $\mathrm{I}_{\mathrm{E}}$ ). The transistor is always operated in this region. In the active region, the curves are almost flat. A very large change in $\mathrm{V}_{\text {CB }}$ produces only a very small change in IC. It means that the circuit has very high output resistance about $500 \mathrm{~K} \Omega$.

## (iii). Cut-off Region:

It is the region along the X -axis as shown by shaded or dotted portion. This corresponds to the curve marked $\mathrm{I}_{\mathrm{E}}=0$. In the cut-off region both the junctions of a
Transistor are reverse biased. A small collector current flows even when the emitter Current ( $\mathrm{I}_{\mathrm{E}}$ ) is equal to zero.
If the collector to base voltage $\left(\mathrm{V}_{\mathrm{CB}}\right)$ is increased beyond a certain large value, the collector current ( $\mathrm{I}_{\mathrm{C}}$ ) increases rapidly due to avalanche breakdown and the transistor action is lost. This region is called breakdown region.

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(b) For a transistor connected in CE configuration, sketch the typical output and input characteristics and explain the shape of characteristics.

## Common Emitter Configuration (CE Configuration):

This configuration is also called the grounded emitter configuration. In this case the input is connected between base and emitter, while the output is taken across the collector and emitter. Thus emitter of the transistor is common to both input and output circuits and hence the name, common emitter configuration. The common emitter arrangement for NPN transistor is as shown in Fig.


## Base Current Amplification Factor ( $\beta$ ):

The base current amplification factor is defined as the ratio of change in collector current $\left(\Delta \mathrm{I}_{\mathrm{C}}\right)$ to the change in emitter current $\left(\Delta \mathrm{I}_{\mathrm{E}}\right)$ when the collector to emitter voltage $\left(\mathrm{V}_{\mathrm{CE}}\right)$ is maintained at a constant value.

$$
\beta=\frac{\Delta \mathrm{I}_{\mathrm{C}}}{\Delta \mathrm{I}_{\mathrm{B}}}\left(\text { at constant } \mathrm{V}_{\mathrm{CE}}\right)
$$

The value of $\beta$ is always greater then unity. Practical value of $\beta$ in commercial transistors lie between 20 to 500 .

## Characteristics of common Emitter configuration:

The circuit arrangement for determining the characteristics of a common emitter NPN transistor is shown inFig.In this circuit, the collector to emitter voltage $\left(\mathrm{V}_{\mathrm{EC}}\right)$ can be varied by adjusting the potentiometer $\mathrm{R}_{2}$. The base to emitter voltage ( $\mathrm{V}_{\mathrm{BE}}$ ) can be varied by adjusting the potentiometer $\mathrm{R}_{1}$. The DC voltmeters and milliammeters are connected in the base and collector circuits to measure the voltages and currents.


## 1. Input Characteristics:

The curve plotted between the base current $\left(\mathrm{I}_{\mathrm{B}}\right)$ and the base to emitter voltage $\left(\mathrm{V}_{\mathrm{BE}}\right)$ at constant collector to emitter voltage $\left(\mathrm{V}_{\mathrm{CE}}\right)$ at constant collector to emitter voltage $\left(\mathrm{V}_{\mathrm{CE}}\right)$ are known as input characteristics of a transistor in common emitter configuration.

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Input Resistance $\left(\mathrm{R}_{\mathrm{i}}\right)$ : It is the ratio of change in base to emitter voltage $\left(\mathrm{V}_{\mathrm{BE}}\right)$ to the Corresponding change in base current $\left(\Delta \mathrm{I}_{\mathrm{B}}\right)$ for a constant collector to emitter voltage ( $\mathrm{v}_{\mathrm{CE}}$ ).

$$
\mathrm{R}_{i}=\frac{\Delta \mathrm{V}_{\mathrm{BE}}}{\Delta \mathrm{I}_{\mathrm{B}}}
$$

(at constant $\mathrm{V}_{\mathrm{CE}}$ )

When the collector to emitter voltage $\left(\mathrm{V}_{\mathrm{CE}}\right)$ is increased, the value of base current $\left(\mathrm{I}_{\mathrm{B}}\right)$ decreased slightly as shown in Fig.

## 2. Output Characteristics:



The curves plotter between the collector current ( $\mathrm{I}_{\mathrm{C}}$ ) and the collector to emitter Voltage ( $\mathrm{V}_{\mathrm{CE}}$ ) at constant base current $\left(\mathrm{I}_{\mathrm{B}}\right)$ is known as output characteristic of a transistor in common emitter configuration.
The output characteristic may be divided into three important regions namely saturation region, active region, and cut-off region.
(i) Saturation Region:

In this region (shown by dotted area) a small change in collector to emitter voltage $\left(\mathrm{V}_{\mathrm{CE}}\right)$ results in a large value of collector current.

## (ii) Active Region:

It is the region between saturation and cut-off region. In this region the curves are almost flat. When the collector to emitter voltage $\left(\mathrm{V}_{\mathrm{CE}}\right)$ is increased. Further, the collector current I. slightly increases. The slope of the curve is little bit more than the output characteristics of common base configuration. Therefore, the output resistance ( $\mathrm{R}_{\mathrm{o}}$ ) of this configuration is less as compared to common base configuration.

## (iii) Cut-off Region:

It is the region along the X -axis is shown by shaded area. This corresponds to the curve marked $\mathrm{I}_{\mathrm{B}}=0$. In the cutoff region both the junctions of a transistor are reverse biased. A small collector current flows even when the base current $\left(\mathrm{I}_{\mathrm{B}}\right)$ is equal to zero. It is the reverse leakage current ( $\mathrm{I}_{\text {CEO }}$ ) that flows in the collector circuit.

If the collector to emitter voltage $\left(\mathrm{V}_{\mathrm{CE}}\right)$ is increased beyond a certain large collector current $\left(\mathrm{I}_{\mathrm{C}}\right)$ increases rapidly due to avalanche breakdown and the action is lost. This region is called breakdown region.

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(c) Explain various characteristics of BJT in Common Collector configuration with neat diagram.
Common collector configuration (CC configuration):


This configuration is also called the grounded collector configuration' In this case the input is common between base and Collector. While the output is taken across the emitter and collector. Thus the collector of the transistor is common to both input and output circuits and hence the name common collector configuration. The common collector circuit arrangement for NPN transistor as shown in Fig.

## Current Amplification Factor ( $\gamma$ ):

The current amplification is defined as the ratio of change in emitter current $\left(\Delta \mathrm{I}_{\mathrm{E}}\right)$ to the change in base current $\left(\Delta \mathrm{I}_{\mathrm{B}}\right)$. It is generally denoted by $\gamma$.

$$
\gamma=\frac{\Delta \mathrm{I}_{\mathrm{E}}}{\Delta \mathrm{I}_{\mathrm{B}}}
$$

The value of $\gamma$ is nearly equal to $\beta$.

## Characteristics of common Collector configuration:

The circuit arrangement for determining the characteristics of a common collector NPN transistor is shown in Fig. In this circuit, the emitter to collector voltage ( $\mathrm{V}_{\mathrm{EC}}$ ) can be varied by adjusting the potentiometer $\mathrm{R}_{2}$. The base to collector voltage ( $\mathrm{V}_{\mathrm{BC}}$ ) can be varied by adjusting the potentiometer $\mathrm{R}_{1}$. The DC voltmeter and millimeters are connected in the base and emitter circuits to measure the voltages and currents.


## 1. Input Characteristics:

The curves plotted between the base current $\left(\mathrm{I}_{\mathrm{B}}\right)$ and the base to collector voltage $\left(\mathrm{V}_{\mathrm{BC}}\right)$ at constant emitter to collector voltage ( $\mathrm{V}_{\mathrm{EC}}$ ) are known as input characteristics of a transistor in common collector configuration.


## 2. Output Characteristics:

The curves plotted between the emitter current ( $\mathrm{I}_{\mathrm{E}}$ ) and the emitter to collector voltage ( $\mathrm{V}_{\mathrm{EC}}$ ) at constant base current ( $\mathrm{I}_{\mathrm{B}}$ ) are known as output characteristics of a transistor is common collector configuration.

3. Explain the emitter bias method used in transistor amplifier circuits. (Nov/Dec 2017)

## Emitter Bias

This biasing network uses two supply voltages, $\mathrm{V}_{\mathrm{CC}}$ and $\mathrm{V}_{\mathrm{EE}}$, which are equal but opposite in polarity. Here $\mathrm{V}_{\mathrm{EE}}$ forward biases the base-emitter junction through $\mathrm{R}_{\mathrm{E}}$ while $\mathrm{V}_{\mathrm{CC}}$ reverse biases the collector-base junction. Moreover

$$
\begin{aligned}
V_{E} & =-V_{E E}+I_{E} R_{E} \\
V_{C} & =V_{C C}-I_{C} R_{C} \\
V_{B} & =V_{B E}+V_{E} \\
I_{C} & =\beta I_{B} \\
I_{E} & \approx I_{C}
\end{aligned}
$$



Emitter Bias Circuit

In this kind of biasing, $I_{C}$ can be made independent of both $\beta$ and $V_{B E}$ by choosing $R_{E} \gg R_{B} / \beta$ and $V_{E E}$ $\gg V_{B E}$, respectively; which results in a stable operating point.

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4. Explain the selection of $Q$ point for transistor bias circuits and discuss the limitations on the output voltage swing. (Nov / Dec 2015)

The dc load line for a transistor circuit is a straight line drawn on the transistor output characteristics. For a common emitter CE circuit. The load line is a graph of collector current versus collector emitter voltage for a given value of collector resistance and a given supply voltage. The load lines show all corresponding levels of $\mathrm{I}_{\mathrm{c}}$ and $\mathrm{V}_{\mathrm{CE}}$ that can exist in a particular circuit.

Consider the common emitter circuit in fig. Note that the polarities of the transistor terminal voltage are such that the base emitter junction is forward biased and the collector base junction is reverse biased. These are the normal bias polarities for the transistor junctions. The dc load line for the circuits in fig drawn on the device common emitter characteristics in fig.

$\mathrm{V}_{\mathrm{CE}}=($ Supply voltage $)-\left(\right.$ Voltage drop across $\left.\mathrm{R}_{\mathrm{C}}\right)$
$\mathrm{V}_{\mathrm{CE}}=\mathrm{V}_{\mathrm{CC}}-\mathrm{I}_{\mathrm{C}} \mathrm{R}_{\mathrm{C}}$
If the base emitter voltage is zero, the transistor is not conducting and IC $=0$. Substituting the $V_{C C}$ and $R_{C}$ values from fig into equal 5-1
$\mathrm{V}_{\mathrm{CE}}=20 \mathrm{~V}-(0 * 10 \mathrm{k}$ ohms $)=20 \mathrm{~V}$

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Plot point A on the common emitter characteristics in fig. 5-2 at $\mathrm{I}_{\mathrm{c}}=0$ and $\mathrm{V}_{\mathrm{CE}}=20 \mathrm{~V}$. This is one point on the dc load line.

Now assume a collector current of 2 mA , and calculate the corresponding collector emitter voltage level.
$\mathrm{V}_{\mathrm{CE}}=20 \mathrm{~V}-\left(2 \mathrm{~mA}^{*} * 10 \mathrm{k}\right.$ ohms $)=0 \mathrm{~V}$
Plot point B fig 5-2 at VCE $=0$ and $\mathrm{I}_{\mathrm{C}}=2 \mathrm{~mA}$. The straight line drawn though point A and point B is the dc load line for $\mathrm{R}_{\mathrm{C}}=10 \mathrm{kohms}$ and $\mathrm{V}_{\mathrm{CC}}=20 \mathrm{~V}$. If either of these two quantities is changed, a new load line must be drawn.


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As already stated the dc load line represents all corresponding $I_{C}$ and $V_{C E}$ levels that can exist in the circuit as represented by Eq. 5-1 for example a point plotted at $\mathrm{V}_{\mathrm{CE}}=16 \mathrm{~V}$ and $\mathrm{I}_{\mathrm{C}}=1.5 \mathrm{~mA}$ on fig $5-2$ does not appear on the load line. This combination of voltage and current cannot exist in this particular circuit. Knowing any one of $\mathrm{I}_{\mathrm{B}}, \mathrm{I}_{\mathrm{C}}$, or $\mathrm{V}_{\mathrm{CE}}$, it is easy to determine the other two from a dc load line drawn on the device characteristics. It is not always necessary to have the device characteristics in order to draw the dc load line. A simple graph of $\mathrm{I}_{\mathrm{C}}$ versus $\mathrm{V}_{\mathrm{CE}}$ can be used as demonstrated in example 5-1.

## Limitation on the output voltage swing:

The maximum possible transistor collector emitter voltage swing for a given circuit can be determined without using the transistor characteristics. For convenience, it may be assumed that $I_{c}$ can be driven to zero at one extreme and to $\mathrm{V}_{\mathrm{cc}} / \mathrm{R}_{\mathrm{c}}$ at the other extreme, [see fig]. This changes the collector emitter voltage from $\mathrm{V}_{\mathrm{CE}}=\mathrm{V}_{\mathrm{cc}}$ to $\mathrm{V}_{\mathrm{CE}}=0$, as illustrated in fig. thus with the Q point at the center of the load line, the maximum possible collector voltage swing is seen to be approximately $\bar{\mp} V_{c c} / 2$.

## DFET-Structure, Operation \& Characteristics

5. (a) Explain construction and operation of Junction Field Effect Transistor (JFET)? (NOV/DEC 2012) (May/June-2012)
(b) Explain drain and transfer characteristics of JFET? (May 2017)

## (a) Construction and operation:

The basic construction of an n-channel JFET is shown in fig. It consists of an n-type silicon bar referred as the channel. Two small pieces of p-type material are attached to its sides forming pn junctions. If the bar is of n-type the JFET is called as on n-channel JFET, and if the bar is of p-type it is called a ptype channel JFET fig shows schematic diagram of both types of FET's with their symbols.


## N-channel JFET



Symbol

The channel ends are designated as source(S) and drain (D). The source $S$ is the terminal through which the majority carriers enters the bar and drain D is the terminal through which the majority carriers leave the bar. The two p-regions, which are formed by alloying or by diffusion, are connected together and their terminal is called gate. When no bias applied to JFET, depletion regions are formed at two pn junctions as shown in fig. Recall that depletion region is a region depleted of charge carriers and therefore behaves insulators

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## P-channel JFET

## Operation of N-channel JFET

When Vds is of some fixed positive value and reverse bias on Vgs increasing.


## Operation of N-channel JFET

Let us assume that the gate is not biased and a fixed positive voltage is applied between the drain and source terminals as shown in fig. Due to this applied voltage will move through the n-type channel from source to drain. When the gate is negative biased with respect to source, the an junction are reverse biased and the depletion region are formed. Since the channel is lightly doped compared to heavily doped p-region, the depletion region penetrates deeply into the channel. As a result, the effective channel resistance significantly and reduces the drain current $\mathrm{I}_{\mathrm{D}}$. If the reverse biased on the gate is increased further the depletion will cover the entire width of the channel and ID is cut off completely fig.

## 2. $\mathrm{V}_{\mathrm{GS}}=\mathbf{0}, \mathrm{V}_{\mathrm{DS}}$ is varied

First assume that the gate source voltage $\left(\mathrm{V}_{\mathrm{GS}}\right)$ is set to the zero. When the drain source voltage $\mathrm{V}_{\mathrm{DS}}$ is also zero, the current flowing through FET is also zero that is $\mathrm{I}_{\mathrm{D}}=0$. The instant the voltage $V_{D S}$ is applied, electrons starts flowing from source to drain terminals establishing the current $I_{D}$ under this condition the channel between drain and source act as a resistance.
(b) Characteristics of JFET:-

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The circuit diagram to obtain the characteristics of JFET is shown in fig.


The characteristics that we consider are
i) Drain characteristics
ii) Transfer characteristics

In drain characteristics the relation between Id and VDS for different values of VGS is plotted. In transfer characteristics the relation between ID and VDGS for constant is plotted.

## (i) Drain characteristics with $V_{G S}=0$ (May 2017)

The drain characteristics for $\mathrm{V}_{\mathrm{GS}}=0$ is shown in fig. To plot this characteristic the gate to source voltage is kept at zero and $V_{D S}$ is varied from zero. When $V_{D S}$ is zero the drain current $\mathrm{I}_{\mathrm{D}}$ is also zero. When $V_{D S}$ is increased the drain, current starts flowing through the channel and FET behaves like a resistor till point $A$. That is for low values of $V_{D S}$, current varies directly with voltage following ohm's law. The portion of characteristics where the FET behaves like a resistor is known as ohms region. The FET can be used as a voltage variable resistor in this region if we increase $\mathrm{V}_{\mathrm{DS}}$, a stage is reached at which pinch off occurs and the drain current reaches a saturation level. The drain to source voltage at which pinch off occurs is known as pinch off voltage $V_{P}$, and corresponding $I_{D}$ is known as $I_{D S s}$. The point $B$ at which pinch-off occurs is shown in fig. Even if we increase $V_{D S}$ above $V_{P}$ the drain current $V_{D S}$ above Vp the drain current does not increase. The region where the drain current is constant inspite of the variation in $\mathrm{V}_{\mathrm{DS}}$ is known as pinch-off region. If we increase $\mathrm{V}_{\mathrm{DS}}$ for there a stage is reached at which the gate channel junction FET breakdown and increase rapidly. This region in the characteristics is known as breakdown region. When a bias $(-1 \mathrm{~V})$ is applied between gate source the pinch off occurs at less drain current less than IDSS. The drain characteristics for different values of $\mathrm{V}_{\mathrm{GS}}$ shown fig.


Characteristics of JFET for VGS=0


## Characteristics of JFET for different values of $V_{G S}$

## (ii) Transfer characteristics

It is a plot of drain current Id versus $\mathrm{V}_{\mathrm{GS}}$ constant values. To plot the characteristics $\mathrm{V}_{\mathrm{DS}}$ is kept constant and $\mathrm{V}_{\mathrm{GS}}$ is varied. When $\mathrm{V}_{\mathrm{GS}}=$ the current flowing the FET is Equal to $\mathrm{I}_{\mathrm{DSS}}$ and when $\mathrm{V}_{\mathrm{GS}}=\mathrm{V}_{\mathrm{GS}}$ (off), the drain current is zero.
Shockley's equation:-
The relation between $V_{G S}$ and $\mathrm{I}_{\mathrm{D}}$ can be represented by Shockley's equation
$\mathrm{I}_{\mathrm{D}}=\mathrm{I}_{\mathrm{DSS}}\left(1-\mathrm{V}_{\mathrm{GS}} / \mathrm{Vp}\right)^{2}$. 3.1

Using this mathematically expression, we can develop the plot of $I_{D}$ versus $\mathrm{V}_{\mathrm{GS}}$ for any JFET, provide the two parameters IDSs and Vp are known.


Transfer characteristics of JFET.

## MOSFET-Structure, Operation \& Characteristics

6. With neat diagram explain the construction \& working of depletion MOSFET and enhancement MOSFET with its necessary characteristics curve. (Nov/Dec 2018 R-13) (May/June 2016) (Apr/May 2018) OR
Brief about the construction and operation of n-channel depletion type MOSFET with a neat diagram. Enumerate the characteristics of depletion type MOSFET with a suitable graph. (April/May 2019-R17)

## Depletion MOSFET:

- The construction of an N-channel depletion MOSFET is shown in fig. If consists of a lightly doped p-type substrate in which two highly doped n-regions are diffused. The two heavily doped n-


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regions act as the source and drain. A lightly doped n-type channel is introduced between the two heavily doped source and drain. A thin layer of ( $1 \mu \mathrm{~m}$ thick) silicon dioxide is coated on the surface. Holes are cut in the oxide layer to make contact with n-regions due to $\operatorname{sio}_{2}$ layer the gate is completely insulated from the channel. This permits operation with gate source or gate channel voltages above and below zero. In addition the insulated layer of $\operatorname{sio}_{2}$ accounts for very high input impedance of MOSFET. In some MOSFETS the p-type substrate is internally connected to source, whereas in many discrete devices an additional terminal is provided for substrate labeled SS.


## Basic operation:

In fig a voltage VDS is applied between the drain and source terminals and the gate to source voltage is set to zer. As a result, current is established from drain to source (conventional direction) similar to JFET like in JFET, the satuarated drain current IDSS flow during pinch-off and it is labeled as IDSS.


If a negative voltage is applied to gate with repeat to source. These holes recombine with electrons and reduce the number of free electrons in the n-channel available for conduction. The more negative the bias, lesser the number of free electrons in the channel. Since the negative voltage on the gate deplete channel, the device is referred to as depletion MOSFET. The depletion mode of operation is similar to JFET operation. When sufficient negative voltage is applied to gate the channel may be completely cut off and the corresponding $\mathrm{V}_{\mathrm{GS}}$ is called ( $\mathrm{V}_{\mathrm{GS}}$ (OFF)).

If a positive voltage is applied to gate with respect to source then the electrons are induced in the channel. The induced electrons constitute additional current from source to drain. If we increase $\mathrm{V}_{\mathrm{GS}}$ more in positive direction more number of electrons is induced and hence the drain current increases.

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That is, the application of a positive gate -to -source voltage has enhanced the number of charge carriers compared to that of when $\mathrm{V}_{\mathrm{GS}}=0 \mathrm{v}$. For this reason the mode in which the MOSFET. Operates for positive values of gate-to-source voltage is known as enhancement mode.



It is a plot of drain current versus drain source voltage for various value of gate-source voltage. The drain characteristics of depletion MOSFET is shown ii fig. Note that for negative of $\mathrm{V}_{\mathrm{GS}}$ the characteristics of depletion MOSFET is similar to those N-channel JFET. If the gate is made positive additional carrier are introduced in the channel and the channel conductivity increases. Therefore the depletion MOSFET consists of two regions of operation

The transfer characteristics of deletion MOSFET is shown in fig. The general shape of the transfer characteristics is similar to those for the JFET. However the deletion MOSFET can be operated with $\mathrm{V}_{\mathrm{GS}}>0$. As a result IDSS is not maximum drain current as it is for JFET. The equation fior transfer characteristics curve of depletion MOSFET is same as that of JFET.

The three circuit symbols for n-channel MOSFET and p-channel MOSFET are shown in fig.


Symbol of N-channel and P-channel MOSFET'S

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N-channel enhancement MOSFET (May/June-2013), (May/June2016), (Nov/Dec2015) (May 2017) (Apr/May 2018)

- The construction of n-channel enhancement MOSFET is shown in fig. like depletion MOSFET it also consists of a p-type substrate and two heavily doped n-regions that act as source and drain. The sio ${ }_{2}$ layer is present to isolate the gate from the region between the drain and source. The source and drain terminals are connected through metallic contacts to n -doped regions. But the enhancement MOSFET does not contain diffused channel MOSFET does not contain diffused channel between the source and drain


When the drain is made positive with repeat to source and no potential is applied to gate due to absence of the channel, a small drain current (ie., a reverse leakage current) flows. The we apply a positive voltage to that gate with respect to source and substrate, negative charge carriers are induced in the substrate the negative charge carriers which are minority carriers in the p-type substrate form an "inversion layer". As the gate potential is increased more and more negative charge carriers are induced. There negative carriers that are accumulated between source and drain current flows from source to drain through the induced channel. The magnetized of the drain current depends on the gate potential. Since the conduction of the channel is enhanced by the positive bias voltage on the gate the device known as enhancement MOSFET.

## Drain characteristics :

The drain characteristics of enhancement MOSFET is shown in fig.
The current IDSS for VGS=0 is very small of the order of nano amperes shown in fig. Note that the drain current increases with positive increases with positive increase in gate source have voltage.


## Transfer characteristics:

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The $n$-channel enhancement MOSFET requires a positive gate to source voltage for its operation fig shows the general transfer characteristics of an n-channel MOSFET. Since the drain current is zero for VGS=0, the IDSS is zero for this device. As VGS is made positive the current ID increases slowly at first and then more rapidly with an increase in VGS. The gate source voltage at which there is significant increase in drain current is called the threshold voltage and is referred to as VT or VGS the equation for the transfer characteristics of enhancement MOSFET differs as the curve states at VGS(th) rather than at VGS. The equation for transfer characteristics is $I_{D}=\mathrm{K}\left(V_{G S-} V_{G S(\text { th }))^{2}}\right.$

## UJT (UNIJUNCTION FIELD EFFECT TRANSISTOR)

7. (a) Explain the construction operation and characteristics of UJT? (May/June2016), (Nov/Dec2015) (Nov/Dec 2018)
(b) Describe the operation of UJT as a relaxation oscillator and derive its frequency of oscillation? (Nov/Dec 2016)

## (A) UNI-JUNCTION TRANSISTOR (UJT) <br> 

## Construction:


$\begin{array}{lll}\text { Fig.: (a) Basic structure of UJT } & \text { (b) Symbolic representation } & \text { (c) Equivalent circuit }\end{array}$
UJT is an n-type silicon bar in which p-type emitter is embedded. It has three terminals base1, base2 and emitter ' $E$ '. Between $B_{1}$ and $B_{2}$ UJT behaves like ordinary resistor and the internal resistances are given as $R_{B 1}$ and $R_{B 2}$ with emitter open $R_{B B}=R_{B 1}+R_{B 2}$. Usually the p-region is heavily doped and n-region is lightly doped. The equivalent circuit of UJT is as shown. When $V_{B B}$ is applied across $B_{1}$ and $B_{2}$, we find that potential at A is

$$
V_{A B 1}=\frac{V_{B B} R_{B 1}}{R_{B 1}+R_{B 2}}{ }_{B B}\left\lfloor\eta V_{B 1} V_{B 2}\right\rfloor
$$

$\eta$ is intrinsic standoff ratio of UJT and ranges between 0.51 and 0.82 . Resistor $R_{B 2}$ is between 5 to $10 \mathrm{~K} \Omega$.

When voltage $V_{B B}$ is applied between emitter ' $E$ ' with base $1 \quad B_{1}$ as reference and the emitter voltage $V_{E}$ is less than $\left(V_{D}+\eta V_{B E}\right)$ the UJT does not conduct. $\left(V_{D}+\eta V_{B B}\right)$ is designated as $V_{P}$ which is the value of voltage required to turn on the UJT. Once $V_{E}$ is equal to $V_{P} \equiv \eta V_{B E}+V_{D}$, then UJT is forward biased and it conducts.

The peak point is the point at which peak current $I_{P}$ flows and the peak voltage $V_{P}$ is across the UJT. After peak point the current increases but voltage across device drops, this is due to the fact that emitter starts to inject holes into the lower doped n-region. Since p-region is heavily doped compared to n-region. Also holes have a longer life time, therefore number of carriers in the base region increases rapidly. Thus potential at 'A' falls but current $I_{E}$ increases rapidly. $R_{B 1}$ Acts as a decreasing resistance.

The negative resistance region of UJT is between peak point and valley point. After valley point, the device acts as a normal diode since the base region is saturated and $R_{B 1}$ does not decrease again.


Fig.: V-I Characteristics of UJT
(B) Operation of UJT as a relaxation oscillator and its derivation- frequency of oscillation. (Nov 2016)

UJT as a relaxation oscillator consists of UJT and a capacitor $\mathrm{C}_{\mathrm{E}}$ which is charged through $\mathrm{R}_{\mathrm{E}}$ as the supply voltage $V_{B B}$ is switched $O N$. The voltage across the capacitor increases exponentially and when the capacitor voltage reaches the peak point voltage $\mathrm{V}_{\mathrm{p}}$, the UJT starts conducting and the capacitor voltage is discharged rapidly through $\mathrm{EB}_{1}$ and $\mathrm{R}_{1}$.After the peak point voltage of UJT is reached, it provides negative resistance to the discharge path which is useful in working of the relaxation oscillator. As the capacitor voltage reaches zero the device then cuts off and capacitor $\mathrm{C}_{\mathrm{E}}$ starts to charge again. This cycle is repeated continuously generating a saw tooth waveform across $\mathrm{C}_{\mathrm{E}}$.

The inclusion of external resistors $R_{2}$ and $R_{1}$ in series with $B_{2}$ and $B 1$ provides spike waveform. When the UJT fires, the sudden surge of current through $B_{1}$ causes drop across R 1 , which provides positive spikes. At the time of firing fall of $V_{\text {EB1 }}$ causes $\mathrm{I}_{2}$ to increases rapidly which generates negative going spikes across $\mathrm{R}_{2}$.

By changing the value of $\mathrm{R}_{\mathrm{E}}$ and $\mathrm{C}_{\mathrm{E}}$ the frequency of oscillation changes.


## Frequency of oscillation:

Voltage across the capacitance prior to breakdown is given by
$\mathrm{V}_{\mathrm{c}}=\mathrm{V}_{\mathrm{BB}}\left(1-\mathrm{e}^{-\mathrm{t} / \mathrm{RE}_{\mathrm{E}} \mathrm{C}_{\mathrm{E}}}\right)$
$\mathrm{R}_{\mathrm{E}} \mathrm{C}_{\mathrm{E}}$ - Charging time constant
Discharge of capacitor occurs when $\mathrm{V}_{\mathrm{C}}$ is equal to the peak point voltage $\mathrm{V}_{\mathrm{p}}$,
$\mathrm{V}_{\mathrm{p}}=\eta \mathrm{V}_{\mathrm{BB}}=\mathrm{V}_{\mathrm{BB}}\left(1-\mathrm{e}^{-\mathrm{t} / \mathrm{RE}^{\mathrm{E}}}\right)$
Where $\eta=\left(1-\mathrm{e}^{-\mathrm{t} / \mathrm{RE}_{\mathrm{E}}}\right)$
$\mathrm{e}^{-\mathrm{t} / \mathrm{R}_{\mathrm{E}} \mathrm{C}_{\mathrm{E}}}=1-\eta$
Taking Log on both side

$$
\begin{gathered}
\frac{\mathrm{t}}{\mathrm{R}_{\mathrm{E}} \mathrm{C}_{\mathrm{E}}}=\log _{\mathrm{e}} \frac{1}{(1-\eta)} \\
\mathrm{t}=\mathrm{R}_{\mathrm{E}} \mathrm{C}_{\mathrm{E}} \ln \frac{1}{(1-\eta)} \\
\mathrm{f}=1 / \mathrm{t}=\frac{1}{\mathrm{R}_{\mathrm{E}} \mathrm{C}_{\mathrm{E}} \ln \frac{1}{(1-\eta)}}
\end{gathered}
$$

## THYRISTOR (SCR)

8. DRAW AND EXPLAIN THE V-I CHARACTERISTICS OF THYRISTOR (SCR) (or) DISCUSS THE DIFFERENT MODES OF OPERATION OF THYRISTOR WITH THE HELP OF ITS STATIC V-I CHARACTERISTICS. (Nov/Dec 2017) (Apr/May 2018) (OR)
Outline the structure of SCR and explain its operation. Also, illustrate its V-I characteristics. (Apr/May 2019-R17)


Circuit diagram


Fig: V-I Characteristics of SCR

A typical V-I characteristics of a thyristor is shown above. In the reverse direction the thyristor appears similar to a reverse biased diode which conducts very little current until avalanche breakdown occurs. In the forward direction the thyristor has two stable states or modes of operation that are connected together by an unstable mode that appears as a negative resistance on the V-I characteristics. The low current high voltage region is the forward blocking state or the off state and the low voltage high current mode is the on state. For the forward blocking state the quantity of interest is the forward blocking voltage $V_{B O}$ which is defined for zero gate current. If a positive gate current is applied to a thyristor then the transition or break over to the on state will occur at smaller values of anode to cathode voltage as shown. Although not indicated the gate current does not have to be a dc current but instead can be a pulse of current having some minimum time duration. This ability to switch the thyristor by means of a current pulse is the reason for wide spread applications of the device.

However once the thyristor is in the on state the gate cannot be used to turn the device off. The only way to turn off the thyristor is for the external circuit to force the current through the device to be less than the holding current for a minimum specified time period.

## HOLDING CURRENT $I_{H}$

After an SCR has been switched to the on state a certain minimum value of anode current is required to maintain the thyristor in this low impedance state. If the anode current is reduced below the critical holding current value, the thyristor cannot maintain the current through it and reverts to its off state usually $I_{\mu}$ is associated with turn off the device.

## LATCHING CURRENT $I_{L}$

After the SCR has switched on, there is a minimum current required to sustain conduction. This current is called the latching current. $I_{L}$ associated with turn on and is usually greater than holding current.

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Fig.: Effects on gate current on forward blocking voltage
9. Sketch the four layer construction of an SCR and the two transistor equivalent circuit explains the device operation. (Non / Dec 2016)(May 2017)

A thyristor is the most important type of power semiconductor devices. They are extensively used in power electronic circuits. They are operated as bi-stable switches from non-conducting to conducting state.

A thyristor is a four layer, semiconductor of p-n-p-n structure with three p-n junctions. It has three terminals, the anode, cathode and the gate.

The word thyristor is coined from thyratron and transistor. It was invented in the year 1957 at Bell Labs. The Different types of Thyristors are

- Silicon Controlled Rectifier (SCR).
- TRIAC
- DIAC
- Gate Turn Off Thyristor (GTO)


## SILICON CONTROLLED RECTIFIER (SCR)

The SCR is a four layer three terminal device with junctions $J_{1}, J_{2}, J_{3}$ as shown. The construction of SCR shows that the gate terminal is kept nearer the cathode. The approximate thickness of each layer and doping densities are as indicated in the figure. In terms of their lateral dimensions Thyristors are the largest semiconductor devices made. A complete silicon wafer as large as ten centimeter in diameter may be used to make a single high power thyristor.


## Two transistor model of SCR

## OPERATION

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When the anode is made positive with respect the cathode junctions $J_{1} \& J_{3}$ are forward biased and junction $J_{2}$ is reverse biased. With anode to cathode voltage $V_{A K}$ being small, only leakage current flows through the device. The SCR is then said to be in the forward blocking state. If $V_{A K}$ is further increased to a large value, the reverse biased junction $J_{2}$ will breakdown due to avalanche effect resulting in a large current through the device. The voltage at which this phenomenon occurs is called the forward breakdown voltage $V_{B O}$. Since the other junctions $J_{1} \& J_{3}$ are already forward biased, there will be free movement of carriers across all three junctions resulting in a large forward anode current. Once the SCR is switched on, the voltage drop across it is very small, typically 1 to 1.5 V . The anode current is limited only by the external impedance present in the circuit.


Fig.: Simplified model of a thyristor
Although an SCR can be turned on by increasing the forward voltage beyond $V_{B O}$, in practice, the forward voltage is maintained well below $V_{B O}$ and the SCR is turned on by applying a positive voltage between gate and cathode. With the application of positive gate voltage, the leakage current through the junction $J_{2}$ is increased. This is because the resulting gate current consists mainly of electron flow from cathode to gate. Since the bottom end layer is heavily doped as compared to the p-layer, due to the applied voltage, some of these electrons reach junction $J_{2}$ and add to the minority carrier concentration in the p-layer. This raises the reverse leakage current and results in breakdown of junction $J_{2}$ even though the applied forward voltage is less than the breakdown voltage $V_{B O}$. With increase in gate current breakdown occurs earlier.

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## DIAC

## 10. Explain in detail about DIAC and its characteristics?



(b)

(a)

(b)

- The DIAC can be turned ON only when the applied voltage across it is main terminal reaches the break - over voltage.
- The M.T. 2 is positive with respect to M.T.1, the DIAC passes current through the DIAC $P_{1} N_{1} P_{2} N_{2}$ from M.T. 2 to
- M.T. 1 as shown in Fig. 5.12 (a). The DIAC turn 'ON' the applied voltage makes M.T. 2 negative with respect to the M.T.1, the DIAC current through the diode
- When the current drops below the holding value. It is used as a triggering device.


## Characteristics of a DIAC

The DIAC is operated with M.T. 2 positive with respect to M.T.1, the V I characteristics obtained is as shown in Fig. 5.13 by the curve marked $O A B$. Similarly the DIAC is operated with its M.T. 2 negative with respect to M.T.I, the V-1 characteristics obtained as shown in Fig. 5.13 by the curve marked $O C D$.

## Applications

The DIAC is used as a triggering device; it is not a control device. It is used in,

- Temperature control
- Triggering of TRIAC
- Light diming circuits
- Motor speed control


## Forward current



Fig. 5.13

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## $\underline{\underline{T R I A C}}$

## 11. EXPLAIN THE CONSTRUCTION, OPERATION \& STATIC CHARACTERISTICS OF TRIAC

A triac is a three terminal bi-directional switching thyristor device. It can conduct in both directions when it is triggered into the conduction state. The triac is equivalent to two SCRs connected in anti-parallel with a common gate. Figure below shows the triac structure. It consists of three terminals viz., $M T_{2}, M T_{1}$ and gate G.


Fig. TRIAC Structure


Fig. TRIAC Symbol

The gate terminal G is near the $M T_{1}$ terminal. Figure above shows the triac symbol. $M T_{1}$ is the reference terminal to obtain the characteristics of the triac. A triac can be operated in four different modes depending upon the polarity of the voltage on the terminal $M T_{2}$ with respect to $M T_{1}$ and based on the gate current polarity.

The characteristics of a triac are similar to that of an SCR, both in blocking and conducting states. A SCR can conduct in only one direction whereas triac can conduct in both directions.

## MODE 1: $M T_{2}$ positive, Positive gate current ( $I^{+}$mode of operation)

When $M T_{2}$ and gate current are positive with respect to $\mathrm{MT}_{1}$, the gate current flows through $\mathrm{P}_{2}-\mathrm{N}_{2}$ junction as shown in figure below. The junction $\mathrm{P}_{1}-\mathrm{N}_{1}$ and $\mathrm{P}_{2}-\mathrm{N}_{2}$ are forward biased but junction $\mathrm{N}_{1}-\mathrm{P}_{2}$ is reverse biased. When sufficient number of charge carriers is injected in $\mathrm{P}_{2}$ layer by the gate current the junction $\mathrm{N}_{1}-\mathrm{P}_{2}$ breakdown and triac starts conducting through $\mathrm{P}_{1} \mathrm{~N}_{1} \mathrm{P}_{2} \mathrm{~N}_{2}$ layers. Once triac starts conducting the current increases and it's V-I characteristics is similar to that of thyristor. Triac in this mode operates in the first-quadrant.


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MODE 2: MT $_{2}$ positive, Negative gate current ( $I^{-}$mode of operation)


When $\mathrm{MT}_{2}$ is positive and gate G is negative with respect to $\mathrm{MT}_{1}$ the gate current flows through $\mathrm{P}_{2}-\mathrm{N}_{3}$ junction as shown in figure above. The junction $\mathrm{P}_{1}-\mathrm{N}_{1}$ and $\mathrm{P}_{2}-\mathrm{N}_{3}$ are forward biased but junction $\mathrm{N}_{1}-\mathrm{P}_{2}$ is reverse biased. Hence, the triac initially starts conducting through $\mathrm{P}_{1} \mathrm{~N}_{1} \mathrm{P}_{2} \mathrm{~N}_{3}$ layers. As a result the potential of layer between $\mathrm{P}_{2}-$ $\mathrm{N}_{3}$ rises towards the potential of $\mathrm{MT}_{2}$. Thus, a potential gradient exists across the layer $\mathrm{P}_{2}$ with left hand region at a higher potential than the right hand region. This results in a current flow in $\mathrm{P}_{2}$ layer from left to right, forward biasing the $\mathrm{P}_{2} \mathrm{~N}_{2}$ junction. Now the right hand portion $\mathrm{P}_{1}-\mathrm{N}_{1}-\mathrm{P}_{2}-\mathrm{N}_{2}$ starts conducting. The device operates in first quadrant. When compared to Mode 1 , triac with $\mathrm{MT}_{2}$ positive and negative gate current is less sensitive and therefore requires higher gate current for triggering.

## MODE 3: MT $_{2}$ negative, Positive gate current ( $\mathrm{III}^{+}$mode of operation)

When $\mathrm{MT}_{2}$ is negative and gate is positive with respect to $\mathrm{MT}_{1}$ junction $\mathrm{P}_{2} \mathrm{~N}_{2}$ is forward biased and junction $\mathrm{P}_{1^{-}}$ $N_{1}$ is reverse biased. $N_{2}$ layer injects electrons into $P_{2}$ layer as shown by arrows in figure below. This causes an increase in current flow through junction $\mathrm{P}_{2}-\mathrm{N}_{1}$. Resulting in breakdown of reverse biased junction $\mathrm{N}_{1}-\mathrm{P}_{1}$. Now the device conducts through layers $\mathrm{P}_{2} \mathrm{~N}_{1} \mathrm{P}_{1} \mathrm{~N}_{4}$ and the current starts increasing, which is limited by an external load.


The device operates in third quadrant in this mode. Triac in this mode is less sensitive and requires higher gate current for triggering.

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MODE 4: MT $_{2}$ negative, Negative gate current ( III $^{-}$mode of operation)


In this mode both $\mathrm{MT}_{2}$ and gate G are negative with respect to $\mathrm{MT}_{1}$, the gate current flows through $\mathrm{P}_{2} \mathrm{~N}_{3}$ junction as shown in figure above. Layer $\mathrm{N}_{3}$ injects electrons as shown by arrows into $\mathrm{P}_{2}$ layer. These results in increase in current flow across $\mathrm{P}_{1} \mathrm{~N}_{1}$ and the device will turn ON due to increased current in layer $\mathrm{N}_{1}$. The current flows through layers $\mathrm{P}_{2} \mathrm{~N}_{1} \mathrm{P}_{1} \mathrm{~N}_{4}$. Triac is more sensitive in this mode compared to turn ON with positive gate current. (Mode 3).

Triac sensitivity is greatest in the first quadrant when turned ON with positive gate current and also in third quadrant when turned ON with negative gate current. When $M T_{2}$ is positive with respect to $M T_{1}$ it is recommended to turn on the triac by a positive gate current. When $M T_{2}$ is negative with respect to $M T_{1}$ it is recommended to turn on the triac by negative gate current. Therefore Mode 1 and Mode 4 are the preferred modes of operation of a triac ( $I^{+}$mode and $I I I^{-}$mode of operation are normally used).

## TRIAC CHARACTERISTICS

Figure below shows the circuit to obtain the characteristics of a triac. To obtain the characteristics in the third quadrant the supply to gate and between $M T_{2}$ and $\mathrm{MT}_{1}$ are reversed.


Figure below shows the V-I Characteristics of a triac. Triac is a bidirectional switching device. Hence its characteristics are identical in the first and third quadrant. When gate current is increased the break over voltage decreases.


Fig.: Triac Characteristic
Triac is widely used to control the speed of single-phase induction motors. It is also used in domestic lamp dimmers and heat control circuits, and full wave AC voltage controllers.

## IGBT-Structure, Operation \& Characteristics

## 12. EXPLAIN THE CONSTRUCTION, OPERATION \& STATIC CHARACTERISTICS OF INSULATED GATE BIPOLAR TRANSISTOR (IGBT). (NOV/DEC-2012) (May/June2016) (May 2017) (Nov/Dec 2018 R-13)

IGBT is a voltage-controlled device. It has high input impedance like a MOSFET and low on-state conduction losses like a BJT.

Figure below shows the basic silicon cross-section of an IGBT. Its construction is same as power MOSFET except that $\mathrm{n}^{+}$layer at the drain in a power MOSFET is replaced by $\mathrm{P}^{+}$substrate called collector.


Structure


Symbol

Fig.: Insulated Gate Bipolar Transistor
IGBT has three terminals gate (G), collector (C) and emitter (E). With collector and gate voltage positive with respect to emitter the device is in forward blocking mode. When gate to emitter voltage becomes greater than the threshold voltage of IGBT, a n-channel is formed in the P-region. Now device is in forward conducting state. In this state $p^{+}$substrate injects holes into the epitaxial $n^{-}$layer. Increase in collector to emitter voltage will result in increase of injected hole concentration and finally a forward current is established.

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## CHARACTERISTIC OF IGBT

Figure below shows circuit diagram to obtain the characteristic of an IGBT. An output characteristic is a plot of collector current $I_{C}$ versus collector to emitter voltage $V_{C E}$ for given values of gate to emitter voltage $V_{G E}$.


Fig.: Circuit Diagram to Obtain Characteristics


Fig. Output Characteristics
A plot of collector current $I_{C}$ versus gate-emitter voltage $V_{G E}^{O m}$ for a given value of $V_{C E}$ gives the transfer characteristic. Figure below shows the transfer characteristic.

## Note

Controlling parameter is the gate-emitter voltage $V_{G E}$ in IGBT. If $V_{G E}$ is less than the threshold voltage $V_{T}$ then IGBT is in OFF state. If $V_{G E}$ is greater than the threshold voltage $V_{T}$ then the IGBT is in ON state.

IGBTs are used in medium power applications such as ac and dc motor drives, power supplies and solid state relays.


Fig. Transfer Characteristic

1. Design a voltage divider bias circuit for transistor to establish the quiescent point $\mathrm{V}_{\mathrm{CE}}=\mathbf{1 2 v}, \mathrm{Ic}=$ 1.5 mA , Stability factor $\mathrm{S} \leq 3, Q=50, V_{B E}=0.7 \mathrm{~V}, V C C=22.5 \mathrm{~V}$ and $\mathrm{Rc}=5.6 \mathrm{~K} \Omega$.
(May 2017) (Nov/Dec 2017)
$\beta=50, \quad V_{B E}=0.7 \mathrm{~V}, \quad V_{C C}=22.5 \mathrm{~V}, \quad R_{C}=5.6 \mathrm{k} \Omega, \quad V_{C E}=12 \mathrm{~V}, \quad I_{C}=1.5 \mathrm{~mA}, \quad S \leq 3$ Emitter Resistance $\left(R_{E}\right)$
$V_{C E}=V_{C C}-I_{C}\left(R_{C}+R_{E}\right)$
$12=22.5-\left(1.5 \times 10^{-3}\right)\left(5.6 \times 10^{3}+R_{E}\right)=14.1-1.5 \times 10^{-3} R_{E}$
$R_{E}=1.4 \times 10^{3} \Omega=1.4 k \Omega$
Resistances $R_{1}$ and $R_{2}$
Stability factor (s)
$3=\frac{\beta+1}{1+\beta\left(\frac{R_{\underline{E}}}{R_{t h}+R_{E}}\right)}=\frac{50+1 \text { w.EnggT}}{1+50 \times \frac{1.4 \times 10^{3}}{R_{t h}+1.4 \times 10^{3}}}=\frac{\mathrm{ecom} 51}{1+\frac{70 \times 10^{3}}{R_{t h}+1.4 \times 10^{3}}}$
$3\left[\frac{\left(R_{\text {th }}+1.4 \times 10^{3}\right)+70 \times 10^{3}}{R_{t h}+1.4 \times 10^{3}}\right]=51$
$3\left[\left(R_{t h}+1.4 \times 10^{3}\right)\right]+\left(70 \times 10^{3}\right)=51\left(R_{t h}+1.4 \times 10^{3}\right)$
$48\left[R_{t h}+\left(1.4 \times 10^{3}\right)\right]=210 \times 10^{3}$
$R_{t h}+1.4 \times 10^{3}=\frac{\left(210 \times 10^{3}\right)}{48}=4375$
$R_{t h}=4375-1.4 \times 10^{3} ; R_{t h}=2975 \Omega ; R_{t h}=2.98 \mathrm{k} \Omega$
For good voltage divider the value of resistor
$R_{2}=0.1 \beta . R_{E}=0.1 \times 50 \times\left(1.4 \times 10^{3}\right)=7 \times 10^{3} \Omega=7 k \Omega$
Thevenin's Resistance ( $R_{t h}$ )
$2.98=R_{1} \| R_{2}=\frac{R_{1} \cdot R_{2}}{R_{1}+R_{2}}=\frac{7 R_{1}}{R_{1}+7}$
$2.98\left(R_{1}+7\right)=7 R_{1}$; $4.02 R_{1}=20.86$
$R_{1}=\frac{20.86}{4.02}=5.2 \mathrm{k} \Omega$
2. For an n channel silicon FET with $\mathrm{a}=3^{*} 10^{-4} \mathbf{c m}$ and $\mathrm{ND}_{\mathrm{D}}=10^{15}$ electronics $/ \mathrm{cm}^{3}$ find (a) the pinch off voltage and (b) the channel half width for $V_{G S}=1 / 2 V P$ and $I d=0$. (May / Jun 2016)

## Solution:

The relative dielectric constant of silicon is given in table 5-1 as 12 , and hence $\epsilon=12 \epsilon_{0}$. Using the value of $e$ and $\epsilon_{0}$ from appendixes A and B , we have from Eq expressed in mks units,

$$
V_{P}=\frac{1.60 \times 10^{-19} \times 10^{21} \times\left(3 \times 10^{-6}\right)^{2}}{2 \times 12 \times\left(36 \pi \times 10^{9}\right)^{-1}}=6.8 \mathrm{~V}
$$

b. Solution Eq for b , we obtain for $\mathrm{V}_{\mathrm{GS}}=1 / 2 \mathrm{~V}_{\mathrm{P}}$

$$
b=a\left[1-\left({\left(\frac{V_{G S}}{V_{P}}\right.}^{1 / 2}\right]=\left(3 \times 1^{-4}\right)\left[1-\left(\frac{1}{2}\right)^{\frac{1}{2}}\right]=0.87 \times 10^{-4} \mathrm{~cm}\right.
$$

Hence the channel width has been reduced to about one third its value for $\mathrm{V}_{\mathrm{GS}}=0$
3. Determine the base current for the $C B$ transistor circuit if $I_{C}=\mathbf{8 0} \mathbf{~ m A}$ and $Q=170$. (Nov/Dev 2016)

Given
$\mathrm{I}_{\mathrm{C}}=80 \mathrm{~mA}$
$\beta=17 \varphi_{\dot{C}}{ }_{I_{B}}^{\beta}=\frac{{ }^{80 \times 10^{-3}}}{I_{B}}=170 \therefore I_{B}=\frac{I_{C}}{\beta}=\frac{{ }^{80 \times 10^{-3}}}{170}=0.4706 \mathrm{~mA}$
4. Draw the two-transistor equivalent circuit of SCR? (May 2017)

(a)

5. A transistor has a typical $Q=100$. If the collector current is $\mathbf{4 0} \mathbf{m A}$. What is the value of emitter current? (May 2017)
Given: $\mathrm{I}_{\mathrm{C}}=40 \mathrm{~mA} \quad \beta=100 \quad \beta=\frac{I_{c}}{I_{B}}$
$\therefore I_{B}=\frac{I_{c}}{\beta}=\frac{40 \times 10^{-3}}{100}=0.0004 \mathrm{~A}$
$\mathrm{I}_{\mathrm{E}}=\mathrm{I}_{\mathrm{B}}+\mathrm{I}_{\mathrm{C}} \quad \mathrm{I}_{\mathrm{E}}=0.0004+40 \times 10^{-3}=0.0404 \mathrm{~A}$

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6. If the collector current is 2 mA and the base current is $25 \mu \mathrm{~A}$, what is the emitter current?

Solution: $\quad \mathrm{I}_{\mathrm{C}}=2 \mathrm{~mA}$,

$$
\begin{aligned}
& \mathrm{I}_{\mathrm{B}}=25 \mu \mathrm{~A}, \\
& \quad \therefore \mathrm{IE}=\mathbf{2 . 0 2 5 m A}
\end{aligned}
$$

7. Calculate $I_{C}$ and $I_{E}$ for a transistor that has $a=0.99$ and $I_{B}=150 \mu A$. Determine the value of $Q_{d c}$ for the transistor? (Nov / Dec 2015)
Solution:

$$
\beta=\frac{\alpha}{1-\alpha}=\frac{0.99}{1-099}=99
$$

$\beta=\frac{I_{C}}{I_{B}} ; I_{C}=\beta \times I_{B}=99 \times 150 \mu A=14 \mathrm{~mA}$
$\alpha=\frac{I_{C}}{I_{E}} ; I_{E}=\frac{I c}{\alpha}=\frac{14}{0.99}=14.14 \mathrm{~mA}$
8. A germanium transistor is to be operated at zero signal $I_{C}=1 \mathrm{~mA}$. If the collector supply voltage $V_{C C}=12 \mathrm{~V}$, what is the value of $R_{B}$ in the base resistor method? Assume $\beta=100$. If another transistor of same batch with $\boldsymbol{\beta}=\mathbf{5 0}$ is used, what will be new value of zero signal Ic for same $\mathrm{R}_{\mathrm{B}}$ ? Comment on the results. (Nov/Dec 2018-R17)(13 Marks)
Solution:

$$
\begin{aligned}
\mathrm{V}_{\mathrm{CC}} & =12 \mathrm{~V}, \quad \beta=100 \\
\mathrm{~V}_{\mathrm{BE}} & =0.3 \mathrm{~V} \because \text { Germanium transistor } \\
\text { Zero signal } \mathrm{I}_{\mathrm{C}} & =1 \mathrm{~mA} \\
\therefore \quad \text { Zero signal } \mathrm{I}_{\mathrm{B}} & =\frac{\mathrm{I}_{\mathrm{C}}}{\beta}=\frac{1 \mathrm{~mA}}{100}=0.01 \mathrm{~mA}
\end{aligned}
$$

Using the relation, $V_{C C}=I_{B} R_{B}+V_{B E}$ we have

$$
\mathrm{R}_{\mathrm{B}}=\frac{\mathrm{V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{BE}}}{\mathrm{I}_{\mathrm{B}}}=\frac{12-0.3}{0.01 \mathrm{~mA}}=1170 \mathrm{k} \Omega
$$

ii)

$$
\beta=50
$$

Using the relation, $V_{C C}=I_{B} R_{B}+V_{B E}$ we have

$$
\mathrm{I}_{\mathrm{B}}=\frac{\mathrm{V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{BE}}}{\mathrm{R}_{\mathrm{B}}}=\frac{12-0.3}{1170 \mathrm{k} \Omega}=0.01 \mathrm{~mA}
$$

$\therefore$ Zero signal $\mathrm{I}_{\mathrm{C}}=\beta \mathrm{I}_{\mathrm{B}}=50 \times 0.01 \mathrm{~mA}=0.5 \mathrm{~mA}$

Comment: It is clear from the above example that with the change in transistor parameter $\beta$, the zero-signal collector current has changed from 1 mA to 0.5 mA . Therefore, the base resistor method cannot provide stabilization.
9. The intrinsic stand-off ratio for a UJT is 0.6 . If the inter base resistance is $10 \mathrm{~K} \Omega$, what are the value of $\mathbf{R}_{\mathrm{B} 1}$ and $\mathrm{R}_{\mathrm{b} 2}$ ? (Nov/Dec 2018-R17) (4 Marks)

$$
\begin{aligned}
\text { Sol. : } \quad \begin{aligned}
\eta & =0.6, R_{B B}=10 \mathrm{k} \Omega \\
\eta & =\left.\frac{R_{B 1}}{R_{B B}}\right|_{I_{E}=0} \text { i.e. } 0.6=\frac{R_{B 1}}{10} \\
\therefore \quad R_{B 1} & =6 \mathrm{k} \Omega \\
\therefore \quad R_{B B} & =R_{B 1}+R_{B 2} \text { i.e } 10=6+R_{B 2} \\
\therefore \quad R_{B 2} & =4 \mathrm{k} \Omega
\end{aligned} . \begin{array}{ll} 
\\
\therefore \quad R_{B 2}
\end{array}
\end{aligned}
$$

10. When $V_{G S}$ of a JFET changes from -3.1 $\overline{\mathrm{V}}$ to $-\mathbf{3} \mathrm{V}$, the drain current changed from 1 mA to 1.3 mA. Find the value of transconductance. (Nov/Dec 2018-R17) (2 Marks)

## Solution:

$$
g_{m}=\frac{\Delta I_{D}}{\Delta V_{G S}}=\frac{(1.3-1) \times 10^{-3}}{(3.1-3)}=3 \mathrm{~mA} / \mathrm{V}
$$

11. Find the $\mathbf{Q}$ point of the transistor shown below. Also draw the DC load line. Give $\boldsymbol{\beta}=\mathbf{1 0 0}$ and $\mathrm{V}_{\mathrm{BE}}=0.7 \mathrm{~V}$. (Nov/Dec 2018-R17) (15 Marks)

## Sol. :

$$
\begin{aligned}
\mathrm{I}_{\mathrm{B}}= & \frac{\mathrm{V}_{\mathrm{EE}}-\mathrm{V}_{\mathrm{BE}}}{\mathrm{R}_{\mathrm{B}}+(1+\beta) \mathrm{R}_{\mathrm{E}}}=\frac{10-0.7}{47 \mathrm{~K}+(1+100) 4.7 \mathrm{~K}}=17.83 \mu \mathrm{~A} \\
\mathrm{I}_{\mathrm{C}}= & \beta \mathrm{I}_{\mathrm{B}}=100 \times 17.83 \mu \mathrm{~A}=1.783 \mathrm{~mA} \\
\mathrm{I}_{\mathrm{E}} & =\mathrm{I}_{\mathrm{C}}+\mathrm{I}_{\mathrm{B}}=1.783 \mathrm{~mA}+17.83 \mu \mathrm{~A}=1.8 \mathrm{~mA} \\
\mathrm{~V}_{\mathrm{C}} & =\mathrm{V}_{\mathrm{CC}}-\mathrm{I}_{\mathrm{C}} \mathrm{R}_{\mathrm{C}}=10-\left(1.783 \times 10^{-3} \times 1 \times 10^{3}\right) \\
& =8.217 \mathrm{~V} \\
\mathrm{~V}_{\mathrm{E}} & =-\mathrm{V}_{\mathrm{EE}}+\mathrm{I}_{\mathrm{E}} \mathrm{R}_{\mathrm{E}}=-10 \mathrm{~V}+\left(1.8 \times 10^{-3} \times 4.7 \times 10^{3}\right) \\
& =-\mathbf{1 . 5 4} \mathrm{V}
\end{aligned}
$$


$\therefore \quad \mathrm{V}_{\mathrm{CE}}=\mathrm{V}_{\mathrm{C}}-\mathrm{V}_{\mathrm{E}}=8.217-(-1.54)=9.757 \mathrm{~V}$
$\therefore \quad$ The $Q$ point of the circuit is $\mathbf{V}_{\mathrm{CE}}=9.757 \mathrm{~V}$ and

$$
\mathrm{I}_{\mathrm{C}}=1.783 \mathrm{~mA}
$$



$$
\begin{aligned}
\mathrm{V}_{\mathrm{CE}} & =0, \mathrm{I}_{\mathrm{C}}=\frac{\mathrm{V}_{\mathrm{CC}}-\left(-\mathrm{V}_{\mathrm{EE}}\right)}{\mathrm{R}_{\mathrm{C}}+\mathrm{R}_{\mathrm{E}}} \\
& =\frac{10+10}{1 \mathrm{~K}+4.7 \mathrm{~K}}=3.5 \mathrm{~mA}
\end{aligned}
$$

when $\mathrm{I}_{\mathrm{C}}=0, \mathrm{~V}_{\mathrm{CE}}=\mathrm{V}_{\mathrm{CC}}-\left(-\mathrm{V}_{\mathrm{EE}}\right)=10+10=20 \mathrm{~V}$
12. In a self-bias n-channel JFET, the operating point is to be set at $I_{D}=1.5 \mathrm{~mA}$ and $V_{D S}=10 \mathrm{~V}$. The parameters are $I_{D S S}=5 \mathrm{~mA}$ and $V_{G S}(o f f)=-2 V$. Find the values of $R_{S}$ and $R_{D}$ if $V_{D D}=20 \mathrm{~V}$. (Nov/Dec 2018-R17) (9 Marks)


Given : $\mathrm{I}_{\mathrm{D}}=1.5 \mathrm{~mA}, \mathrm{I}_{\mathrm{DSS}}=5 \mathrm{~mA}$,
$\mathrm{V}_{\mathrm{GS}(\mathrm{OFF})}=-2 \mathrm{~V}=\mathrm{V}_{\mathrm{p}}, \mathrm{V}_{\mathrm{DD}}=20 \mathrm{~V}$ and $\mathrm{V}_{\mathrm{DS}}=10 \mathrm{~V}$
Step 1 : Calculate $V_{G S}$
We have $I_{D}=I_{D S S}\left[1-\frac{\mathrm{V}_{G S}}{\mathrm{~V}_{\mathrm{P}}}\right]^{2}$
$\therefore \quad \mathrm{V}_{\mathrm{GS}}=\mathrm{V}_{\mathrm{P}}\left[1-\sqrt{\frac{\mathrm{I}_{\mathrm{D}}}{\mathrm{I}_{\mathrm{DSS}}}}\right]=-2\left[1-\sqrt{\frac{1.5}{5}}\right]=-0.9 \mathrm{~V}$
Step 2 : Calculate $R_{s}$

$$
\begin{array}{rlrl} 
& & \mathrm{V}_{\mathrm{GS}} & =\mathrm{V}_{\mathrm{G}}-\mathrm{V}_{\mathrm{S}}=0-\mathrm{V}_{\mathrm{S}}=-0.9 \mathrm{~V} \\
\therefore & \mathrm{~V}_{\mathrm{S}} & =0.9 \mathrm{~V} \\
\therefore & \mathrm{R}_{\mathrm{S}} & =\frac{\mathrm{V}_{\mathrm{S}}}{\mathrm{I}_{\mathrm{D}}}=\frac{0.9 \mathrm{~V}}{1.5 \mathrm{~mA}}=600 \Omega
\end{array}
$$

# EC8353-ELECTRONIC DEVICES AND CIRCUITS 

## UNIT-III AMPLIFIERS

## PART-A

## BJT Small Signal Model

1. Which is the BJT configuration is suitable for impedance matching application and why?

CC configuration is suitable for impedance matching application because of very high input impedance and low output impedance.
2. Draw the hybrid small signal model of BJT device. (MAY/JUNE2016)

3. What are the tools used for small signal analysis of BJT?

- h - Parameter circuit model.
- z - Parameter circuit model.
- y - Parameter circuit model.
- Trans-conductance parameter circuit model.
- Physical model
- T-model

4. What are the steps used for small signal analysis of BJT?

- Draw the actual circuit diagram
- Replace coupling capacitors and emitter bypass capacitor by short circuit.
- Replace dc source by a short circuit. In other words, short $\mathrm{V}_{\mathrm{CC}}$ and ground lines.

5. State the phase relationship between input / output currents and phase relationship between the input / output voltages of various transistors configurations. (Nov/Dec 2018)

For all the transistor configurations, input and output currents are in phase.
The input and output voltages of both CB and CC configuration are in phase. But in common-emitter amplifier the input and output voltages are $180^{\circ}$ out of phase.

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6. Draw the low frequency hybrid model of BJT in common emitter configuration.


## CE, CB, CC Amplifiers- $\underline{\underline{\text { Gain }} \text { and frequency response }}$

7. Draw the hybrid small signal model of CB configuration? (Apr/May 2018)

8. Why emitter is always forward biased and collector is always reverse biased with respect to base?

To supply majority charge carrier to base and to remove the charge carriers away from the collector-base junction.
9. Why CE configuration is most popular in amplifier circuits?

Because it's current, voltage and power gain are quite high and the ratio of output impedance and input impedance are quite moderate.
10. Give the voltage gain for $C E$ configuration including source resistance.

$$
\begin{gathered}
\mathrm{A}_{\mathrm{VS}}=\mathrm{A}_{\mathrm{i}} \times \mathrm{R}_{\mathrm{L}} / \mathrm{R}_{\mathrm{S}}+\mathrm{R}_{\mathrm{i}} \\
=\left(-\mathrm{h}_{\mathrm{fe}} / 1+\mathrm{h}_{\mathrm{oe}} \mathrm{R}_{\mathrm{L}}\right) \times \mathrm{R}_{\mathrm{L}} /\left(\mathrm{R}_{\mathrm{S}}+\mathrm{R}_{\mathrm{i}}\right)
\end{gathered}
$$

11. Define the $h_{i e}$ and $h_{f e}$ for a common emitter transistor configuration.

From the h - parameter equivalent circuit of the common emitter configuration.
$\mathrm{H}_{\mathrm{ie}}=\Delta \mathrm{V}_{\mathrm{BE}} / \Delta \mathrm{I}_{\mathrm{B}} \mid \mathrm{V}_{\mathrm{CE}}$ constant
$\mathrm{H}_{\mathrm{fe}}=\Delta \mathrm{I}_{\mathrm{C}} / \Delta \mathrm{I}_{\mathrm{B}} \mid \mathrm{V}_{\mathrm{CE}}$ constant
12. Give the current gain expression for a common emitter transistor configuration.

Current gain for common emitter configuration:

$$
\mathrm{A}_{\mathrm{i}}=-\mathrm{I}_{\mathrm{C}} / \mathrm{I}_{\mathrm{b}}=-\mathrm{h}_{\mathrm{fe}} / 1+\mathrm{h}_{\mathrm{oe}} \mathrm{R}_{\mathrm{L}}
$$

13. What is trans-conductance? Give its expression for MOSFET. (Nov/Dec 2017)

The trans-conductance is a ratio of output current to input voltage and hence it represents the gain of the MOSFET.
Tran conductance expression for MOSFET

$$
\begin{aligned}
& \mathrm{g}_{\mathrm{m}}=2 \sqrt{ }\left(\mathrm{KI}_{\mathrm{DQ}}\right) \\
& \mathrm{I}_{\mathrm{DQ}}=\mathrm{K}\left(\mathrm{~V}_{\mathrm{GSQ}}-\mathrm{V}_{\mathrm{T}}\right)^{2}
\end{aligned}
$$

14. State the values of $\mathrm{C}_{\mathrm{gd}}$ and $\mathrm{C}_{\mathrm{gs}}$ in various operating regions of MOSFET.

Values of gate capacitances in Triode Region:

$$
\mathrm{C}_{\mathrm{gs}}=\mathrm{C}_{\mathrm{gd}}=\left(\mathrm{WL} \mathrm{C}_{\mathrm{ox}}\right)^{1 / 2}
$$

Values of gate capacitances in Saturation Region:

$$
\begin{aligned}
& \mathrm{C}_{\mathrm{gs}}=\left(\mathrm{WL} \mathrm{Cox}_{\mathrm{ox}}\right) 2 / 3 \\
& \mathrm{C}_{\mathrm{gd}}=0
\end{aligned}
$$

Values of gate capacitances in Cut - off Region:

$$
\begin{gathered}
\mathrm{C}_{\mathrm{gs}}=\mathrm{C}_{\mathrm{gd} \mathrm{~d}}=0 \\
\mathrm{C}_{\mathrm{gd}}=\text { WL C Cox } \\
\mathrm{C}_{\mathrm{ox}}-\text { Gate Capacitance. }
\end{gathered}
$$

## 15. List various gate capacitances in MOSFET.

There are three gate capacitances in MOSFET:
$\mathrm{Cgs}_{\mathrm{gs}}$ gate source capacitance,
$\mathrm{C}_{\mathrm{gd}}$ - gate drain Capacitance, and
$\mathrm{C}_{\mathrm{gb}}$ - gate body Capacitance.

## CS and Source follower

16. Explain the effect of source resistor on CS MOSFET amplifier.

The source resistor is introduced to stabilize the Q - point against variations in the MOSFET parameters. In BJT circuits, a source resistor reduces the small gain.
17. What is source follower? (Apr/May 2018)

A common-drain amplifier, also known as a source follower, is one of three basic single-stage field effect transistor (FET) amplifier topologies, typically used as a voltage buffer.

## Gain and frequency response

18. What is the significance of octaves and decades in frequency response?

- Octaves and Decades are the measure of change in frequency.
- Ten times change in frequency is called a Decade. On the other hand, an Octave corresponds to a doubling of the frequency.
- For example, an increase in frequency from 100 Hz to 200 Hz is an octave. Likewise, a decrease in frequency from 100 Hz to 50 Hz is also an octave.
- If the frequency is reduced to one hundredth of fc (from fc to 0.01 fc ), the drop in the voltage gain is -40 dB . In each decade the voltage gain drops by -20 db .


## 19. Draw general frequency response curve (or) haqtoppeer firquencies of an amplifier.



- In the above diagram the frequency $f_{2}$ lies in high frequency region, while the frequency $f_{1}$ lies in low frequency region.
- These two frequencies are also referred to as half power half - power frequencies since gain or output voltage drops to $70.7 \%$ of maximum value and this represents a power level of one half the power at the reference frequency in mid - frequency region.


## Additional Questions

20. What is the relation between $\alpha$ and $\beta$ of the transistor?

$$
\alpha=\frac{\beta}{\beta+1}
$$

21. Why must the base be narrow for the transistor action?
$\beta$ is the ratio of IC to IB. IB becomes less if the base width is narrow. Higher value of $\beta$ can be obtained with lower value of base current.
22. What are emitter efficiency and base transport factor of a transistor?

The ratio of current of injected carriers at emitter junction to the total emitter current is called the emitter injection efficiency. Transport Factor, $\beta=$ IC / IB
23. What is the relation between the current of a transistor?
$\mathrm{I}_{\mathrm{E}}=\mathrm{I}_{\mathrm{B}}+\mathrm{I}_{\mathrm{C}}$
24. How many h-parameters are there for a transistor?

* $h_{r}$-reverse voltage gain
$\dot{*} \mathrm{~h}_{0}$-output admittance.
* $\mathrm{h}_{\mathrm{i}}$,-input impedance
* $\mathrm{h}_{\mathrm{f}}$-forward current gain

25. Why h-parameters are called hybrid parameters?

Because they have different units are mixed with other parameters.
26. What are the advantages of the h-parameters? (Apr/May 2011)
(1) Real numbers up to radio frequencies
(2) Easy to measure
(3) Determined from transistor static characteristics curve
(4) Convenient to use in the circuit analysis and design
(5) Easily convertible from one configuration to other
27. Draw the hybrid model for a transistor. (Eng Treet

28. What are $h$-parameters? Define the four $h$-parameters.

One of a set of four transistor equivalent circuit parameters that conveniently specify transistor performance for small voltage and current in a particular circuit also known as hybrid parameter.

Input resistance with output short - circuited, in $\Omega$.

$$
\mathbf{h}_{11}=\mathbf{V}_{\mathrm{i}} / \mathbf{I}_{\mathbf{i}} \mid \mathbf{V}_{\mathbf{0}}=\mathbf{0}
$$

Fraction of output voltage at input with input open circuited. This parameter is ratio of similar quantities, hence unitless.
$\mathbf{h}_{12}=\mathbf{V}_{\mathbf{i}} / \mathbf{V}_{\mathrm{o}} \mid \mathbf{I}_{\mathbf{i}}=\mathbf{0}$
Forward current transfer ratio or current gain with output short circuited.
$\mathbf{h}_{21}=I_{0} / I_{i} \mid V_{0}=0$
This parameter is a ratio of similar quantities, hence unitless. Output admittance with input open - circuited, in mhos.

$$
h_{22}=\mathbf{I}_{0} / V_{0} \mid \mathbf{I}_{\mathbf{i}}=\mathbf{0}
$$

29. State Miller's theorem. (Nov/Dec 2016)

Miller's theorem states that, if Z is the impedance connected between two nodes node 1 and node 2 , it can be replaced by two separate impedance $Z_{1}$ and $Z_{2}$; where $Z_{1}$ is connected between node - 1 and ground, and node $Z_{2}$ is connected between node -2 and ground.

The Vi and Vo are the voltages at the node -1 and node -2 respectively, The values of $\mathrm{Z}_{1}$ an $\mathrm{Z}_{2}$ can be derived from the ratio of Vo and Vi , denoted as K . Thus it is not necessary to know the values of Vi and Vo to calculate the values of $\mathrm{Z}_{1}$ and $\mathrm{Z}_{2}$

The values of impedance $Z_{1}$ and $Z_{2}$

$$
\mathrm{Z}_{1}=\mathrm{Z} /(1-\mathrm{K}) ; \quad \mathrm{Z}_{2}=\mathrm{Z} \mathrm{x} \mathrm{~K} /(\mathrm{K}-1)
$$

30. What do you mean by faithful amplification?

During the process of raising the strength of the input signal if the shape of the output voltage is exactly same as that of the input signal, the amplification is called faithful amplification.

## 31. Define the various $h$-parameters for a common emitter transistor.

From the h - parameter equivalent circuit of the common emitter configuration.

$$
\begin{aligned}
& \mathrm{V}_{\mathrm{be}}=\mathrm{h}_{\mathrm{ie}} \mathrm{I}_{\mathrm{b}}+\mathrm{h}_{\mathrm{re}} \mathrm{~V}_{\mathrm{ce}} \\
& \mathrm{I}_{\mathrm{c}}=\mathrm{h}_{\mathrm{fe}} \mathrm{I}_{\mathrm{b}}+\mathrm{h}_{\mathrm{oe}} \mathrm{~V}_{\mathrm{ce}} \\
& \text { Where, } \left.\mathrm{h}_{\mathrm{ie}}=\frac{\Delta \mathrm{VBE}}{\Delta \mathrm{IB}} \right\rvert\, \mathrm{V}_{\mathrm{CE}} \text { constant } \\
& \mathrm{h}_{\mathrm{re}}=\frac{\Delta \mathrm{VBE}}{\Delta \mathrm{VCE}} \mathrm{I}_{\mathrm{B}} \text { constant } \\
& \mathrm{h}_{\mathrm{fe}}=\frac{\left.\frac{\Delta \mathrm{IC}}{\Delta \mathrm{IP}} \right\rvert\, \mathrm{V}_{\mathrm{CE}} \text { constant }}{} \\
& \left.\mathrm{h}_{\mathrm{oe}}=\frac{\Delta \mathrm{IE}}{\Delta \mathrm{VC}} \right\rvert\, \mathrm{I}_{\mathrm{B}} \text { constant }
\end{aligned}
$$

32. State the advantages of using h-parameters fgganfyzingtransistor amplifiers.
i.) Real numbers at audio frequencies
ii.) Easy to measure
iii.) Can be obtained from the transistor static characteristics curves,
iv.) Convenient to use in circuit analysis and design,
v.) Most of the transistor manufacturers specify the h - parameters.

## 33. What is bandwidth of an amplifier.

The bandwidth of an amplifier is defined as the difference between the lower cut - off frequency and upper cut off frequency.

$$
\mathrm{BW}=\mathrm{f}_{2}-\mathrm{f}_{1}
$$

34. State the effect of coupling and bypass capacitors on the frequency response of amplifier.

Reactance of a capacitor is given by $X_{c}=1 / 2 \pi f \mathrm{f}$. At medium and high frequencies, the factor f makes $\mathrm{X}_{\mathrm{c}}$ very small, so that all coupling capacitors behave as short circuits. At low frequencies, $\mathrm{X}_{\mathrm{c}}$ increases. This increase in $X_{c}$ drops the signal voltage across the capacitor and reduces the circuit gain. As signal frequencies decrease, the capacitor reactance's increase and circuit gain continues to fall, reducing the output voltage.
35. State the effect of internal transistor capacitance on the frequency response of amplifier.

At high frequencies, the reactance of the junction capacitance are low. As frequency increases, the reactance of junction capacitances fall. When these reactance become small enough, they provide shunting effect as they are in parallel with junctions. This reduces the circuit gain and hence the output voltage.
36. Give the expression for $r_{0}$ of NMOS transistor.

$$
\begin{aligned}
& \mathrm{r}_{\mathrm{o}}=\left(\partial \mathrm{i}_{\mathrm{D}} / \partial \mathbf{v}_{\mathrm{DS}}\right)^{-1} \mid \mathrm{v}_{\mathrm{GS}}=\mathrm{V}_{\mathrm{GSQ}}=\text { const. } \\
& \mathrm{r}_{\mathrm{o}}=\left[\lambda \mathrm{K}\left[\left(\mathrm{v}_{\mathrm{GSQ}}-\mathrm{V}_{\mathrm{T}}\right)^{2}\right]^{-1} \approx\left[\lambda \mathrm{I}_{\mathrm{DQ}}\right]^{-1}\right.
\end{aligned}
$$

## 37. Draw the small signal equivalent circuit of CS JFET (Nov/Dec2015).



Small signal equivalent circuit of common-source circuit with NMOS transistor model


Expanded small signal equivalent
circuit, including output resistance,
for NMOS transistor

## 38. What is Gate capacitance in MOSFET.

Gate capacitance is a parallel - plate capacitance formed by a gate electrode with the channel, with the oxide layer acts as a capacitor dielectric. It is denoted as $\mathrm{C}_{\mathrm{ox}}$.
39. Draw the small signal equivalent circuit ofPARSS trâcistor.


Small signal equivalent circuit of common source amplifier with PMOS transistor model
40. Explain the loading effect.

The small signal overall voltage gain is,
$\mathbf{G}_{\mathrm{v}}=\mathbf{v}_{\mathrm{o}} / \mathbf{v}_{\mathrm{s}}=-\mathbf{g m}_{\mathrm{m}}\left(\mathbf{r}_{\mathbf{o}} \| \mathbf{R}_{\mathrm{D}}\right)\left(\mathbf{R}_{\mathrm{i}} / \mathbf{R}_{\mathbf{i}}+\mathbf{R}_{\mathrm{si}}\right)=\mathbf{A}_{\mathrm{v}}\left(\mathbf{R}_{\mathrm{i}} / \mathbf{R}_{\mathrm{i}}+\mathbf{R}_{\mathrm{si}}\right)$
Since Rsi is not zero, the amplifier input signal $v_{i}$ is less than the signal voltage, This is known as loading effect.
It reduces the voltage gain of the amplifier.
41. What do you mean by drain diffusion and source diffusion capacitance?

Drain and Source capacitances are due to the reverse - biased pn junctions formed by the $\mathrm{n}^{+}$source region and the p - type substrate, and the $\mathrm{n}^{+}$drain region and the p - type substrate. These are denoted as source diffusion capacitance and drain diffusion capacitance respectively.
42. Give the expression of unity gain frequency ( $f_{T}$ )for MOSFET amplifier?

Unity gain frequency for MOSFET:
$\mathrm{f}_{\mathrm{T}}=\mathrm{g}_{\mathrm{m}} / 2 \pi\left(\mathrm{C}_{\mathrm{gs}}+\mathrm{C}_{\mathrm{gd}}\right)$
From the above expression we can say that $\mathrm{f}_{\mathrm{T}}$ is proportional to gm and inversely proportional to the internal capacitances.
43. Compare different amplifiers.

| COMMON SOURCE AMPLIFIER | Good voltage amplifier and better trans conductance amplifier | - Large Voltage gain <br> - High input resistance <br> - High output resistance |
| :---: | :---: | :---: |
| COMMON DRAIN AMPLIFIER | Good voltage buffer | - Voltage gain $\approx 1$ <br> - High input resistance <br> - Low input resistance |
| COMMON GATE AMPLIFIERS | Good current buffer | - Current Gain $\approx 1$ <br> - Low input resistance <br> - High output resistance |

44. What is the need of coupling capacitors in amplifier design? (Aril/May 2019) (Nov / Dec 2015) Coupling capacitors isolates the DC condition of one stage from the following stages. It is used to couple output of one stage to another stage.
45. Differentiate between power transistor and signal transistor. (May / Jun 2016)

| S.No | Power transistor | Small signal transistor |
| :---: | :--- | :--- |
| 1 | $\mathrm{n}^{-1}$ drift layer is present | $110 \mathrm{n}^{-1}$ drift layer |
| 2 | Secondary breakdown occurs | No secondary breakdown |
| 3 | Used in power circuits | Used in amplifying circuits |

## EnggTreRterm

## BJT Small signal Model-Analysis of CE, CB, CC amplifiers

1. Draw the small signal model of BJT device (OR) Draw the parameters equivalent circuit or small signal model of a transistor in CE, CB, CC configuration? (Apr/May 2018). (OR)
Draw the hybrid model of BJT in CE, CC and CB configuration.

## h - Parameter model for CE, CC and CB configuration

The variable $\mathrm{I}_{\mathrm{b}}, \mathrm{I}_{\mathrm{c}}, \mathrm{V}_{\mathrm{b}}$, and $\mathrm{V}_{\mathrm{c}}$ represent total instantaneous current and voltage.
Ib - Input current; $\mathrm{I}_{\mathrm{c}}$ - Output current; $\mathrm{V}_{\mathrm{be}}$ - Input voltage; $\mathrm{V}_{\mathrm{ce}}$ - Output voltage
CE Configuration

$\underline{\text { h- Parameter equivalent circuit }}$


$$
\begin{align*}
& \mathrm{V}_{\mathrm{be}}=\mathrm{h}_{\mathrm{ie}} \mathrm{I}_{\mathrm{b}}+\mathrm{h}_{\mathrm{re}} \mathrm{~V}_{\mathrm{ce}}  \tag{1}\\
& \mathrm{I}_{\mathrm{c}}=\mathrm{h}_{\mathrm{fe}} \mathrm{I}_{\mathrm{b}}+\mathrm{h}_{\mathrm{oe}} \mathrm{~V}_{\mathrm{ce}}  \tag{2}\\
& \text { Where, } \quad h_{\text {ie }}=\left.\frac{\Delta V_{B E}}{\Delta I_{B}}\right|_{C E} \text { - constant }  \tag{3}\\
& h_{\text {re }}=\left.\frac{\Delta V_{B E}}{\Delta V_{\text {CE }}}\right|_{\text {B }}-\text { constant }----  \tag{4}\\
& h_{f e}=\left.\frac{\Delta \mathrm{I}_{\mathrm{C}}}{\Delta \mathrm{I}_{\mathrm{B}}}\right|_{\mathrm{CE}} \text { - constant ----(5) } \\
& \mathrm{h}_{\mathrm{oe}}=\left.\frac{\Delta \mathrm{I}_{\mathrm{c}}}{\Delta V_{\mathrm{C}}}\right|_{\mathrm{I}}-\text { constant }----(6) \\
& h_{\text {ie }} \text { - Input resistance; }
\end{align*}
$$



Relationship between h-parameters of different transistor configuration:

CE to CB conversion formulae
$h_{\mathrm{ib}}=\frac{h_{\mathrm{le}}}{1+h_{\mathrm{fe}}}$

$h_{\text {fo }}=\frac{1}{1+h_{\text {e }}}$
$h_{\mathrm{ob}}=\frac{h_{\mathrm{oc}}}{1+h_{\mathrm{fe}}}$

CE to CC conversion formulae
$h_{i c}=h_{i c} *$

$$
h_{\mathrm{rc}}=1-h_{\mathrm{re}} \approx 1 *
$$

$$
h_{\mathrm{fc}}=-\left(1+h_{\mathrm{fe}}\right) *
$$

$$
h_{\mathrm{oc}}=h_{\mathrm{oe}} *
$$

 output resistance ( $\mathrm{R}_{0}$ ) for CE amplifier using h - parameter model. (April/May 2015 \& 18 ) (Nov/Dec' 2014\& 16)
Illustrate the steps involved in analyzing a BJT amplifier circuit using small signal model. (April/May 2019) (5 Marks)

## Circuit diagram


(a) CE amplifier
$\underline{\mathrm{h} \text { - Parameter model }}$

(b) CE amplifier in its h-parameter model

Current gain $\left[A_{I}\right] A_{I}=\frac{\mathrm{I}_{\mathrm{L}}}{\mathrm{I}_{\mathrm{b}}}$

$$
\begin{aligned}
& \mathrm{IC}_{\mathrm{C}}=\mathrm{h}_{\mathrm{fe}} \mathrm{I}_{\mathrm{b}}+\mathrm{h}_{\mathrm{oe}} \mathrm{~V}_{\mathrm{C}} ; \mathrm{I}_{\mathrm{C}}=\mathrm{h}_{\mathrm{fe}} \mathrm{I}_{\mathrm{b}}+\mathrm{h}_{\mathrm{oe}}\left(-\mathrm{I}_{\mathrm{c}} \mathrm{R}_{\mathrm{L}}\right) ; \quad\left\{\text { since }, \mathrm{V}_{\mathrm{c}}=-\mathrm{I}_{\mathrm{C}} \mathrm{R}_{\mathrm{L}}\right\} \\
& \mathrm{I}_{\mathrm{C}}+\mathrm{h}_{\mathrm{oe}} \mathrm{R}_{\mathrm{L}} \mathrm{I}_{\mathrm{c}}=\mathrm{h}_{\mathrm{fe}} \mathrm{I}_{\mathrm{b}} ; \mathrm{Ic}_{\mathrm{c}}\left(1+\mathrm{h}_{\mathrm{oe}} \mathrm{R}_{\mathrm{L}}\right)=\mathrm{h}_{\mathrm{fe}} \mathrm{I}_{\mathrm{b}} \\
& \frac{\mathrm{I}_{\mathrm{C}}}{\mathrm{I}_{\mathrm{b}}}=\frac{\mathrm{h}_{\mathrm{fe}}}{1+\mathrm{h}_{\text {oe }} \mathrm{RL}_{\mathrm{L}}} \\
& \mathrm{~A}_{\mathrm{I}}=\frac{-\mathrm{I}_{\mathrm{C}}}{\mathrm{I}_{\mathrm{b}}}=-\frac{\mathrm{h}_{\mathrm{fe}}}{1+\mathrm{h}_{\mathrm{oe}} \mathrm{R}_{\mathrm{L}}} \\
& \text { Input Resistance }\left(R_{i}\right) R_{i}=\frac{V_{b}}{I_{b}} \\
& \mathrm{~V}_{\mathrm{b}}=\mathrm{h}_{\mathrm{ie}} \mathrm{I}_{\mathrm{b}}+\mathrm{h}_{\mathrm{re}} \mathrm{~V}_{\mathrm{C}} \\
& \mathrm{~V}_{\mathrm{C}}=-\mathrm{I}_{\mathrm{C}} \mathrm{R}_{\mathrm{L}} ; \mathrm{V}_{\mathrm{C}}=\mathrm{A}_{\mathrm{I}} \mathrm{I}_{\mathrm{b}} \mathrm{R}_{\mathrm{L}}
\end{aligned}
$$


Substituting, $A_{I}=\frac{-h_{F e}}{1+h_{o e} R_{L}} \quad$ to the above equation
$R_{i}=h_{i e}+h_{r e}\left(\frac{-h_{f e}}{1+h_{o e} R_{L}}\right) \times R_{L}$
$R_{i}=h_{i e}-\frac{h_{r e} h_{f e} R_{L}}{1+h_{o e} R_{L}}$
Voltage gain (A ) $A_{V}=\frac{V_{c}}{V_{b}}=\frac{A_{I} I_{b} \underline{R_{L}}}{V_{b}} \therefore \therefore \frac{I_{b}}{V_{b}}=\frac{1}{R_{i}}$

$$
A_{v}=\frac{A_{I} R_{L}}{R_{i}}
$$

Output admittance $(\underset{\mathbf{o}}{(\mathbf{Y}}) \mathrm{Y}_{\mathrm{o}}=\frac{\mathrm{I}_{\mathrm{c}}}{\mathrm{V}_{\mathrm{c}}}$ with $\mathrm{V}_{\mathrm{s}}=0$

$$
\begin{aligned}
& \mathrm{I}_{\mathrm{c}}=\mathrm{h}_{\mathrm{fe}} \mathrm{I}_{\mathrm{b}}+\mathrm{h}_{\mathrm{oe}} \mathrm{~V}_{\mathrm{c}} \\
& \mathrm{I}_{\mathrm{c}} \\
& \frac{h_{\mathrm{fe}} \mathrm{I}_{\mathrm{b}}+\mathrm{h}_{\mathrm{oe}} \mathrm{~V}_{\mathrm{c}}}{\mathrm{~V}_{\mathrm{c}}} \\
& \mathrm{~V}_{\mathrm{c}} \\
& \mathrm{Y}_{\mathrm{o}}=\frac{\mathrm{h}_{\mathrm{fe}} \mathrm{I}_{\mathrm{b}}}{\mathrm{~V}_{\mathrm{c}}}+\mathrm{h}_{\mathrm{oe}}
\end{aligned}
$$

From h parameter circuit with $\mathbf{V}_{\mathbf{s}}=\mathbf{0}$

$$
\begin{aligned}
& \mathrm{R}_{\mathrm{s}} \mathrm{I} \mathrm{~b}+\mathrm{h}_{\mathrm{ie}} \mathrm{I}_{\mathrm{b}}+\mathrm{h}_{\mathrm{re}} \mathrm{~V}_{\mathrm{c}}= \\
& \left(\mathrm{R}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ie}}\right) \mathrm{I}_{\mathrm{b}}=-\mathrm{h}_{\mathrm{re}} \mathrm{~V}_{\mathrm{c}} \\
& \frac{\mathrm{I}_{\mathrm{b}}}{\mathrm{~V}_{\mathrm{c}}}=\frac{-\mathrm{h}_{\mathrm{re}}}{\mathrm{R}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ie}}}
\end{aligned}
$$

(Apply KVL)

Substitute, $\quad \frac{\mathrm{Ib}}{\mathrm{V}_{\mathrm{c}}}=\frac{-\mathrm{h}_{\mathrm{re}}}{\mathrm{R}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ie}}} \quad$ in $\mathrm{Y}_{\mathrm{o}}=\frac{\mathrm{h}_{\text {Fe }} \mathrm{I}_{\mathrm{b}}}{\mathrm{V}_{\mathrm{c}}}+\mathrm{h}_{\mathrm{oe}}$

$$
\begin{aligned}
& Y_{\mathrm{o}}=\frac{\mathrm{I}_{\mathrm{c}}}{\mathrm{~V}_{\mathrm{c}}}=\mathrm{h}_{\mathrm{fe}}\left(\frac{-\mathrm{h}_{\mathrm{re}}}{\mathrm{R}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ie}}}\right)+\mathrm{h}_{\mathrm{oe}} \\
& Y_{\mathrm{o}}=\mathrm{h}_{\mathrm{oe}}-\frac{\mathrm{h}_{\mathrm{Fe}} \mathrm{~h}_{\mathrm{re}}}{\mathrm{R}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ie}}} \quad \text { and } \quad \mathrm{R}_{\mathrm{o}}=\frac{1}{Y_{\mathrm{o}}}
\end{aligned}
$$

(B) Draw the circuit of CE amplifier with amplifier operation. (April/May 2019) (8 Marks) (OR) Approximate analysis of CE amplifier using simplified Hybrid Model.

Analysis of CE Amplifier using simplified Hybrid Model:


Fig. Simplified CE model


Fig. Approximate CE model
Current gain $\left[\mathrm{A}_{\mathrm{I}}\right] \mathrm{A}_{\mathrm{I}}=\frac{\mathrm{L}_{\mathrm{L}}}{\mathrm{I}_{\mathrm{b}}}$

$$
\mathrm{A}_{\mathrm{I}}=\frac{-\mathrm{IC}}{\mathrm{I}_{\mathrm{b}}}=-\mathrm{h}_{\mathrm{fe}}
$$

Input Resistance $\left(R_{i}\right) R_{i}=\frac{\mathrm{V}_{\mathrm{b}}}{\mathrm{I}_{\mathrm{b}}}$

$$
\mathrm{R}_{\mathrm{i}}=\mathrm{h}_{\mathrm{ie}}
$$

Voltage gain (A) $A_{V} A_{V}=\frac{V_{c}}{V_{b}}=\frac{A_{I} \underline{L_{b}} \underline{R_{L}}}{V_{b}} \therefore \cdot \frac{\mathrm{I}_{b}}{V_{b}}=\frac{1}{R_{i}}$

$$
A_{v}=\frac{A_{I} R_{L}}{R_{i}}
$$

Output admittance $\left(\mathbf{Y}_{0}\right) \mathrm{Y}_{0}=0$

$$
\mathrm{R}_{\mathrm{o}}=1 / \mathrm{Y}=\infty
$$

3. (A) Derive the expressions for currengigin, 居ffane gain, input impedance and output impedance for an Emitter Follower (common collector) circuit.
Circuit diagram

(a) CC amplifier
$\underline{\mathrm{h} \text { parameter equivalent circuit }}$

(b) CC amplifier In its h-parameter model

Current gain (A) $A_{\mathrm{I}}=\frac{\mathrm{LL}}{\mathrm{I}_{\mathrm{b}}}=\frac{-\mathrm{I}}{\mathrm{e}} \mathrm{I}_{\mathrm{b}}$
Apply KCL
$\mathrm{I}_{\mathrm{e}}=\mathrm{h}_{\mathrm{fc}} \mathrm{I}_{\mathrm{b}}+\mathrm{h}_{\mathrm{oc}} \mathrm{V}_{\mathrm{e}} \quad=\mathrm{h}_{\mathrm{fc}} \mathrm{I}_{\mathrm{b}}+\mathrm{h}_{\mathrm{oc}}\left(-\mathrm{I}_{\mathrm{e}} \mathrm{R}_{\mathrm{L}}\right) \quad\left(\right.$ since, $\left.\mathrm{V}_{\mathrm{e}}=-\mathrm{I}_{\mathrm{e}} \mathrm{R}_{\mathrm{L}}\right)$

$\mathrm{A}_{\mathrm{i}}=\frac{\mathrm{I}_{\mathrm{e}}}{\mathrm{I}_{\mathrm{b}}}=\frac{-\mathrm{I}_{\mathrm{L}}}{\mathrm{I}_{\mathrm{b}}}=\frac{-\mathrm{h}_{\mathrm{fc}}}{1+\mathrm{h}_{\mathrm{oc}} \mathrm{R}_{\mathrm{L}}}$
Input Resistance $\left(\mathbf{R}_{\mathbf{i}}\right) \mathrm{R}_{\mathrm{i}}=\frac{\mathrm{V}_{\mathrm{b}}}{\mathrm{I}_{\mathrm{b}}}$
Apply KVL
$\mathrm{V}_{\mathrm{b}}=\mathrm{h}_{\mathrm{ic}} \mathrm{I}_{\mathrm{b}}+\mathrm{h}_{\mathrm{rc}} \mathrm{V}_{\mathrm{e}}\left(\mathrm{V}_{\mathrm{e}}=-\mathrm{I}_{\mathrm{e}} \mathrm{R}_{\mathrm{L}}\right)$
$\mathrm{V}_{\mathrm{e}}=\mathrm{A}_{\mathrm{I}} \mathrm{Ib}_{\mathrm{L}}$

$$
\left\{\mathrm{A}_{\mathrm{I}}=\frac{-\mathrm{I}_{\mathrm{e}}}{\mathrm{I}_{\mathrm{b}}}\right\}
$$

Now

$$
\begin{aligned}
& R_{i}=h_{i c}+h_{r e} A_{I} R_{L} \\
& \mathrm{R}_{\mathrm{i}}=\mathrm{h}_{\mathrm{ic}}-\mathrm{h}_{\mathrm{rc}}\left(\underset{1+\mathrm{h}_{o c} \mathrm{R}_{\mathrm{L}}}{\mathrm{~h}_{\underline{E c}} \mathrm{R}}\right) \\
& \left\{A_{I}=\frac{-h_{F c}}{1+h_{o c} R_{L}}\right\}
\end{aligned}
$$

Voltage gain ( $A_{v}$ ) $A_{v}=\frac{\underline{V}_{e}}{V_{b}}$


$$
\begin{aligned}
& A_{V}=\frac{A_{I} I_{-} R_{\underline{L}}}{V_{b}} \leftrightharpoons \frac{A_{I} I_{b} R_{L}}{I_{b} R_{i}} \\
& \left\{\because \frac{\mathrm{I}_{\mathrm{b}}}{\mathrm{~V}_{\mathrm{b}}}=\frac{1}{\mathrm{R}_{\mathrm{i}}}\right\} \\
& A v=\frac{\mathrm{A}_{\mathrm{I}} \mathrm{R}_{\mathrm{L}}}{\mathrm{R}_{i}}
\end{aligned}
$$

Output admittance $(\underset{\mathbf{0}}{(\mathbf{Y}}) \mathrm{Y}_{0}=\frac{\mathrm{I}_{2}}{\mathrm{~V}_{2}}$ with $\mathrm{V}_{\mathrm{s}}=0$
$Y_{O}=\frac{\mathrm{I} \mathrm{e}}{\mathrm{V}_{\mathrm{e}}}$ with $\mathrm{V}_{\mathrm{s}}=0$
$\mathrm{I}_{\mathrm{e}}=\mathrm{h}_{\mathrm{fc}} \mathrm{I}_{\mathrm{b}}+\mathrm{h}_{\mathrm{oc}} \mathrm{V}_{\mathrm{e}}$
Dividing the above equation by $V_{e}, \quad \frac{I_{e}}{V_{e}}=\frac{h_{f c} I_{b}}{V_{e}}+h_{o c}$
From circuit $V_{s}=0$
Apply KVL
$\mathrm{Rs}_{\mathrm{s}} \mathrm{I}_{\mathrm{b}}+\mathrm{h}_{\mathrm{ic}} \mathrm{I}_{\mathrm{b}}+\mathrm{h}_{\mathrm{rc}} \mathrm{V}_{\mathrm{e}}=0$
$\left(\mathrm{Rs}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ic}}\right) \mathrm{I}_{\mathrm{b}}=-\mathrm{h}_{\mathrm{rc}} \mathrm{V}_{\mathrm{e}}$
$\frac{\mathrm{I}_{\mathrm{b}}}{\mathrm{V}_{\mathrm{e}}}=\frac{-\mathrm{h}_{\mathrm{rc}}}{\mathrm{R}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ic}}}--$
Sub equation (2) in (1)
$\frac{\underline{\mathrm{I}_{\mathrm{e}}}}{\mathrm{V}_{\mathrm{e}}}=\mathrm{h}_{\mathrm{fc}}\left(\frac{-\mathrm{h}_{\mathrm{rc}}}{\mathrm{R}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ic}}}\right)+\mathrm{h}_{\mathrm{oc}}$
$\mathrm{y}_{\mathrm{o}}=\frac{\mathrm{I}_{\mathrm{e}}}{\mathrm{V}_{\mathrm{e}}}=\mathrm{h}_{\mathrm{oc}}-\frac{\mathrm{h}_{\mathrm{fc}} \mathrm{h}_{\mathrm{rc}}}{\mathrm{R}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ic}}}$ and $\mathrm{R}_{\mathrm{o}}=\frac{1}{\mathrm{y}_{\mathrm{o}}}$
(B) Draw the circuit of CC amplifier with DC sources eliminated and deduce the small signal model for amplifier operation. (April/May 2019) (8 Marks) (OR) Approximate analysis of CC amplifier using simplified Hybrid Model.

In simplified CE model, the input is applied to base and output is taken from collector, and emitter is common between input and output. The same simplified model can be modified to get simplified CC model.
For simplified CC model, make collector common and take output from emitter.


The $\mathrm{h}_{\mathrm{fb}} \mathrm{I}_{\mathrm{b}}$ current direction is now exactly ofnggitree thatome model because the current $\mathrm{h}_{\mathrm{fc}} \mathrm{I}_{\mathrm{b}}$ always points towards emitter.
Current gain (A) $A_{I}=\frac{\underline{L}}{\underline{L_{b}}}=\frac{-I_{e}}{I_{b}}$

$$
\mathrm{A}_{\mathrm{i}}=1+\mathrm{h}_{\mathrm{fe}}
$$

Input Resistance $\left(\mathbf{R}_{\mathbf{i}}\right) \mathrm{R}_{\mathrm{i}}=\frac{\mathrm{V}_{\mathrm{b}}}{\mathrm{I}_{\mathrm{b}}}$

## Apply KVL

$$
\begin{gathered}
\mathrm{V}_{\mathrm{b}}=\mathrm{h}_{\mathrm{ie}} \mathrm{I}_{\mathrm{b}}+\mathrm{Io}_{\mathrm{L}} ; \quad \text { (divide both sides by } \mathrm{Ib} \text { ) } \\
\left\{\mathrm{A}_{\mathrm{I}}=\frac{-\mathrm{I}_{\mathrm{e}}}{\mathrm{I}_{\mathrm{b}}}=\frac{-\mathrm{I}_{o}}{\mathrm{I}_{\mathrm{b}}}\right\}
\end{gathered}
$$

Now

$$
\mathrm{R}_{\mathrm{i}}=\frac{\mathrm{V}_{\mathrm{b}}}{\mathrm{I}_{\mathrm{b}}}=\mathrm{h}_{\mathrm{ie}}+\left(1+\mathrm{I}_{\mathrm{o}}^{\mathrm{h}} \mathrm{fe}_{\mathrm{Le}}\right) \mathrm{R}_{\mathrm{L}}
$$

Voltage gain $\left(A_{V}\right) A_{V}=\frac{\underline{V}_{e}}{V_{b}}$

$$
\begin{array}{ll}
A_{V}=\frac{A_{I}-\underline{L} \underline{L_{L}} \underline{R_{\mathrm{L}}}}{\mathrm{~V}_{\mathrm{b}}} \Rightarrow \frac{\mathrm{~A}_{\underline{I}-\underline{L_{b}} \underline{R_{\mathrm{L}}}}^{I_{\mathrm{b}} R_{i}}}{\mathrm{R}_{i}} & \left\{\because \frac{\mathrm{I}_{\mathrm{b}}}{\mathrm{~V}_{\mathrm{b}}}=\frac{1}{\mathrm{R}_{\mathrm{i}}}\right\} \\
\mathrm{Av}=\frac{\mathrm{A}_{\mathrm{I}} \mathrm{R}_{\mathrm{L}}}{}
\end{array}
$$


Output admittance $\left(\underset{\mathbf{0}}{\left(\mathbf{Y}_{\mathbf{0}}\right)} \mathrm{Y}_{0}=\frac{\mathrm{I}_{2}}{\mathrm{~V}_{2}}\right.$ with $\mathrm{V}_{\mathrm{s}}=0$
$Y_{o}=\frac{\mathrm{I}_{\mathrm{e}}}{\mathrm{V}_{\mathrm{e}}}$ with $\mathrm{V}_{\mathrm{s}}=0$
$\mathrm{I}_{\mathrm{e}}=\mathrm{h}_{\mathrm{fc}} \mathrm{I}_{\mathrm{b}}+\mathrm{h}_{\mathrm{oc}} \mathrm{V}_{\mathrm{e}}$
Dividing the above equation by $V_{e}, \quad \frac{I_{e}}{V_{e}}=\frac{h_{f c} I_{b}}{V_{e}}+h_{o c}$
From circuit $V_{s}=0$
Apply KVL
$\mathrm{RS}_{\mathrm{S}} \mathrm{I}_{\mathrm{b}}+\mathrm{h}_{\text {ic }} \mathrm{I}_{\mathrm{b}}+\mathrm{h}_{\mathrm{rc}} \mathrm{V}_{\mathrm{e}}=0$
$\left(R_{s}+h_{i c}\right) I_{b}=-h_{r c} V_{e}$
$\frac{\mathrm{I}_{\mathrm{b}}}{\mathrm{V}_{\mathrm{e}}}=\frac{-\mathrm{h}_{\mathrm{rc}}}{\mathrm{R}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ic}}}--$
Sub equation (2) in (1)
$\frac{\underline{\mathrm{I}}}{\mathrm{V}_{\mathrm{e}}}=\mathrm{h}_{\mathrm{fc}}\left(\frac{-\mathrm{h}_{\mathrm{rc}}}{\mathrm{R}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ic}}}\right)+\mathrm{h}_{\mathrm{oc}}$
$\mathrm{y}_{\mathrm{o}}=\frac{\mathrm{I}_{\mathrm{e}}}{\mathrm{V}_{\mathrm{e}}}=\mathrm{h}_{\mathrm{oc}}-\frac{\mathrm{h}_{\mathrm{fc}} \mathrm{h}_{\mathrm{rc}}}{\mathrm{R}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ic}}}$ and $\mathrm{R}_{\mathrm{o}}=\frac{1}{\mathrm{y}_{\mathrm{o}}}$
 2016)

Circuit diagram

(a) CB amplifier
h parameter model

(b) h-parameter equivalent circuit for CB amplifier

Current gain (A) $\underset{\mathrm{I}}{\mathrm{A}} \mathrm{A}_{\mathrm{I}}=\frac{\mathrm{LL}}{\mathrm{I}_{\mathrm{e}}}=\frac{-\mathrm{I}_{\mathbf{c}}}{\mathrm{I}_{\mathrm{e}}}$

$$
\begin{aligned}
& \mathrm{I}_{\mathrm{c}}=\mathrm{h}_{\mathrm{fb}} \mathrm{I}_{\mathrm{e}}+\mathrm{h}_{\mathrm{ob}} \mathrm{~V}_{\mathrm{c}} \\
& \mathrm{~h}_{\mathrm{fb}} \mathrm{I}_{\mathrm{e}}+\mathrm{h}_{\mathrm{ob}}\left(-\mathrm{I}_{\mathrm{c}} \mathrm{R}_{\mathrm{L}}\right) \quad \therefore \mathrm{V}_{\mathrm{c}}=-\mathrm{I}_{\mathrm{c}} \mathrm{R}_{\mathrm{L}} \\
& \mathrm{I}_{\mathrm{c}}+\mathrm{h}_{\mathrm{ob}} \mathrm{I}_{\mathrm{c}} \mathrm{R}_{\mathrm{L}}=\mathrm{h}_{\mathrm{fb}} \mathrm{I}_{\mathrm{e}} \\
& \left(1+\mathrm{h}_{\mathrm{ob}} \mathrm{R}_{\mathrm{L}}\right) \mathrm{I}_{\mathrm{c}}=\mathrm{h}_{\mathrm{fb}} \mathrm{I}_{\mathrm{e}}
\end{aligned}
$$

Input Resistance $R_{i} R_{i}=\frac{V_{e}}{I_{e}}$
$\mathrm{V}_{\mathrm{e}}=\mathrm{h}_{\mathrm{ib}} \mathrm{I}_{\mathrm{e}}+\mathrm{h}_{\mathrm{rb}} \mathrm{V}_{\mathrm{c}}$
$\mathrm{V}_{\mathrm{c}}=-\mathrm{R}_{\mathrm{L}} \mathrm{I}_{\mathrm{c}}$

$$
=\mathrm{A}_{\mathrm{I}} \mathrm{IeR}_{\mathrm{L}}
$$

$\mathrm{R}_{\mathrm{i}}=\frac{\mathrm{V}_{\mathrm{e}}}{\mathrm{I}_{\mathrm{e}}}=\frac{\mathrm{h}_{\mathrm{ib}} \mathrm{I}_{\mathrm{e}}+\mathrm{h}_{\mathrm{rb}} \mathrm{A}_{\mathrm{I}} \mathrm{I}_{\mathrm{e}} \mathrm{R}_{\mathrm{L}}}{\mathrm{Ie}}$
$\mathrm{R}_{\mathrm{i}}=\mathrm{h}_{\mathrm{ib}}+\mathrm{h}_{\mathrm{rb}} \mathrm{A}_{\mathrm{I}} \mathrm{R}_{\mathrm{L}}$
Voltage gain (A $\underset{\mathbf{V}}{\left.()_{V}\right)} A_{V_{e}}^{\underline{V}_{\mathbf{c}}}=\frac{A_{I} \underline{I} e^{R_{L}}}{V_{e}}$

$$
=\frac{\mathrm{A}_{\mathrm{I}} \mathrm{R}_{\mathrm{L}}}{\mathrm{R}_{\mathrm{c}}} \quad \left\lvert\, \frac{\mathrm{I}_{\mathrm{e}}}{\mathrm{~V}_{\mathrm{e}}}=\frac{1 \text { EnggTree.com }}{\mathrm{R}_{\mathrm{i}}}\right.
$$

Output admittance $\left(\mathbf{Y}_{\mathbf{0}}\right) \mathrm{Y}_{0}=\frac{\mathrm{I}_{\mathrm{c}}}{\mathrm{V}_{\mathrm{c}}}$ with $\mathrm{V}_{\mathrm{s}}=0$

$$
\begin{aligned}
& \mathrm{I}_{\mathrm{c}}=\mathrm{h}_{\mathrm{fb}} \mathrm{I}_{\mathrm{e}}+\mathrm{h}_{\mathrm{ob}} \mathrm{~V}_{\mathrm{c}} \\
& \div \mathrm{V}_{\mathrm{c}} \quad \frac{\mathrm{I}_{\mathrm{c}}}{\mathrm{~V}_{\mathrm{c}}}=\frac{\mathrm{h}_{\mathrm{fb}} \mathrm{I}_{\mathrm{e}}}{\mathrm{~V}_{\mathrm{c}}}+\mathrm{h}_{\mathrm{ob}}---(1) \\
& \text { When } V_{s}=0 \\
& R_{s} I_{e}+h_{\text {ib }} I_{e}+h_{r b} V_{c}=0 \\
& \left(R_{s}+h_{i b}\right) I_{e}=-h_{r b} V_{c} \\
& \frac{\mathrm{I}_{\mathrm{e}}}{\mathrm{~V}_{\mathrm{c}}}=-\frac{\mathrm{h}_{\mathrm{rb}}}{\mathrm{R}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ib}}}
\end{aligned}
$$

Sub (2) in (1)

$$
\begin{aligned}
& \underline{I_{c}}=h_{f b}\left(\frac{-h_{r b}}{R_{s}+h_{i b}}\right)+h_{o b} \\
& V_{c}=\frac{I_{c}}{V_{c}}=h_{\mathrm{ob}}-\frac{h_{\mathrm{fb}} \cdot h_{\mathrm{rb}}}{R_{\mathrm{s}}+h_{\mathrm{ib}}} \\
& \mathrm{R}_{\mathrm{o}}=\frac{1}{\mathrm{y}_{0}}
\end{aligned}
$$

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5. Explain the frequency response operation of BJT amplifier with suitable circuit diagram.

From the fig 9.1, the capacitors $\mathrm{C}_{\mathrm{s}}, \mathrm{C}_{\mathrm{C}}$ and $\mathrm{C}_{\mathrm{E}}$ will determine the low-frequency response.
$\mathrm{C}_{\mathrm{s}}$ is normally connected between the applied source and active device. In fig 9.2The total resistance is now $\mathrm{R}_{\mathrm{S}}$ $+\mathrm{R}_{\mathrm{i}}$, the cutoff frequency is established as

$$
\mathrm{f}_{\mathrm{LS}}=\frac{1}{2 M\left(R_{\mathrm{C}}+R_{i}\right) C_{\varsigma}}
$$



Fig Loaded BJT amplifier with capacitors that affect the low- frequency response


Fig Determining the effect of $\mathrm{C}_{\mathrm{s}}$ on the low frequency response
At mid or high frequency, the reactance of the capacitor will be small to permit short circuit approximation for the element. the voltage $\mathrm{V}_{\mathrm{i}}$ related to $\mathrm{V}_{\mathrm{S}}$ by

$$
\left.\mathrm{V}_{\mathrm{i}}\right|_{\text {mid }}=\frac{R_{i} V_{S}}{R_{i}+R_{S}}
$$

The value of $\mathrm{R}_{\mathrm{i}}$ is determined by $\mathrm{R}_{\mathrm{i}}=\mathrm{R}_{1}\left\|\mathrm{R}_{2}\right\| \beta \mathrm{r}_{\mathrm{e}}$


Fig Localized ac equivalent for $\mathrm{C}_{\mathrm{s}}$

The voltage $\mathrm{V}_{\mathrm{i}}$ applied to the input of the active device can be calculated using the voltage divider rule: $\quad \mathrm{V}_{\mathrm{i}}$
$=\frac{R_{i} V_{S}}{R_{S}+R_{i}-j X_{C s}}$
Since the coupling capacitor is normally connected
between the output of the active device and the applied load, the R-C configuration that determines the low cutoff frequency due to $\mathrm{C}_{\mathrm{C}}$.
From fig 9.4 the total series resistance is now $\mathrm{R}_{0}+\mathrm{R}_{\mathrm{L}}$ and the cutoff frequency is determined by,

$$
\mathrm{f}_{\mathrm{LC}}=\frac{1}{2 M\left(R_{0+\underline{R}}\right) C_{C}}
$$

The resulting value for $\mathrm{R}_{0}, \mathrm{R}_{0}=\mathrm{R}_{\mathrm{C}} \| \mathrm{r}_{0}$ To determine $f_{\text {LE, }} \mathrm{C}_{\mathrm{E}}$ must be determined from

$$
\mathrm{f}_{\mathrm{LE}}=\frac{1}{2 M R_{e C_{E}}}
$$



Fig determining the effect of $\mathrm{C}_{\mathrm{c}}$ on the low freq

Fig Localized ac equivalent for $\mathrm{C}_{\mathrm{c}}$ with $\mathrm{V}_{\mathrm{i}}=\mathbf{0} \mathrm{V}$
The value of $\mathrm{R}_{\mathrm{e}}$ is determined by $\mathrm{R}_{\mathrm{e}}=\mathrm{R}_{\mathrm{E}} \|\left(\frac{R S^{\prime}}{\beta}+r \underset{e}{ }\right)$. where $\mathrm{R}_{\mathrm{s}^{\prime}}=\mathrm{R}_{\mathrm{S}}\left\|\mathrm{R}_{1}\right\| \mathrm{R}_{2}$


Fig .9.6 Localized ac equivalent of $C_{E}$

The effect of $\mathrm{C}_{\mathrm{E}}$ on the gain is given by,

$$
A_{V}=-R_{C} / r_{e}+R_{E}
$$

The maximum gain is available where $R_{E}$ is $0 \Omega$. At low frequency with bypass capacitor $\mathrm{C}_{\mathrm{E}}$ in open circuit.

As the frequency increases, the reactance of the capacitor $\mathrm{C}_{\mathrm{E}}$ will decrease, reducing the parallel impedance of $\mathrm{R}_{\mathrm{E}}$ and $C_{E}$ until $R_{E}$ shorted out by $C_{E}$.

At the midband frequency level, the Short circuit equivalents for the capacitors can be inserted. The highest low frequency cutoff determined by $\mathrm{C}_{\mathrm{S}}, \mathrm{C}_{\mathrm{C}}$ or $\mathrm{C}_{\mathrm{E}}$.
If there are two or more high cutoff frequencies, the effect will be to raise the lower cutoff frequency and reduce the resulting bandwidth of the system. there is an interaction between the capacitive elements that can affect the resulting low cutoff frequency.

## 6. Discuss the factors involved in the selection of $\mathrm{I}_{\mathrm{c}}, \mathrm{R}_{\mathrm{c}}$ and $\mathrm{RE}^{2}$ for a single stage common emitter BJT amplifier circuit, using voltage divider bias (Nov/Dec2015)

It is also called potential divider bias or self-bias.
In all D.C bias discussed in the above sections clearly states that the values of D.C bias currents and voltage of collector depends on the currents gain $\beta\left(\beta=\frac{I C}{I B}\right)$. But we know it is purely a temperature sensitive one particularly in silicon type. Hence the nominal value of $\beta$ is not well defined.
So it is not desirable to provide a D.C bias circuit which is independent of the transistor current gain $(\beta)$. This is avoided by potential or voltage divider bias shown in the


Here R1 and R2 forms potential dividing Rc collector load resister and its equivalent thevinins circuits is as follows;


This method is widely used since its provides a EARgGTrefert:com
In this method two resistors R1 and R2 connected across the supply voltage Vcc and it provide biasing.
Emitter resistance Re provides bias to BE junction. This causes the base current and hence collector current flows in zero signal condition.
Applying KVL law to BE junction circuit we get fig.

$\mathrm{V}_{\mathrm{B}}$ is the voltage across R 2 which is given by $\mathrm{V}_{\mathrm{B}}=\mathrm{VCC} *(\mathrm{R} 2 /(\mathrm{R} 1+\mathrm{R} 2))$
Jut by taking this value as a source voltage and $\mathrm{R}_{\mathrm{B}}=R 1 \| \mathrm{R} 2$

$$
R_{B}=\frac{R 1 R 2}{R 1+R 2}
$$

We can draw the thevinins equivalent circuit which is shown in fig Then as per KVL law,
$V_{B}-I_{B} R_{B}-V_{B E}-I_{E} R_{E}=0$
$\mathrm{V}_{\mathrm{B}}-\mathrm{I}_{\mathrm{B}} \mathrm{R}_{\mathrm{B}}-\mathrm{V}_{\mathrm{BE}}-\left(\mathrm{I}_{\mathrm{C}}+\mathrm{I}_{\mathrm{B}}\right) \mathrm{R}_{\mathrm{E}}=0 \quad \mathrm{wv}^{2}\left(\mathrm{I}_{\mathrm{E}}=\mathrm{I}_{\mathrm{B}}+\mathrm{I}_{\mathrm{C}}\right)$
$\mathrm{V}_{\mathrm{B}}=\mathrm{I}_{\mathrm{B}} \mathrm{R}_{\mathrm{B}}+\mathrm{V}_{\mathrm{BE}}+\left(\mathrm{I}_{\mathrm{C}}+\mathrm{I}_{\mathrm{B}}\right) \mathrm{R}_{\mathrm{E}}$
Then apply KVL to output side we get
$\mathrm{V}_{\mathrm{CC}}-\mathrm{I}_{\mathrm{C}} \mathrm{R}_{\mathrm{C}}-\mathrm{I}_{\mathrm{E}} \mathrm{R}_{\mathrm{E}}-\mathrm{V}_{\mathrm{CE}}=0$
But $\mathrm{I}_{\mathrm{C}}=\mathrm{I}_{\mathrm{E}}$
$\mathrm{V}_{\mathrm{CC}}-\mathrm{I}_{\mathrm{C}} \mathrm{R}_{\mathrm{C}}-\mathrm{I}_{\mathrm{C}} \mathrm{R}_{\mathrm{E}}-\mathrm{V}_{\mathrm{CE}}=0$
$\mathrm{V}_{\mathrm{CC}}-\mathrm{I}_{\mathrm{C}}\left(\mathrm{R}_{\mathrm{C}}+\mathrm{R}_{\mathrm{E}}\right)-\mathrm{V}_{\mathrm{CE}}=0$
$\mathrm{I}_{\mathrm{C}}\left(\mathrm{R}_{\mathrm{C}}+\mathrm{R}_{\mathrm{E}}\right)=\mathrm{V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{CE}}$
$\mathrm{I}_{\mathrm{C}}=\mathrm{V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{CE}} /\left(\mathrm{R}_{\mathrm{C}}+\mathrm{R}_{\mathrm{E}}\right)$
Also $\quad \mathrm{V}_{\mathrm{CE}}=\mathrm{V}_{\mathrm{CC}}-\mathrm{I}_{\mathrm{C}} /\left(\mathrm{R}_{\mathrm{C}}+\mathrm{R}_{\mathrm{E}}\right)$
Then put $\mathrm{I}_{\mathrm{c}}$ into $\mathrm{V}_{\mathrm{B}}$ we get
$\mathrm{V}_{\mathrm{B}}=\mathrm{I}_{\mathrm{B}} \mathrm{R}_{\mathrm{B}}+\mathrm{V}_{\mathrm{BE}}+\mathrm{R}_{\mathrm{E}}\left[\mathrm{V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{CE}} /\left(\mathrm{R}_{\mathrm{C}}+\mathrm{R}_{\mathrm{E}}\right)+\mathrm{I}_{\mathrm{B}}\right]$
$=I_{B} R_{B}+V_{B E}+I_{B} R_{E}+\left[V_{C C}-V_{C E} /\left(R_{C}+R_{E}\right)\right]$
$\mathrm{V}_{\mathrm{B}}=\mathrm{I}_{\mathrm{B}}\left(\mathrm{R}_{\mathrm{B}}+\mathrm{R}_{\mathrm{E}}\right)+\mathrm{V}_{\mathrm{BE}}+\left[\mathrm{V}_{\mathrm{CC}} * \mathrm{~V}_{\mathrm{CE}} /\left(\mathrm{R}_{\mathrm{C}}+\mathrm{R}_{\mathrm{E}}\right)\right]-\left[\mathrm{V}_{\mathrm{CE}} * \mathrm{R}_{\mathrm{E}} /\left(\mathrm{R}_{\mathrm{C}}+\mathrm{R}_{\mathrm{E}}\right)\right]$

## 7. Explain the frequency response of an amplifier with suitable characteristics.

The plot between the gain of the amplifier and frequency of the signal is known as frequency response of the amplifier. The frequency covers a wide range from 0 Hz to very high frequencies(> 100 MHz ).

Decibels: The decibel (dB) is a measure of the difference in magnitude between two power levels. The power gain in decibel is given by,

$$
\mathrm{G}_{\mathrm{dB}}=10 \log { }_{10} \frac{P_{2}}{P_{1}} \mathrm{~dB}
$$

Where $\mathrm{P}_{2}=$ specified terminal power;

$$
\mathrm{P}_{1}=\text { reference power }
$$

If the power $\mathrm{P}_{2}$ is output power $\left(\mathrm{P}_{0}\right)$ and $\mathrm{P}_{1}$ is input power $\left(\mathrm{P}_{\mathrm{i}}\right)$ of an amplifier. Then the power gain is given by,

$$
\mathrm{G}_{\mathrm{dB}}=10 \log _{10} \frac{\underline{P}_{0}}{P_{i}}
$$

If $\mathrm{V}_{0}$ and $\mathrm{V}_{\mathrm{i}}$ are output and input voltage of an amplifier then voltage gain, $\mathrm{G}_{\mathrm{dB}}=20 \log _{10} \frac{V_{0}}{V_{i}}$
The frequency response is divided into three region 1) Low frequency region 2) Mid frequency region 3) High frequency region.


Fig: Frequency response of an amplifier

1) Mid frequency region: The gain of the amplifier is maximum $A_{v_{\text {mid }}}$ intersecting the frequency response at point $A$ and $B$. The corresponding frequencies $f_{1}$ ans $f_{2}$ are generally called corner, cutoff or half power frequencies.
If the maximum voltage gain in mid-band is $\mathrm{A}_{\mathrm{Vmid}}=\mathrm{V}_{0} / \mathrm{V}_{\mathrm{i}}$ then the gain at half power frequencies is $\mathrm{A}_{\mathrm{Vmid}} / \sqrt{2}$

$$
\text { The output power in mid-band is, } \quad \mathrm{P}_{\mathrm{o}(\text { mid })}=\mathrm{V}_{0}{ }^{2} / \mathrm{R}_{0}=\left(\mathrm{A}_{\mathrm{Vmid}} \mathrm{~V}_{\mathrm{i}}\right) 2 / \mathrm{R}_{0}
$$

The power at half power frequency is, $\mathrm{P}_{\mathrm{o}(\mathrm{HPF})}=\mathrm{V}_{0}{ }^{2} / \mathrm{R}_{0}=\left(\mathrm{A}_{\mathrm{Vmid}} \mathrm{V}_{\mathrm{i}} / \sqrt{ } 2\right)^{2} / \mathrm{R}_{0}$ $=\mathrm{P}_{0 \text { (mid) }} / 2$
2) Cutoff Frequency: The frequency at which the voltage gain is equal to 0.707 times of its maximum value is called cutoff frequency.
3) Bandwidth: The bandwidth of the amplifier is defined as the difference between the two half power frequencies $f_{1}$ and $\mathrm{f}_{2}$

$$
\text { Bandwidth }=\mathrm{f}_{2}-\mathrm{f}_{1}
$$

Where $f_{1}=$ the lower cutoff frequency
$\mathrm{f}_{2}=$ the upper cutoff frequency
4) Low frequency region: In midband frequencies the coupling and bypass capacitor are replaced by short circuits.

$$
\text { Capacitive reactance } \mathrm{X}_{\mathrm{c}}=\frac{1}{2 M f C}
$$

At Low frequency, the coupling and bypass capacitor are increased. Hence the voltage gain decreases.
5) High frequency region: Here the internal capacitance across the junction affects the performance of the amplifier.

The capacitance, $\mathrm{C}_{\mathrm{b}}{ }^{\prime} \mathrm{e}=$ feedback path from bias to emitter
$\mathrm{C}_{\mathrm{ce}}=$ feedback path from collector to emitter
These capacitors divert the signal to ground.
$\mathrm{C}_{\mathrm{b}}{ }^{\prime} \mathrm{c}=$ feedback path from base to collector
This provides a bypass path for the input ac signal.

## MOSFET-Small Signal Model

## 8. Draw and explain the small signal model of MOSFET.

To operate as an small signal amplifier, we bias the MOSFET in saturation region.


- The DC bias Point
- The signal current in the drain
- The voltage gain

The DC bias Point: $I_{D}-1 / 2 K_{n}{ }^{\prime}(\mathrm{W} / \mathrm{L})\left(\mathrm{V}_{\mathrm{GS}}-\mathrm{V}_{\mathrm{t}}\right)^{2}$

$$
\mathrm{V}_{\mathrm{D}}=\mathrm{V}_{\mathrm{DD}}-\mathrm{I}_{\mathrm{D}} \mathrm{R}_{\mathrm{D}}
$$

$\mathrm{V}_{\mathrm{D}} \gg \mathrm{V}_{\mathrm{GS}}-\mathrm{V}_{\mathrm{t}}$
The required signal depends on $V_{D}$, which is sufficiently greater than $\left(V_{G S}-V_{t}\right)$.

## The Voltage Gain:



$$
\begin{aligned}
& V_{D}=V_{D D}-I_{D} R_{D} \\
& V_{D}=V_{D D}-\left(I_{D}+i_{d}\right) R_{D} \\
& V_{D}=V_{D D}-I_{D} R_{D}-i_{d} R_{D} \\
& V_{d}=-i_{d} R_{D}=-g_{\mathrm{m}} V_{\mathrm{gs}} R_{D} \\
& A_{\mathrm{v}}=V_{d} / V_{\mathrm{gs}}=-g_{\mathrm{m}} R_{D}
\end{aligned}
$$

In the small signal analysis, signal are superimposed on the DC quantities,
The drain current, $\quad i_{D}=I_{D}+i_{d}$.
The AC drain current $i_{d}$ is related to $\mathrm{v}_{\mathrm{gs}}$ is so called transistor Trans conductance $\left(\mathrm{g}_{\mathrm{m}}\right)$.

Sometimes expressed in terms of the overdrive voltage, $\mathrm{V}_{\mathrm{OV}}=\mathrm{V}_{\mathrm{GS}}-\mathrm{V}_{\mathrm{t}}$

$$
\mathrm{g}_{\mathrm{m}}=\mathrm{K}_{\mathrm{n}}^{\prime}(\mathrm{W} / \mathrm{L}) \mathrm{V}_{\mathrm{OV}}[\mathrm{~S}]
$$

This $g_{m}$ depends on the bias. The Trans conductance $g_{m}$ equals the slope of $\mathrm{i}_{\mathrm{D}}$. $\mathrm{vgs}^{\mathrm{g}}$ characteristic. Similarly drain voltage, $\mathrm{V}_{\mathrm{D}}=\mathrm{V}_{\mathrm{D}}+\mathrm{V}_{\mathrm{d}}$

In saturation mode, MOSFET acts a voltage controlled current source, The control voltage $\mathrm{V}_{\mathrm{gs}}$ and output current ${ }_{\mathrm{i}}$ give rise to small signal $\Pi$-model.

For Operation in the saturation region $V_{G D} \leq V_{t} \Rightarrow V_{G S}-V_{D S} \leq V_{t}$
Where the total drain to source voltage is $\mathrm{V}_{\mathrm{DS}}=\mathrm{V}_{\mathrm{DS}}+\mathrm{V}_{\mathrm{d}}$


- $\mathrm{i}_{\mathrm{g}}=0$ and $\mathrm{v}_{\mathrm{gs}} \rightarrow$ infinite input resistance
- $r_{0}$ models the finite output resistance in the range from $\approx 10 \mathrm{~K} \Omega$ to $1 \mathrm{M} \Omega$ and depends on bias current $\mathrm{I}_{\mathrm{D}}$.

$$
\mathrm{g}_{\mathrm{m}}=\mathrm{K}_{\mathrm{n}}{ }^{\prime}(\mathrm{W} / \mathrm{L})\left(\mathrm{V}_{\mathrm{GS}}-\mathrm{V}_{\mathrm{t}}\right)
$$

it can be, $\mathrm{g}_{\mathrm{m}}=\mathrm{I}_{\mathrm{D}} /\left(\mathrm{V}_{\mathrm{GS}}-\mathrm{V}_{\mathrm{t}}\right) / 2$
Similar to $g_{m}=I_{C} / V_{T}$ for BJT. Hence the bias current $g_{m}$ is much larger for than for MOSFET.

## MOSFET have these advantages over BJT:

$\checkmark$ High input resistance.
$\checkmark$ Small physical size.
$\checkmark$ Low power dissipation.
$\checkmark$ Relative ease of fabrication.
Becomes amplifiers combines the advantages of BJT and MOSFET, They provide very large input resistance from MOSFET and a large output impedance from the BJT.

## 9. Explain Small signal model of $P$ Channel EASGTEP.



The above diagram shows the common source circuit with p-channel MOSFET and its A.C equivalent circuit. The A.C equivalent circuit seen for n-channel MOSFET also applies to the p-channel MOSFET; however, there is a change in current directions and voltage polarities compared to the circuit containing the $n$-channel MOSFET. The above diagram shows the small signal equivalent circuit of the p-channel MOSFET amplifier.

## 10. Explain the Common - Source (CS) Configuration. (April/May 2019) (Nov/Dec 2017)

The diagram shows the common source circuit with voltage divider biasing and coupling capacitor. The MOSFET is biased near the middle of the saturation region by R1 and R2 resistors to work as an amplifier.
Assume that,the signal frequency is sufficiently large for the coupling capacitor to act essentially as a short circuit. The signal source is represented by a Thevenin equivalent circuit, in which the signal voltage source vs, is in series with an equivalent source resistance Rsi.
Here $\mathrm{R}_{\mathrm{si}}$ should me much less than the amplifier input resistance,
$R_{i}=R_{1} \| R_{2}$ in order to minimize loading effects.
The following diagram shows the resulting small- signal equivalent circuit.


Common-source circuit with
voltage divider biasing and coupling

$V_{o}=-g_{m} V_{g s}\left(r_{o} \| R_{D}\right)$
$\mathrm{V}_{\mathrm{i}}=\mathrm{V}_{\mathrm{gs}}$
$A_{v}=v_{o} / v_{i}=-g_{m} v_{g s}\left(r_{o} \| R_{D}\right) / v_{g s}=-g_{m}\left(r_{o} \| R_{D}\right)$
The input gate to source voltage is
$v_{i}=\left(R_{i} / R_{i}+R_{s i}\right) v_{s}$
So the small signal overall voltage gain is,

## $G_{v}=v_{o} / v_{s}=-\mathbf{g}_{\mathrm{m}}\left(\mathbf{r}_{\mathbf{o}} \| \mathbf{R}_{\mathrm{D}}\right)\left(\mathbf{R}_{\mathrm{i}} / \mathbf{R}_{\mathrm{i}}+\mathbf{R}_{\mathrm{s}}\right)=\mathbf{A}_{\mathrm{v}}\left(\mathbf{R}_{\mathrm{i}} / \mathbf{R}_{\mathrm{i}}+\mathbf{R}_{\mathrm{s}}\right)$

Since Rsi is not zero, the amplifier input signal $v_{i}$ is less than the signal voltage, This is known as loading effect. It reduces the voltage gain of the amplifier.
The input resistance is $\mathrm{R}_{\text {is }}=\mathrm{R}_{1} \| \mathrm{R}_{2}$
The output resistance is $R_{o}=R_{D} \| r_{o}$
We can also relate the A.C drain current to the A.C drain to source voltage, as
$V_{d s}=-I_{d}\left(R_{D}\right)$

## 11. Analysis of Common - Drain (CD) or Source follower Amplifier.(Nov/Dec 2016)(May 2017)



The above diagram shows the common - drain amplifier circuit. It is also known as grounded drain amplifier.
In this amplifier circuit, drain is used as a signal ground and hence RD is not needed.
The input signal is coupled to via Cc1 to the MOSFET gate and the output signal at the output signal at the MOSFET source is coupled via Cc2 to a load resistance RL.
Since RL is in effect connected in series with the source terminal of the MOSFET, it is more convenient to use the MOSFET's T model for the analysis. This is shown in the following diagram.
$\mathrm{R}_{\mathrm{i}}=\mathrm{R}_{\mathrm{G}}$
$\mathrm{v}_{\mathrm{i}}=\mathrm{v}_{\mathrm{s}} \mathrm{x} \mathrm{R}_{\mathrm{i}} /\left(\mathrm{R}_{\mathrm{i}}+\mathrm{R}_{\mathrm{si}}\right)=\mathrm{v}_{\mathrm{s}} \mathrm{x} \mathrm{R}_{\mathrm{G}} /\left(\mathrm{R}_{\mathrm{G}}+\mathrm{R}_{\mathrm{si}}\right)$
From the following diagram it can be seen that the load resistance RL is in parallel with ro and resistance $1 / \mathrm{gm}$ in series with $\mathrm{R}_{\mathrm{L}} \| \mathrm{r}_{\mathrm{o}}$.

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The input voltage $v_{i}$ appears across the total resistance and hence by applying the voltage divider rule, we have $v_{o}=v_{i x}\left(R_{L} \| r_{o}\right) /\left(1 / g_{m}\right)+\left(R_{L} \| r_{o}\right)$ $A_{v}=v_{o} / v_{i}=\left(R_{L} \| r_{o}\right) /\left(1 / g_{m}\right)+\left(R_{L} \| r_{o}\right)$

The open circuit voltage gain $\mathrm{A}_{\mathrm{vo}}(\mathrm{RL}=$ Infinity) is given as
$\mathrm{A}_{\mathrm{v}}=\mathrm{r}_{\mathrm{o}} /\left(1 / \mathrm{g}_{\mathrm{m}}\right)+\mathrm{r}_{\mathrm{o}}$
Since $r_{0} \gg 1 / \mathrm{gm}$, the open circuit voltage gain tends to unity; however, it is always less than unity.
Usually, $\mathrm{R}_{\mathrm{L}} \ll \mathrm{r}_{\mathrm{o}}$ and hence the voltage gain given by above expression Av becomes
$\mathrm{A}_{\mathrm{v}}=\mathrm{v}_{\mathrm{o}} / \mathrm{v}_{\mathrm{i}}=\mathrm{R}_{\mathrm{L}} /\left(1 / \mathrm{g}_{\mathrm{m}}\right)+\mathrm{R}_{\mathrm{L}}$
( $\mathrm{R}_{\mathrm{L}} \ll \mathrm{r}_{\mathrm{o}}$ )
$\mathrm{A}_{\mathrm{vs}}=\mathrm{G}_{\mathrm{v}}=\mathrm{v}_{\mathrm{o}} / \mathrm{v}_{\mathrm{s}}=\mathrm{v}_{\mathrm{o}} / \mathrm{v}_{\mathrm{i}} \mathrm{XV}_{\mathrm{i}} / \mathrm{v}_{\mathrm{s}}$
$=\left(R_{L} \| r_{o}\right) /\left(1 / g_{m}\right)+\left(R_{L} \| r_{o}\right) X R_{G} /\left(R_{G}+R_{s i}\right)$
The output resistance is given by
$\mathrm{R}_{\mathrm{o}}=1 / \mathrm{g}_{\mathrm{m}} \| \mathrm{r}_{\mathrm{o}}=1 / \mathrm{g}_{\mathrm{m}}$.

D.C. Ioad line and transition point separating saturation and non-saturatiol regions
The above diagram shows the D.C load line, the transition point, and the Q- point, which is in the saturation region.

## 12. Explain High - Frequency MOSFET Model.

Following diagram shows the high frequency equivalent circuit model for MOSFET. In this model, capacitance $\mathrm{C}_{\mathrm{db}}$ can be neglected to simplify the analysis. The resulted model is shown


High frequency equivalent circuit neglecting $C_{d b}$

## 13. Calculate the current gain of high frequency model. (OR) Derive an expression for MOSFET unity gain frequency(f $f_{T}$ ). (April/May 2019)

The $\mathrm{f}_{\mathrm{T}}$ is the frequency at which the short - circuit current gain of the CS MOSFET amplifier becomes unity.


The above diagram shows the modified high - frequency equivalent circuit to determine the short - circuit current gain. Here, the input is fed with a current - source signal Ii and the output terminals are shorted.
The short circuit current Io is given by
$\mathrm{I}_{\mathrm{o}}=\mathrm{g}_{\mathrm{m}} \mathrm{V}_{\mathrm{gs}}-\mathrm{s} \mathrm{C}_{\mathrm{gd}} \mathrm{Vgs}_{\mathrm{gs}}$

The second term in the above equation is veFyngit ame can Be neglected at the frequencies of interest and thus $\mathrm{I}_{\mathrm{o}}=\mathrm{g}_{\mathrm{m}} \mathrm{V}_{\mathrm{gs}}$
The Vgs in terms of Ii can be given by
$\mathrm{V}_{\mathrm{gs}}=\mathrm{I}_{\mathrm{i}} / \mathrm{s}\left(\mathrm{C}_{\mathrm{gs}}+\mathrm{C}_{\mathrm{gd}}\right)$
Substituting the values of $\mathrm{I}_{\mathrm{i}}$ and $\mathrm{I}_{0}$ from the above equations we have
$\mathrm{I}_{\mathrm{o}} / \mathrm{I}_{\mathrm{i}}=\mathrm{g}_{\mathrm{m}} \mathrm{V}_{\mathrm{gs}} / \mathrm{V}_{\mathrm{gs} .} \mathrm{s}\left(\mathrm{C}_{\mathrm{gs}}+\mathrm{C}_{\mathrm{gd}}\right)=\mathrm{g}_{\mathrm{m}} / \mathrm{s}\left(\mathrm{C}_{\mathrm{gs}}+\mathrm{Cgd}_{\mathrm{gd}}\right)$
For physical frequencies $\mathrm{s}=\mathrm{j} \omega$. From above equation it can be seen that the magnitude of the current becomes unity at the frequency.
$\omega_{\mathrm{T}}=\mathrm{g}_{\mathrm{m}} / \mathrm{C}_{\mathrm{gs}}+\mathrm{C}_{\mathrm{gd}}$
$\mathrm{f}_{\mathrm{T}}=\mathrm{g}_{\mathrm{m}} / 2 \pi\left(\mathrm{C}_{\mathrm{gs}}+\mathrm{Cgd}_{\mathrm{gd}}\right)$
From the above expression we can say that $\mathrm{f}_{\mathrm{T}}$ is proportional togm and inversely proportional to the internal capacitances.
14. Explain Frequency response of CS Amplifier. (Apr/May 2018) (OR) With neat circuit diagram, perform ac analysis for common source using equivalent circuit NMOSFET AMPLIFIER (NOV/DEC2015)
The following diagram shows the CS MOSFET amplifier. Its gain falls at low frequency due to the effect of $\mathrm{C}_{\mathrm{c} 1}$ and $\mathrm{C}_{\mathrm{s}}$ and $\mathrm{C}_{\mathrm{c} 2}$. Its gain falls at high frequency due to the effect of $\mathrm{C}_{\mathrm{gs}}$ and $\mathrm{C}_{\mathrm{gd}}$.


CS MOSFET amplifier


Frequency response of CS MOSFET amplifier
Above diagram shows frequency response of CS MOSFET amplifier.

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## High Frequency Response:



Equivalent circuit for CS MOSFET amplifier
The above diagram shows equivalent circuit for CS MOSFET amplifier.
Let us consider the output node. The load current is $g_{m} V_{g s}-I_{g d}$, where $g_{m} V_{g s}$ is the output current of the MOSFET and $I_{g d}$ is the current supplied through the very small capacitance $C_{g d}$.
At frequencies in the vicinity of $f_{H}$, the $I_{g d}$ is very small and can be neglected.
Hence we can write
$\mathrm{V}_{\mathrm{o}} \approx-\mathrm{I}_{\mathrm{L}} \mathrm{R}_{\mathrm{L}}=-\mathrm{g}_{\mathrm{m}} \mathrm{V}_{\mathrm{gs}} \mathrm{R}_{\mathrm{L}}{ }^{`}$
Where $\mathrm{R}_{\mathrm{L}}=\mathrm{r}_{\mathrm{o}}\left\|\mathrm{R}_{\mathrm{d}}\right\| \mathrm{R}_{\mathrm{L}}{ }^{`}$
Now consider the input node. We can replace Cgd at the input side with the equivalent capacitance Ceq using Miller's theorem. This is shown in the following diagram.


By Miller's theorem, equivalent capacitance is given by,
$\mathrm{C}_{\mathrm{eq}}=\left(1+\mathrm{A}_{\mathrm{v}}\right) \mathrm{C}=\left(1+\mathrm{A}_{\mathrm{v}}\right) \mathrm{C}_{\mathrm{gd}}$
Since input voltage Vgs, we have
$\mathrm{A}_{\mathrm{v}}=\mathrm{V}_{\mathrm{o}} / \mathrm{V}_{\mathrm{i}}=-\mathrm{g}_{\mathrm{m}} \mathrm{V}_{\mathrm{gs}} \mathrm{R}_{\mathrm{L}}{ }^{\prime} / \mathrm{V}_{\mathrm{gs}}=-\mathrm{g}_{\mathrm{m}} \mathrm{R}_{\mathrm{L}}{ }^{`}$
$\mathrm{C}_{\mathrm{eq}}=\left(1+\mathrm{g}_{\mathrm{m}} \mathrm{R}_{\mathrm{L}}{ }^{`}\right)=$ Total input capacitance Cin can be given by,
$\mathrm{C}_{\mathrm{in}}=\mathrm{C}_{\mathrm{gs}}+\mathrm{C}_{\mathrm{eq}}=\mathrm{C}_{\mathrm{gs}}+\left(1+\mathrm{g}_{\mathrm{m}} \mathrm{R}_{\mathrm{L}}{ }^{`}\right) \mathrm{C}_{\mathrm{gd}}$
The total resistance is given by,
$\mathrm{R}_{\mathrm{si}}{ }^{`}=\mathrm{R}_{\mathrm{si}} \| \mathrm{R}_{\mathrm{G}}$
By considering input circuit as a simple- time constant circuit we have
$\mathrm{T}=\mathrm{RC}=\mathrm{R}_{\mathrm{si}}{ }^{\wedge} \mathrm{C}_{\mathrm{in}}$
$\omega_{\mathrm{H}}=\omega_{\mathrm{o}}=1 / \mathrm{T}=1 / \mathrm{R}_{\mathrm{si}}{ }^{\prime} \mathrm{C}_{\mathrm{in}}$
$\mathrm{f}_{\mathrm{H}}=1 / 2 \pi \mathrm{R}_{\mathrm{si}}{ }^{\prime} \mathrm{C}_{\mathrm{in}}$

## 15. Explain small signal model of MOSFET.



NMOS common-source
circuit with time varying
signal source in series with
gate d.c. source
From the above diagram, we see that the output voltage is

$$
\begin{aligned}
& \mathrm{v}_{\mathrm{ds}}=\mathrm{V}_{\mathrm{o}}=\mathrm{V}_{\mathrm{DD}}-\mathrm{i}_{\mathrm{D}} \mathrm{R}_{\mathrm{D}} \\
& \mathrm{v}_{\mathrm{o}}=\mathrm{V}_{\mathrm{DD}}-\left(\mathrm{I}_{\mathrm{DQ}}+\mathrm{i}_{\mathrm{d}}\right) \mathrm{R}_{\mathrm{D}}=\left(\mathrm{V}_{\mathrm{DD}}-\mathrm{I}_{\mathrm{DQ}} \mathrm{R}_{\mathrm{D}}\right)-\mathrm{i}_{\mathrm{d}} \mathrm{R}_{\mathrm{D}}
\end{aligned}
$$

The output voltage is also a combination of D.C and A.C values. The time - varying output signal is the time - varying drain to source voltage, or
$\mathrm{Vo}=\mathrm{Vds}=-\mathrm{i}_{\mathrm{d}} \mathrm{R}_{\mathrm{D}}$
We have,
$\mathrm{i}_{\mathrm{d}}=\mathrm{g}_{\mathrm{m}} \mathrm{V}_{\mathrm{g}}$
In summary, the following relationships exist between the time varying signals for the circuit. The equations are given in terms of the instantaneous A.C values as well as the phasors. We have,

$$
\mathrm{v}_{\mathrm{gs}}=\mathrm{v}_{\mathrm{i}}
$$

(or)
$\mathrm{V}_{\mathrm{gs}}=\mathrm{V}_{\mathrm{i}}$ and
$I_{d}=g_{m} V_{g s}$
(or)
$\mathrm{I}_{\mathrm{d}}=\mathrm{g}_{\mathrm{m}} \mathrm{V}_{\mathrm{gs}} \quad$ also
$v_{d s}=-i_{d} R_{D}$
(or)
$V_{d s}=-I_{d} R_{D}$


The above diagram shows the A.C equivalent circuit. Here, the D.C sources are made zero.
From the equivalent circuit for the NMOS amplifier circuit, we can draw a small signal equivalent circuit for the MOSFET.


Expanded small signal equivalent circuit, including output resistance, for NMOS transistor


Common-source NMOS transistor with small signal parameters

The above diagram shows the small signal low frequency A.C equivalent circuit for $\mathrm{n}-$ channel MOSFET.
The relation of $\mathrm{I}_{\mathrm{d}}$ by $\mathrm{V}_{\mathrm{gs}}$ is included as a current source gm vgs connected from drain to source.
The input impedance is represented by the open circuit at its input terminals, since gate current IG is zero.
We know that the circuit has the finite output resistance of a MOSFET biased in the saturation region because of the nonzero slope in the $\mathrm{I}_{\mathrm{D}}$ versus $\mathrm{V}_{\mathrm{DS}}$ curve.

We also know that,
$\mathrm{i}_{\mathrm{D}}=\mathrm{K}\left[\left(\mathrm{v}_{\mathrm{CS}}-\mathrm{V}_{\mathrm{T}}\right)^{2}(1+\lambda \mathrm{VDS})\right]$
where $\lambda$ is the channel length modulation parameter and is a positive quantity. The small signal output resistance, is defined as,
$\mathrm{r}_{\mathrm{o}}=\left(\partial_{\mathrm{i}_{\mathrm{D}}} / \partial \mathbf{v}_{\mathrm{DS}}\right)^{-1} \mid \mathrm{v}_{\mathrm{GS}}=\mathrm{V}_{\mathrm{GSQ}}=$ const.
$\mathrm{r}_{\mathrm{o}}=\left[\lambda \mathrm{K}\left[\left(\mathrm{v}_{\mathrm{GSQ}}-\mathrm{V}_{\mathrm{T}}\right)^{2}\right]^{-1} \approx\left[\lambda \mathrm{I}_{\mathrm{DQ}}\right]^{-1}\right.$
This small signal output resistance is also a function of the Q - point parameters. The following diagram shows the small signal equivalent circuit of common - source circuit.


Small signal equivalent circuit of common-source circuit with NMOS transistor
model

1. For the circuit below, find (i) dc bias levels (ii) dc voltage across the capacitors (iii) ac emitter resistance (iv) voltage gain (v) state of the transistor. (Nov/Dec 2018)


## Solution:

Given that,
Emitter resistance, $\mathrm{R}_{\mathrm{E}}=1 \mathrm{~K} \Omega$
Collector resistance, $\mathrm{R}_{\mathrm{C}}=2 \mathrm{~K} \Omega$
Load resistance, $\mathrm{R}_{\mathrm{L}}=1 \mathrm{~K} \Omega$
Collector input voltage, $\mathrm{V}_{\mathrm{CC}}=15 \mathrm{~V}$
Amplification factor, $\beta=100$
Input resistance, $\mathrm{R}_{1}=40 \mathrm{~K} \Omega$ and $\mathrm{R}_{2}=10 \mathrm{~K} \Omega$
Voltage gain, $\mathrm{Av}=$ ?
AC emitter resistance, $\mathrm{r}_{\mathrm{e}}=$ ?
i. DC bias levels: DC bias levels of CE amplifier determined by calculating various dc voltages and dc currents.

DC voltage, $\mathrm{V}_{2}$ across resistor, $\mathrm{R}_{2}$ is

$$
V_{2}=\frac{V_{C C}}{R_{1}+R_{2}} X R_{2}
$$

Substituting the corresponding values, $\mathrm{V}_{2}$ is obtained as,

$$
\begin{gathered}
V_{2}=\frac{15}{40+10} \times 10 \\
V_{2}=3 \mathrm{~V}
\end{gathered}
$$

DC emitter voltage, $\mathrm{V}_{\mathrm{E}}$ across emitter resistor, $\mathrm{R}_{\mathrm{E}}$ is,

$$
\begin{gathered}
\mathrm{V}_{\mathrm{E}}=\mathrm{V}_{2}-2 \mathrm{~V}_{\mathrm{BE}} \\
=3 \mathrm{~V}-0.7 \mathrm{~V} \\
=2.3 \mathrm{~V}
\end{gathered}
$$

DC emitter voltage, $\mathrm{V}_{\mathrm{E}}=2.3 \mathrm{~V}$
DC emitter current, $\mathrm{I}_{\mathrm{E}}$ is given by,

$$
\begin{gathered}
I_{E}=\frac{\underline{V}_{E}}{R_{E}} \\
I_{E}=\frac{2.3 \mathrm{~V}}{1 K \Omega}=2.3 \mathrm{~mA}
\end{gathered}
$$

DC Collector voltage, $\mathrm{V}_{\mathrm{C}}$ is determined as, $\mathrm{V}_{\mathrm{C}}=\mathrm{V}_{\mathrm{CC}}-\mathrm{I}_{\mathrm{C}} \mathrm{R}_{\mathrm{C}}$

$$
\begin{gathered}
\mathrm{V}_{\mathrm{C}}=15 \mathrm{~V}-2.3 \mathrm{X} 2 \mathrm{~K} \Omega \\
\mathrm{~V}_{\mathrm{C}}=10.4 \mathrm{~V}
\end{gathered}
$$

DC base current, $\mathrm{I}_{\mathrm{B}}$ is obtained as,

$$
\begin{aligned}
& \text { Using the sehation } \mathrm{I}_{\mathrm{C}}=\beta \mathrm{I}_{\mathrm{B}} \\
& \mathrm{I}_{\mathrm{B}}=\frac{-}{\mathrm{B}}=\frac{}{100}=0.023 \mathrm{~mA}
\end{aligned}
$$

ii. DC voltages across the capacitors: Fromqgabre comations, DC voltages across capacitors in the circuit is obtained as,

DC voltage across capacitor, $\mathrm{C}_{\mathrm{in}}$ is, $\mathrm{V}_{2}=3 \mathrm{~V}$
DC voltage across emitter capacitor, $\mathrm{C}_{\mathrm{E}}$ is, $\mathrm{V}_{\mathrm{E}}=2.3 \mathrm{~V}$
DC voltage across collector capacitor, $\mathrm{C}_{\mathrm{C}}$ is $\mathrm{V}_{\mathrm{C}}=1.4 \mathrm{~V}$
iii. AC Emitter Resistance: The ac emitter resistance, $\mathrm{r}_{\mathrm{e}}{ }^{\prime}$ is given by, $\left[\mathrm{I}_{\mathrm{E}}=2.3 \mathrm{~mA}\right]$

$$
\mathrm{r}_{\mathrm{e}}^{\prime}=\frac{25 \mathrm{mV}}{\mathrm{I}_{\mathrm{E}}}=\frac{25 \mathrm{mV}}{2.3 \mathrm{~mA}}=10.9 \Omega
$$

iv. Voltage Gain( $\mathbf{A}_{v}$ ): The voltage gain $\mathrm{A}_{v}$ of CE amplifier is defined by,

$$
\mathrm{A}_{\mathrm{V}}=\frac{\mathrm{r}_{\mathrm{c}}}{\mathrm{r}^{\prime}}{ }_{\mathrm{e}}
$$

Here, total ac collector resistance, $\mathrm{r}_{\mathrm{c}}$ is determined by, $\quad r_{e}=R_{c} \| R_{L}$

$$
r=\frac{R_{C} \underline{R_{L}}}{R_{C}+R_{L}}=\frac{2 X 1}{2+1} 10.9 \Omega=0.667 \mathrm{~K} \Omega
$$

Substituting $\mathrm{r}_{\mathrm{c}}$ value in $\mathrm{A}_{\mathrm{V}}$, implies,

$$
A_{V}=\frac{0.667 \mathrm{~K} \Omega}{10.9 \Omega}
$$

Voltage gain, $A_{v}=61.2$
v. State of transistor: From the above calculation it can be determined that the transistor is in active state.

Since $V_{C}>V_{E}$
2. Determine the mid band gain, the upper 3 dB frequency $f_{H}$ of a $C S$ amplifier fed with a signal source having an internal resistance $R_{\text {sig }}=100 \mathrm{~K} \Omega$. The amplifier has $R G=4.7 \mathrm{M} \Omega, R_{D}=R_{L}=15 \mathrm{~K} \Omega \mathrm{gm}=1 \mathrm{~mA} / \mathrm{V}, \mathrm{r}_{0}=150$ $\mathrm{K} \Omega, \mathrm{C}_{\mathrm{gs}}=1 \mathrm{pF}$ and $\mathrm{C}_{\mathrm{gd}}=0.4 \mathrm{pF}$. (May/June2016)


Solution: $A_{M}=\stackrel{R_{G}}{ } g_{m} R_{L}^{\prime}$

$$
\begin{array}{r}
R_{G}+R_{\text {Sig }} \\
\text { Where } \quad R_{L}^{\prime}=r_{0}\left\|R_{D}\right\| R_{L}=150\|15\| 15=7.14 \mathrm{~K} \Omega \\
g_{m} R_{L}^{\prime}=1 \times 7.14=7.14 \mathrm{~V} / \mathrm{V}
\end{array}
$$

Thus $\quad=-\frac{4.7}{4.7+0.1} \times 7.14=-7 V / V$
$A_{M}$
The equivalent capacitance $\mathrm{C}_{\mathrm{eq}}$ is found as

$$
C_{e q}=\left(1+g_{m} R_{L}^{\prime}\right) C_{g d}=(1+7.14) \times 0.4=3.26 p F
$$

The total input capacitance $\mathrm{C}_{\mathrm{in}}$ can be now obtained as

$$
C_{i n}=C_{g d}+C_{e q}=1+3.26=4.26 p F
$$

The upper 3 dB frequency $\mathrm{f}_{\mathrm{H}}$ is found from

$$
f_{H}=\frac{1}{2 \pi C_{i n}\left(R_{\text {sig }} \| R_{G}\right)}=\frac{1}{2 \pi \times 4.26 \times 1^{-12}(0.1 \| 4.7) \times 10^{6}}=382 \mathrm{kHz}
$$

3. The MOSFET shown fig has the followingpqgTree $\mathcal{G O m}_{2} \mathrm{E}_{2}, Q=0.5 \times 10^{-3}, \mathrm{r}_{\mathrm{d}}=75 \mathrm{~K} \Omega$. It is biased at at $\mathrm{Id}=1.9 \mathrm{~m}$ A. (Nov/Dec2017)

a) Verify that the MOSFET is biased in its active region.
b) Find the input resistance.
c) Draw the small single equivalent circuit and find the voltage gain VL/VS.

Solution:
a) $\mathrm{V}_{\mathrm{DS}}=\mathrm{V}_{\mathrm{DD}}-\mathrm{I}_{\mathrm{D}}\left(\mathrm{R}_{\mathrm{D}}+\mathrm{R}_{\mathrm{S}}\right)=18-(1.9 \mathrm{~mA})(2.2 * 103+500)=12.87 \mathrm{~V}$

$$
V_{G}=\left(\frac{22 * 10^{6}}{47 * 10^{6}+22 * 10^{6}}\right) 18=5.74 \mathrm{~V}
$$

Using equation 7.25 to find $\mathrm{V}_{\mathrm{GS}}$, we have
$\mathrm{V}_{\mathrm{GS}}=5.74-(1.9)(5)=4.79 \mathrm{~V}$

$$
\left|V_{G S}-V_{T}\right|=|4.79-2|=2.79 \mathrm{~V}
$$

Therefore condition 8.30 is satisfied;

$$
12.87=\left|V_{D S}\right|>\left|V_{G S}-V_{T}\right|=2.79
$$

And we conclude that the MOSFET is biased in its active region.
b)

$$
r_{i n}=R_{1} \| R_{2}=(47 M \Omega \|(22 M \Omega)=15 M \Omega
$$

c) From equation 8.31,

$$
\mathrm{g}_{\mathrm{m}}=0.5 * 10^{-3}(4.79-2)=1.4 * 10^{-3} \mathrm{~S}
$$

The small single equivalent circuit is shown in fig 8.33 from equation 8.33

$$
\begin{aligned}
& \frac{v_{L}}{v_{s}}=\left(\frac{15 * 10^{6}}{10 * 10^{3}+15 * 10^{6}}\right) *\left(-1.4 * 10^{-3}\right)\left[\left(75 * 10^{3} \|\left(2.2 * 1^{3} \|\left(100 * 10^{3}\right)\right]\right.\right. \\
= & (0.999)\left(-1.4 * 10^{-3}\right)\left(2.09 * 10^{3}\right)=-2.92
\end{aligned}
$$

4. A CC amplifier shown in below figure Fngq $\ddagger C=1$ transistors is 100 and the load resistor is $600 \Omega$ find rin and Av. (Nov/Dec 2015)


Given:
$V_{C C}=15 \mathrm{~V}, R_{B}=75 \mathrm{~K} \Omega, R_{E}=910 \Omega, \beta=100, R L=600 \Omega$
To Find: $\mathrm{r}_{\mathrm{in}}$ and $\mathrm{A}_{V}$
Formulae used $I_{B}=\frac{V_{\underline{C C}}-0.7}{R_{B}+(\beta+1) R_{E}}, I_{E}=\left(1+\beta{ }_{B}{ }^{\prime} r_{E}=\frac{0.026}{I_{E}}\right.$

$$
\begin{gathered}
r_{\text {in }}(\text { stage })=(\beta+1)\left(r_{e}+r_{L}\right) \| R_{B} \\
V_{L}=R_{E} \| R_{L} \\
r_{\text {in }}(\text { stage })=(\beta+1)\left(r_{e}+R_{E}\right) \\
r_{o}(\text { staqe })=R_{R} \| r_{e} \quad\left(r_{s}=0\right) \\
A=\frac{R_{E}}{r_{E}+R_{E}}=\frac{}{r} \text { (output open) }
\end{gathered}
$$

Calculation:

$$
\begin{gathered}
I_{B}=\frac{V_{C C}-0.7}{R_{B}+(\beta+1) R_{E}}=\frac{15-0.7}{75000+(100+1) 910}=\frac{15-0.7}{75000+101 * 910}=\frac{143}{166910} \\
=8.5674 \times 10^{-4} A \\
I_{E}=(1+\beta) I_{B}=(101) \times 8.5674 \times 10^{-4}=0.08653 A \\
r_{E}=\frac{0.026}{I_{E}}=\frac{0.026}{0.08653}=0.300 \\
r_{\text {in }}(\text { stage })=(\beta+1)\left(r_{L}+R_{E R_{E}}=(101) \times(9000+910)=91940.3 \mathrm{ohms}\right. \\
A=\frac{910}{V_{S}}=\frac{r_{E}+R_{E}}{r_{E}}=\frac{10.999}{910+0.300}=0
\end{gathered}
$$

5. Evaluate the $A_{I}, A_{v}, R_{i}, R_{\mathbf{0}}, A_{i s}, A_{v s}$ of EnggTree. cem amplifier with $R_{s}=1 \mathrm{~K} \Omega R_{1}=22 \mathrm{~K} \Omega, R_{2}=10 \mathrm{~K} \Omega$, $R_{\mathrm{c}}=2 \mathrm{~K} \Omega, \mathrm{R}_{\mathrm{L}}=2 \mathrm{~K} \Omega, \mathrm{~h}_{\mathrm{fe}}=50, \mathrm{~h}_{\mathrm{ie}}=1.1 \mathrm{~K} \Omega, \mathrm{~h}_{\mathrm{oe}}=25 \mu \mathrm{~A} / \mathrm{V}$ and $\mathrm{h}_{\mathrm{re}}=2.5 \times 10^{-4}$
(Nov/Dec 2016)


Given
$\mathrm{R}_{\mathrm{s}}=1 \mathrm{~K} \Omega \mathrm{R}_{1}=22 \mathrm{~K} \Omega, \mathrm{R}_{2}=10 \mathrm{~K} \Omega \mathrm{R}_{\mathrm{c}}=2 \mathrm{~K} \Omega, \mathrm{R}_{\mathrm{L}}=2 \mathrm{~K} \Omega, \mathrm{~h}_{\mathrm{fe}}=50, \mathrm{~h}_{\mathrm{ie}}=1.1 \mathrm{~K} \Omega, \mathrm{~h}_{\mathrm{oe}}=25 \mu \mathrm{~A} / \mathrm{V}$ and $\mathrm{h}_{\mathrm{re}}=2.5 \mathrm{X} 10^{-4}$.
i) Current gain

Input impedance $\quad R_{i}=h_{i e}=1.1 \mathrm{k} \Omega$

$$
A_{i}=-h_{f e}=-50
$$

$$
\begin{gathered}
R_{i}=h_{i e}\left\|R_{1}\right\| R_{2} \\
=1.1 \times 10^{3}\left\|22 \times 10^{3}\right\| 10 \mathrm{k} \Omega \\
=12 \times 10 \times 10^{6} \\
=10^{3} \|\left[\frac{32 \times 10^{3}}{32}\right] \\
=1.1 \times 10^{3} \|\left[\frac{220 \times 10^{3}}{32}\right]
\end{gathered}
$$

$$
\begin{aligned}
& =1.1| | 68 / k \\
& =\frac{1.1 \times 6.87 \times 10^{6}}{(1.1+6.87) 10^{3}}=\frac{7.56 \times 10^{6}}{7.975 \times 10^{3}}=0.947 \times 10^{3}=947 \Omega
\end{aligned}
$$

iii)Voltage gain
$A_{v}=\frac{A_{I} R_{L}^{\prime}}{R_{i}}=\frac{-50 \times\left(R_{c} \| R_{L}\right)}{R_{i}}=\frac{-50(2 k \| 2 k)}{1.1 k}=-45.45$
Output voltage

Over all voltage gain

$$
\begin{gathered}
R_{0}=\frac{1}{y_{0}}=\infty \\
R_{0}^{\prime}=R_{0}\left\|R_{L}^{\prime}=\infty\right\| 2 k \quad \| 2 k=1 k
\end{gathered}
$$

$$
\begin{gathered}
A_{v s}=A_{V} \times \frac{V_{i n}}{V_{s}} \\
A_{v s}=\frac{V_{o}}{V_{s}}=\frac{V_{o}}{V_{b}} \times \frac{V_{b}}{V_{s}} \\
\text { where } \frac{V_{o}}{V_{b}}=A v \text { ad } \quad \frac{V_{b}}{V_{s}}=\frac{R_{1}}{R_{1}+R_{3}} \\
A_{v s}=\frac{A v R_{i}^{\prime}}{R_{i}^{\prime}+R_{s}}=\frac{-45.45 \times 947}{947+1 k}=\frac{-45.45 \times 947}{1947}=-22.106
\end{gathered}
$$

Overall current gain

$$
\begin{gathered}
A_{i s}=\frac{I_{L}}{I_{S}}=\frac{I_{L}}{I_{C}} \times \frac{I_{C}}{I_{b}} \times \frac{I_{b}}{I_{S}} \\
\frac{L_{L}}{I_{C}}=\frac{R_{c}}{R_{c}+R}=\frac{-2 k}{2 k+\mathbb{R}}=\frac{-2 k}{4 k}=-0.5 \\
\frac{I_{C}}{I_{b}}=h_{f e}=50 \\
\frac{I_{b}}{I_{S}}=\frac{R_{B}}{R_{B}+R}=\frac{22 \| 10}{22 \| 10+11 k}=\frac{6.87 k}{6.87 k+11 k}=\frac{6.87}{7.97}=0.86
\end{gathered}
$$

$$
\begin{aligned}
\mathrm{A}_{\mathrm{I}} & =\frac{I_{L}}{I_{S}} \\
& =-0.5 \times 50 \times 0.86 \\
A_{I S} & =-21.54
\end{aligned}
$$

6. Fig shows a common emitter amplifier. Determine the input resistance, ac load resistance, voltage gain and output voltage? (May 2017)


Given:
$V_{C C}=12 V, R_{C}=10 k \Omega, R_{\alpha}=3 \mathrm{k} \Omega, \beta=60, R_{1}=100 \mathrm{k} \Omega, R_{2}=50 \mathrm{k} \Omega, r_{E}=1 \mathrm{k} \Omega, R_{E 1}=2 \mathrm{k} \Omega, R_{s}=$ $100 \Omega$,

$$
V_{s}=10 \mathrm{mV}
$$

Input resistance looking directly into the base.

$$
\begin{gathered}
V_{t h}=V_{C C}\binom{R_{2}}{R_{1}+R_{2}}=12\left(\frac{50 \times 10^{3}}{2}\right) \\
=12\left(\frac{50}{100 \times 10^{3}+50 \times 10^{3}}\right) \\
\frac{12}{3}=4 \mathrm{~V} \\
=\frac{100 \times 50 \times 10^{3} \times 10^{3}}{10^{3} \times 100+50 \times 10^{3}}=\frac{100 \times 50 \times 10^{3}}{10^{3}(150)} \\
=\frac{500 \times 10^{3}}{15}=\frac{100 \times 10^{3}}{3}=33.3 \times 10^{3} \Omega=33.3 \mathrm{k} \Omega \\
\text { Emitter resistance }\left(R_{E}\right)
\end{gathered}
$$

$$
\begin{gathered}
R_{E}=\text { EngqTrRe.cqu }{\underset{R}{2}}^{V_{t h}-2 k \Omega=3 k \Omega} \\
I_{E}=\frac{R_{B E}}{R_{E}+\frac{R_{t h}}{\beta}} \\
=\frac{4-0.7}{3 \times 10^{3}+\frac{33.3 \times 10^{3}}{60}} \\
I_{E}=\frac{3.3}{3555.55}=0.000928=.92 \mathrm{~mA}
\end{gathered}
$$

## A.C resistance

$$
r_{e}^{1}=\frac{25}{I_{E}(m A)}=\frac{25}{0.92}
$$

Input resistance

$$
\begin{gathered}
R_{i}=\beta\left(r_{E}+r_{e}^{1}\right)=27 \Omega \\
=60\left(1 \times 10^{3}+27\right) \\
=61620 \Omega \\
=61.6 \mathrm{k} \Omega
\end{gathered}
$$

## Input resistance of the stage

$$
\begin{gathered}
R i s=\left(R_{1} \| R_{2}\right) \| \quad\left[\beta\left(r_{E}+r_{e}^{1}\right)\right] \\
=\frac{33.33 \times 61.6 \times 10^{3} \times 10^{3}}{33.33 \times 10^{3}+61.6 \times 10^{3}} \\
=\frac{2053.12 \times 10^{3}}{94.93} \\
=21.62 \mathrm{k} \Omega
\end{gathered}
$$

## A.C load resistance

$$
\begin{gathered}
r_{2}=R_{c} \| R_{L} \\
=10 \mathrm{k} \| 3 \mathrm{k} \\
=\frac{10 \times 3 \times 10^{6}}{13 \times 10^{3}}=\frac{30}{13} \times 10^{3}=2.3 \mathrm{k} \Omega \\
A_{v}=\frac{r_{L}}{r_{E}+\gamma_{e}^{1}}=\frac{2307}{1 \times 10^{3}+27}=2.246
\end{gathered}
$$

## Overall voltage gain

W.K.T the ratio of base to source voltage

$$
\begin{aligned}
\frac{V_{i n}}{V_{s}}=\frac{R_{i S}}{R_{s}+R_{i S}}= & \frac{21.62 \times 10^{3}}{100+21.62 \times 10^{3}}=\frac{21.62 \times 10^{3}}{21720}=0.99 \\
& \therefore \text { over all voltage gain } \\
A_{v s}= & A_{V} \times \frac{V_{\text {in }}}{V_{s}}=2.246 \times 0.99=2.235
\end{aligned}
$$

## Output voltage

$$
\begin{gathered}
V_{o}=A_{V S} \times V_{S}=2.235 \times 10 \mathrm{mV} \\
V_{o}=22.35 \mathrm{mV}
\end{gathered}
$$

## EnggTree.com

7. An NPN common emitter amplifier circuit has the following parameters: $h_{f e}=50, h_{i e}=1 \mathrm{~K} \Omega$ and $\mathbf{R}_{\mathbf{c}}=3 \mathrm{~K} \Omega$. Find the voltage gain of the amplifier. (April/May 2019)

$$
\begin{aligned}
& A_{V}=\frac{A_{I} R_{L}}{R_{i}} ; \quad A_{I}=-h_{f} ; \quad \quad R_{i}=h_{i e} ; R_{L}=R_{C} ; \\
& A_{I}=-50 ; \\
& R_{i}=1 K ; R_{L}=3 K ;
\end{aligned}
$$

$A_{V}=\frac{-50 \times 3 \times 10^{3}}{1 \times 10^{3}} ;$
$A_{V}=-150$
8. A common emitter amplifier has an input resistance $2.5 \mathrm{k} \Omega$ and voltage gain of 200.If the input signal voltage is 5 mV . Find the base current of the amplifier. (May 2017) (Nov/Dec 2017)
W.K.T
$\mathrm{i}_{\mathrm{b}}$-base current, $\mathrm{R}_{\mathrm{i}}=2.5 \mathrm{k} \Omega, \mathrm{V}_{\mathrm{s}}=5 \mathrm{mV}$
$2.5 \times 10^{-3}=\frac{V s}{i_{b}}=5 \times 10^{-3} / i_{b} \therefore \dot{b}=2 \times 10^{-6} A=2 \mu A$
9. For a certain D-MOSFET, $I_{\text {dss }}=10 \mathrm{~mA}$ and $V_{G S(o f f)}=-8 \mathrm{~V}$. check if it is an n-channel or p-channel device? Justify your answer. (Nov/Dec 2018)
Given that,
For a D-MOSFET,
Saturation currents, $\mathrm{I}_{\mathrm{DSS}}=10 \mathrm{Ma}$
Gate to source cut-off voltage, $\mathrm{V}_{\mathrm{GS}}$ (off) $=-8 \mathrm{~V}$
Since the D-MOSFET has negative $\mathrm{V}_{\mathrm{GS}}$ (off). The device is n-channel D-MOSFET.

1. Derive the expression for current gain, input impedance and voltage gain of a CE transistor Amplifier. (Nov/Dec 2016) (Apr/May 2018)

The ac equivalent circuit can be obtained by replacing all the capacitors and voltage sources by a short circuit.

## Characteristics of CE amplifier:

## A. Without Emitter Resistor

(1) It has good voltage gain with phase inversion i.e., the output voltage is $180^{\circ}$ out of phase with input.
(2) It also has good current gain, power gain and relatively high input and output impedance.


Fig. ac equivalent circuit of CE amplifier


Fig. h-parameter model of CE amplifier


Fig Approximate hybrid model of CE amplifier

The input impedance: $h_{i e}$ seen to be in series with $h_{r e} V_{0}$. For $C E$ circuit, $h_{r e}$ is normally a very small quantity. So that the voltage $\mathrm{h}_{\mathrm{re}} \mathrm{V}_{0}$ fed back from the output to the input circuit is much smaller than the voltage drop across $h_{i e}$.

$$
\mathrm{Z}_{\mathrm{i}}^{\prime}=\mathrm{R}_{\mathrm{B}} \| \mathrm{h}_{\mathrm{ie}} \quad \text { where } \mathrm{R}_{\mathrm{B}}=\mathrm{R}_{1} \| \mathrm{R}_{2}
$$

The output impedance: The output voltage variation have liitle effect upon the input of CE circuit, only the output half of the circuit need to be considered in determining the output impedance.

$$
\mathrm{Z}_{0}^{\prime}=\mathrm{R}_{\mathrm{C}} \frac{1}{h_{o e}}
$$



The voltage gain: $\mathrm{A}_{V}=\mathrm{V}_{0} / \mathrm{V}_{\mathrm{i}}$
w.к.т $\quad \mathrm{V}_{0}=-\mathrm{i}_{\mathrm{c}} \mathrm{R}_{\mathrm{c}} \quad \mathrm{V}_{\mathrm{i}}=\mathrm{i}_{\mathrm{b}} \mathrm{h}_{\mathrm{ie}}$

Where $h_{r e} V_{0}$ is assumed short circuited.

$$
\begin{aligned}
& \mathrm{i}_{\mathrm{c}}=\mathrm{h}_{\mathrm{fe}} \mathrm{i}_{\mathrm{b}} \\
& \mathrm{~A}_{\mathrm{V}}=-\left(\mathrm{h}_{\mathrm{fe}} \mathrm{R}_{\mathrm{C}}\right) / \mathrm{h}_{\mathrm{ie}}
\end{aligned}
$$

## Current Gain:

$$
\begin{aligned}
&=\frac{\mathrm{A}_{\mathrm{I}}=\mathrm{I}_{0} / \mathrm{I}_{\mathrm{i}}=\mathrm{i}_{\mathrm{c}} / \mathrm{I}_{\mathrm{i}}}{i_{b}} \cdot \frac{i b}{}=-\mathrm{h}_{\mathrm{fe}}^{\underline{i} \underline{b}} \\
& I_{i} \\
&=-\mathrm{h}_{\mathrm{fe}} \mathrm{R}_{\mathrm{B}} /\left(\mathrm{h}_{\mathrm{ie}}+\mathrm{R}_{\mathrm{B}}\right) \frac{i_{b}}{=} \mathrm{R}_{\mathrm{B}} /\left(\mathrm{h}_{\mathrm{ie}}+\mathrm{R}_{\mathrm{B}}\right) \\
&
\end{aligned}
$$

## B. With emitter resistor:

A common emitter amplifier with emitter resistor Re provides feedback and voltage gain stabilized in a CE amplifier But it reduces the gain.

To obtain h-parameter model of the circuit, we replace the transistor by its h-parameter model.


## Fig. CE amplifier with Emitter resistor



Fig. AC equivalent circuit of $\mathbf{C E}$ amplifier with Emitter resistor


Fig .h-parameter model of a CE amplifier with emitter resistor


Fig .Approximate Model
Assuming $\mathrm{h}_{\mathrm{re}}$ is very low, The input impedance

$$
\begin{aligned}
& \mathrm{Z}_{\mathrm{i}}^{\prime}=R_{B} \| \mathrm{Zi} \\
& \mathrm{Z}_{\mathrm{i}}=\mathrm{V}_{\mathrm{i}} / \mathrm{I}_{\mathrm{i}}=\mathrm{V}_{\mathrm{i}} / \mathrm{i}_{\mathrm{b}} \\
& \quad \mathrm{~V}_{\mathrm{i}}=\mathrm{h}_{\mathrm{ie}} \mathrm{i}_{\mathrm{b}}+\mathrm{i}_{\mathrm{e}} \mathrm{R}_{\mathrm{E}} \\
& \mathrm{i}_{\mathrm{e}}=\mathrm{i}_{\mathrm{b}}+\mathrm{h}_{\mathrm{fe}} \mathrm{i}_{\mathrm{b}}=\left(1+\mathrm{h}_{\mathrm{fe}}\right) \mathrm{i}_{\mathrm{b}}
\end{aligned} \quad \text { w.к. }\left(\mathrm{i}_{\mathrm{e}}=\mathrm{i}_{\mathrm{b}}+\mathrm{i}_{\mathrm{c}}\right)
$$

sub eq(2) in eq(1), $\quad V_{i}=i_{b}\left(h_{i e}+\left(1+h_{f e}\right) R_{E}\right)$

$$
\begin{aligned}
& \mathrm{Z}_{\mathrm{i}}=\mathrm{V}_{\mathrm{i}} / \mathrm{i}_{\mathrm{b}}=\mathrm{h}_{\mathrm{ie}}+\left(1+\mathrm{h}_{\mathrm{fe}}\right) \mathrm{R}_{\mathrm{E}} \cdots-\cdots-\cdots \\
& \mathrm{Z}_{\mathrm{i}}=R_{B} \| \mathrm{Zi} \\
& \quad=\mathrm{R}_{\mathrm{b}} \|\left(\mathrm{h}_{\mathrm{ie}}+\left(1+\mathrm{h}_{\mathrm{fe}}\right) \mathrm{R}_{\mathrm{E}}\right)
\end{aligned}
$$

Voltage Gain: $\mathrm{A}_{\mathrm{v}}=\mathrm{V}_{0} / \mathrm{V}_{\mathrm{i}}$----------------5

$$
\begin{align*}
& \mathrm{Vo}=\mathrm{I}_{\mathrm{L}} \mathrm{R}_{\mathrm{C}} \\
& =-\mathrm{i}_{\mathrm{c}} \mathrm{R}_{\mathrm{c}} \text { where }\left(\mathrm{i}_{\mathrm{c}}=\mathrm{h}_{\mathrm{fe}} \mathrm{i}_{\mathrm{b}}\right) \\
& =-\mathrm{h}_{\mathrm{fe}} \mathrm{i}_{\mathrm{b}} \mathrm{R}_{\mathrm{c}} \\
& \mathrm{~V}_{\mathrm{i}}=\mathrm{I}_{\mathrm{i}} \mathrm{Z}_{\mathrm{i}} \\
& =\mathrm{i}_{\mathrm{b}}\left(\mathrm{~h}_{\mathrm{ie}}+\left(1+\mathrm{h}_{\mathrm{fe}}\right) \mathrm{R}_{\mathrm{E}}\right)-----
\end{align*}
$$

Sub eq(6) and eq(6) in eq(4)

$$
\begin{aligned}
\mathrm{A}_{\mathrm{V}}= & V_{0} / \mathrm{V}_{\mathrm{i}}=-\mathrm{h}_{\mathrm{fe}} \mathrm{R}_{\mathrm{C}} \mathrm{i}_{\mathrm{b}} /\left(h_{\mathrm{ie}}+\left(1+\mathrm{h}_{\mathrm{fe}}\right) \mathrm{R}_{\mathrm{E}}\right) \mathrm{i}_{\mathrm{b}} \\
& =-\mathrm{h}_{\mathrm{fe}} \mathrm{R}_{\mathrm{C}} / h_{\mathrm{ie}}\left(1+\mathrm{h}_{\mathrm{fe}}\right) \mathrm{R}_{\mathrm{E}}-\cdots-\cdots--\cdots--\cdots
\end{aligned}
$$


Since $\mathrm{h}_{\mathrm{fe}} \gg 1 \mathrm{~A}_{\mathrm{v}}=-\mathrm{R}_{\mathrm{C}} / \mathrm{R}_{\mathrm{E}}$
Output impedance: $\mathrm{Z}_{0}=\mathrm{R}_{\mathrm{C}}$ $\qquad$
Current gain:The current gain is defined as the ratio of output current to input current

$$
\mathrm{A}_{\mathrm{I}}=\mathrm{I}_{0} / \mathrm{I}_{\mathrm{i}}=\mathrm{I}_{0} / \mathrm{i}_{\mathrm{b}} \cdot \mathrm{i}_{\mathrm{b}} / \mathrm{I}_{\mathrm{i}}
$$

$$
\mathrm{I}_{0}=-\mathrm{i}_{\mathrm{c}}
$$

$$
\begin{equation*}
\mathrm{A}_{\mathrm{I}}=-\mathrm{h}_{\mathrm{fe}} \mathrm{i}_{\mathrm{b}} / \mathrm{I}_{\mathrm{i}} \tag{11}
\end{equation*}
$$

using voltage divider rule, $I_{b} / I_{i}=R_{B} / R_{B}+Z_{i}$

$$
\mathrm{A}_{\mathrm{I}}=-\mathrm{h}_{\mathrm{fe}} \mathrm{R}_{\mathrm{B}} / \mathrm{R}_{\mathrm{B}}+\mathrm{Z}_{\mathrm{i}}-\cdots---------------12
$$

## Application:

It is used as voltage amplifier, among the three basic amplifier configuration CE amplifier most frequently used.
2. Derive the expression for current gain, input impedance and voltage gain of a CC transistor Amplifier. This circuit is also known as emitter follower amplifier because its voltage gain is close to unity. Hence a change in base voltage appears as an equal change across the load.

## Characteristics of CC amplifier:

(1) CC amplifier provide current gain and power gain. but no voltage gain.
(2) It has high input impedance and very low output impedance.


Fig. Common collector amplifier


Fig. ac equivalent of CC amplifier


Fig .h-parameter model of a CC amplifier
The input impedance: $\mathrm{Z}_{\mathrm{i}}{ }^{\prime}=\mathrm{Zi} \| R_{B--------------------1} 1$

$$
\begin{aligned}
& \mathrm{Z}_{\mathrm{i}}=\mathrm{V}_{\mathrm{i}} / \mathrm{i}_{\mathrm{b}} \quad \text { EnggTree.com } \\
& \mathrm{V}_{\mathrm{i}}=\mathrm{h}_{\mathrm{ie}} \mathrm{i}_{\mathrm{b}}+\mathrm{I}_{\mathrm{e}} \mathrm{R}_{\mathrm{E}}------2_{\text {w.K. } . ~} \mathrm{i}_{\mathrm{e}}=\left(1+\mathrm{h}_{\mathrm{fe}}\right) \mathrm{i}_{\mathrm{b}}
\end{aligned}
$$

sub eq(2) in eq(1), $\quad V_{i}=i_{b}\left(h_{i e}+\left(1+h_{f e}\right) R_{E}\right)$

$$
\begin{aligned}
& \mathrm{Z}_{\mathrm{i}}=\mathrm{V}_{\mathrm{i}} / \mathrm{i}_{\mathrm{b}}=\mathrm{h}_{\mathrm{ie}}+\left(1+\mathrm{h}_{\mathrm{fe}}\right) \mathrm{R}_{\mathrm{E}}-\cdots--\cdots--3 \\
& \mathrm{Z}_{\mathrm{i}}^{\prime}=R_{B} \| \mathrm{Zi}
\end{aligned}
$$

Current gain: The current gain is defined as the ratio of output current to input current

$\mathrm{A}_{\mathrm{I}}=\mathrm{i}_{\mathrm{e}} / \mathrm{I}_{\mathrm{i}}=\mathrm{I}_{\mathrm{e}} / \mathrm{i}_{\mathrm{b}} . \mathrm{i}_{\mathrm{b}} / \mathrm{I}_{\mathrm{iW.K.T}} \mathrm{i}_{\mathrm{e}}=\left(1+\mathrm{h}_{\text {fe }}\right) \mathrm{i}_{\mathrm{b}}$

$$
\begin{aligned}
& \mathrm{A}_{\mathrm{I}}=-\left(1+\mathrm{h}_{\mathrm{fe}}\right) \mathrm{i}_{\mathrm{b}} / \mathrm{i}_{\mathrm{b}} \cdot \mathrm{i}_{\mathrm{b}} / \mathrm{I}_{\mathrm{i}} \\
& \mathrm{~A}_{\mathrm{I}}=-\left(1+\mathrm{h}_{\mathrm{fe}}\right) \cdot \mathrm{R}_{\mathrm{B}} / \mathrm{R}_{\mathrm{B}}+\mathrm{Z}_{\mathrm{i}} .
\end{aligned}
$$

Voltage Gain: $\mathrm{A}_{\mathrm{v}}=\mathrm{V}_{0} / \mathrm{V}_{\mathrm{i}}----------------4$

$$
\begin{aligned}
& V o=i_{e} R_{E} \\
& A_{v}=-i_{e} R_{E} / V_{i}
\end{aligned}
$$

The input voltage $\mathrm{V}_{\mathrm{i}}=\mathrm{i}_{\mathrm{b}} \mathrm{Z}_{\mathrm{i}}$---------------6
Sub eq(3) in eq(6)

$$
\begin{aligned}
& =\mathrm{i}_{\mathrm{b}}\left(\mathrm{~h}_{\mathrm{ie}}+\left(1+\mathrm{h}_{\mathrm{fe}}\right) \mathrm{R}_{\mathrm{E}}-\cdots-\cdots---7\right. \\
& \mathrm{A}_{\mathrm{V}}=\mathrm{R}_{\mathrm{E}} \mathrm{i}_{\mathrm{e}} /\left(\mathrm{h}_{\mathrm{ie}}+\left(1+\mathrm{h}_{\mathrm{fe}}\right) \mathrm{R}_{\mathrm{E}}\right) \mathrm{i}_{\mathrm{bw.K.T}} \quad \mathrm{i}_{\mathrm{e}}=\left(1+\mathrm{h}_{\mathrm{fe}}\right) \mathrm{i}_{\mathrm{b}} \\
& \quad=-\left(1+\mathrm{h}_{\mathrm{f})} \mathrm{R}_{\mathrm{E}} / \mathrm{h}_{\mathrm{ie}}+\left(1+\mathrm{h}_{\mathrm{fe}}\right) \mathrm{R}_{\mathrm{E}}\right. \\
& \quad=\mathrm{h}_{\mathrm{ie}}+\left(1+\mathrm{h}_{\mathrm{fe}}\right) \mathrm{R}_{\mathrm{E}}-\mathrm{h}_{\mathrm{ie}} / \mathrm{h}_{\mathrm{ie}}+\left(1+\mathrm{h}_{\mathrm{fe}}\right) \mathrm{R}_{\mathrm{E}} \\
& \quad=1-\frac{h i e}{h_{i e}+\left(1+h_{f e}\right) R_{\mathrm{E}}}
\end{aligned}
$$

Since $\left(1+\mathrm{h}_{\mathrm{fe}}\right) \mathrm{R}_{\mathrm{E}} \gg \mathrm{h}_{\mathrm{ie}}$ and $\mathrm{h}_{\mathrm{fe}} \gg 1 \mathrm{~A}_{\mathrm{v}}=1-\frac{h_{i e}--\mathrm{e}}{h_{f e} R_{E}} \quad 9$
Output impedance: $\mathrm{Z}_{0}=\frac{\text { Shortcircitcurrentthroughoutputterminal }}{\text { open circuit voltage between output terminals }}$
Short circuit current through output terminali ${ }_{b}=\mathrm{V}_{\mathrm{s}} / \mathrm{h}_{\mathrm{ie}} \| \mathrm{R}_{\mathrm{B}}+\mathrm{R}_{\mathrm{S}}-----------10$
Open circuit voltage between output terminals $=\mathrm{V}_{\mathrm{s}}$

## Application:

(1) The voltage gain of emitter follower as unity, thus it is used as buffer amplifier.
(2) It is used as impedance matching network.

## 3. Derive the expression for current gain, ifprifirefacfer and voltage gain of a CB transistor Amplifier. (May/June2016)

In this circuit only a fraction of output voltage is feedback to input thus $h_{r e}$ is very small. Therefore $h_{r b} V_{0}$ can be neglected when deriving CB gain and impedance.

## Characteristics of CB amplifier:

Circuair diagram:

(1) This CB circuit provides voltage gain and power gain but no current gain.
(2) It has high output impedance and very low input impedance thus it is unsuitable for most voltage amplification.

a. Input impedance: After neglecting $\mathrm{h}_{\mathrm{rb}} \mathrm{V}_{0}$, The $\mathrm{Z}_{\mathrm{e}}$ is given by,

Apply KVL, $\mathrm{V}_{\mathrm{i}}=\mathrm{I}_{\mathrm{e}} \mathrm{h}_{\mathrm{ib}}+\mathrm{I}_{\mathrm{e}} \mathrm{R}_{\mathrm{B}}-\mathrm{I}_{\mathrm{e}} \mathrm{R}_{\mathrm{B}}=\mathrm{I}_{\mathrm{e}} \mathrm{h}_{\mathrm{ib}}+\mathrm{I}_{\mathrm{e}} \mathrm{R}_{\mathrm{B}}-\mathrm{I}_{\mathrm{E}} \mathrm{h}_{\mathrm{f}} \mathrm{R}_{\mathrm{B}}$

$$
\begin{aligned}
& \mathrm{I}_{C}=\mathrm{I}_{\mathrm{e}} \mathrm{~h}_{\mathrm{bb}}=\mathrm{I}_{\mathrm{e}}\left[\mathrm{~h}_{\mathrm{ib}}+\mathrm{R}_{\mathrm{B}}-\mathrm{h}_{\mathrm{fb}} \mathrm{R}_{\mathrm{B}}\right] \\
& \mathrm{Z}_{\mathrm{e}}=\mathrm{V}_{\mathrm{i}} / \mathrm{I}_{\mathrm{e}}=\mathrm{h}_{\mathrm{ib}}+\mathrm{R}_{\mathrm{B}}\left(1-\mathrm{h}_{\mathrm{fb}}\right)
\end{aligned}
$$

The actual impedance of the circuit is given by

$$
\mathrm{Z}_{\mathrm{i}}=\mathrm{Z}_{\mathrm{e}} \| \mathrm{R}_{\mathrm{e}} \ldots
$$

b. Output impedance: The output has very less impact on the input hence the output impedance can be taken as
$\mathrm{Z}_{\mathrm{e}} \cong 1 / \mathrm{h}_{\mathrm{ob}}$
The actual output impedance is given by, $\mathrm{Z}_{0}=\mathrm{R}_{\mathrm{C}} \| \mathrm{Z}_{\mathrm{C}} \cong \mathrm{R}_{\mathrm{C}}$
$\mathrm{R}_{\mathrm{C}}$ is usually much smaller than $1 / \mathrm{h}_{\mathrm{ob}}$, soothe circuit impedance is approximately equal to $\mathrm{R}_{\mathrm{C}}$.
c. Voltage Gain: it is given by $\mathrm{A}_{\mathrm{v}}=\mathrm{V}_{0} / \mathrm{V}_{\mathrm{i}}$ $\qquad$ . 4
$\mathrm{V}_{0}=\mathrm{I}_{\mathrm{C}}\left(\mathrm{R}_{\mathrm{C}} \| \mathrm{R}_{\mathrm{L}}\right)---------5$

$$
\begin{aligned}
& \mathrm{V}_{\mathrm{i}}=\mathrm{I}_{\mathrm{e}} \mathrm{~h}_{\mathrm{ib}}+\mathrm{I}_{\mathrm{e}} \mathrm{R}_{\mathrm{B}}-\mathrm{I}_{\mathrm{E}} \mathrm{~h}_{\mathrm{fb}} \mathrm{R}_{\mathrm{B}}=\mathrm{I}_{\mathrm{e}}\left[\mathrm{~h}_{\mathrm{ib}}+\mathrm{R}_{\mathrm{B}}\left(1-\mathrm{h}_{\mathrm{fb}}\right)\right] \\
& A_{v}=I_{C}\left(R_{C} \| R_{L}\right) / I_{e}\left[h_{i b}+R_{B}\left(1-h_{f b}\right)\right]--------6 \\
& A_{v}=h_{f b}\left(R_{C} \| R_{L}\right) / h_{\text {ib }}+R_{B}\left(1-h_{f b}\right)-----------7
\end{aligned}
$$

d. Current gain: The transfer current gain of the device is given by $\mathrm{h}_{\mathrm{fc}}=\mathrm{I}_{\mathrm{C}} / \mathrm{I}_{\mathrm{e}}$ 8

The signal current is divided between $\mathrm{R}_{\mathrm{E}}$ and $\mathrm{Z}_{\mathrm{e}}$, and the collector current divides between $\mathrm{R}_{\mathrm{C}}$ and $\mathrm{R}_{\mathrm{L}}$, giving a lower value of current gain.

$$
\begin{aligned}
& \quad \mathrm{I}_{\mathrm{L}}=\mathrm{I}_{\mathrm{C}} \mathrm{R}_{\mathrm{E}} / \mathrm{R}_{\mathrm{E}}+\mathrm{R}_{\mathrm{L}} \\
& =\mathrm{h}_{\mathrm{fc}} \mathrm{I}_{\mathrm{e}} \mathrm{R}_{\mathrm{E}} / \mathrm{R}_{\mathrm{E}}+\mathrm{R}_{\mathrm{L}} \quad \text { but } \mathrm{I}_{\mathrm{e}}=\mathrm{I}_{\mathrm{S}} \mathrm{R}_{\mathrm{B}} / \mathrm{R}_{\mathrm{B}}+\mathrm{Z}_{\mathrm{e}} \\
& \mathrm{~A}_{\mathrm{i}}=\mathrm{I}_{\mathrm{L}} / \mathrm{I}_{\mathrm{S}}=\mathrm{h}_{\mathrm{f}_{\mathrm{c}} \mathrm{R}_{\mathrm{E}} \mathrm{R}_{\mathrm{B}} /\left(\mathrm{R}_{\mathrm{B}}+\mathrm{Z}_{\mathrm{e}}\right)\left(\mathrm{R}_{\mathrm{C}}+\mathrm{R}_{\mathrm{L}} \mathrm{~L}\right)--------9}
\end{aligned}
$$

## e. Power Gain:

The Power gain is given by $A_{P T}=A_{V} * h_{f b}$
Where $A_{i}$ is significantly different from $h_{f b} A_{p}=A_{v} * A_{i} \ldots \ldots-11$

## f. Application:

It is used for very high frequency voltage amplifier.

## UNIT-IV MULTISTAGE AMPLIFIERS AND DIFFERENTIAL AMPLIFIER

## PART-A

## BIMOS cascade amplifier, Differential amplifier

1. What is a differential amplifier?

An amplifier, which is designed to give the difference between two input signals, is called the differential amplifier.
2. What is the function of a differential amplifier?

The function of a differential amplifier is to amplify the difference of two signal inputs, i.e., $V_{0}=A_{D}\left(V_{1}-V_{2}\right)$, where $\mathrm{A}_{\mathrm{D}}$ is the differential gain.
3. What is the differential-mode voltage gain of a differential amplifier?

It is given by

$$
A_{d}={ }_{\overline{2}}^{1}\left(A_{1}-A_{2}\right)
$$

4. What are the ideal values of $A_{d}$ and $A_{c}$ with reference to the differential amplifier?

Ideally, Ac should be zero and $\mathrm{A}_{\mathrm{d}}$ should be large, ideally infinite.
5. What are advantages of differential amplifier?

It has high gain and high CMRR.
6. List some applications of differential amplifiers?

Used in IC applications, AGC circuits and phase inverters.

## Common mode and Difference mode analysis

7. Define differential mode signals of a differential amplifier. (Nov/Dec 2018)

The differential mode signal is the difference between two input voltages. i.e.,

$$
\mathrm{V}_{\mathrm{d}}=\mathrm{V}_{1}-\mathrm{V}_{2}
$$

The differential mode input signal is zero when $\mathrm{V}_{1}=\mathrm{V}_{2}$
8. When two signals $V_{1}$ and $V_{2}$ are connected to the two inputs of a difference amplifier, define a difference signal $V_{d}$ and common-mode signal $V_{c}$
The difference signal $\mathrm{V}_{\mathrm{d}}$ is defined as the difference of the two signal inputs,

$$
\text { i.e., } \mathrm{V}_{\mathrm{d}}=\mathrm{V}_{1}-\mathrm{V}_{2}
$$

The common-mode signal $\mathrm{V}_{\mathrm{c}}$ is defined as the average of the two signals,
I.e., $\mathrm{V}_{\mathrm{c}}=\left(\mathrm{V}_{1}+\mathrm{V}_{2}\right)_{-}$
9. What is the common-mode gain $\mathrm{AC}_{\mathrm{C}}$ in terms of $\mathrm{A}_{1}$ and $\mathrm{A}_{2}$ ?

It is given by $A_{c}=A_{1}+A_{2}$
10. Define CMRR what its ideal value How to improve it. (Nov/Dec2015), (May/ June2016)(May 2017)

The common-mode rejection ratio (CMRR) of a differential amplifier is defined as the ratio of the differentialmode gain to common-mode gain.

$$
\mathrm{CMRR}=\frac{|\mathrm{Ad}|}{\left|\mathrm{A}_{\mathrm{c}}\right|}
$$

Ideal value of is Infinite.
The improve CMRR the following circuits are used
i) Current mirror circuit ii) Temperature compensation. iii) Differential amplifier with constant current bias.
11. Express CMRR in dB.

CMRR (dB) $=20 \log \mathrm{~A}_{\mathrm{d}}-20 \log \mathrm{~A}_{\mathrm{c}}$.
12. What is meant by tuned amplifiers? (A/M 2010)

Tuned amplifiers are amplifiers that are designed to reject a certain range of frequencies below a lower cut off frequency $\omega_{\mathrm{L}}$ and above a upper cut off frequency $\omega_{\mathrm{H}}$ and allows only a narrow band of frequencies.

## 13. Classify tuned amplifiers.

1. Single tuned amplifier.
2. Double tuned amplifier.
3. Synchronously tuned amplifier.
4. Stagger tuned amplifier.
5. What is the other name for tuned amplifier?

Tuned amplifiers used for amplifying narrow band of frequencies hence it is also known as "narrow band amplifier" or "Band pass amplifier.
15. What is the application of tuned amplifiers?(N/D 2007)

The application of tuned amplifiers to obtain a desired frequency and rejecting all other frequency in
(i). Radio and T.V broadcasting as tuning circuit.
(ii). Wireless communication system.
16. What are the advantages of tuned circuit?

- High selectivity
- Smaller collector supply voltage
- Small power gain.


## Neutralization methods

17. What is meant by neutralization? ( $\mathrm{N} / \mathrm{D}$ 2012)

It is the process by which feedback can be cancelled by introducing a current that is equal in magnitude but $180^{\circ}$ out of phase with the feedback signal at the input of the active device. The two signals will cancel and the effect of feedback will be eliminated. This technique is termed as neutralization.
18. What is the need for neutralization (Nov/Dec2015)

In turn RF amplifier at high frequency centered around a radio frequency the inter junction capacitance between base and collector $\mathrm{C}_{\mathrm{bc}}$ of the transistor becomes dominant i.e. its reactance become low enough to be considered. As reactance of $\mathrm{C}_{\mathrm{bc}}$ at RF is low enough it provides the feedback path from collector to base. If this feedback is positive the circuit is converted to an unstable one generating its own oscillations and can stop working as an amplifier. In order to prevent oscillations without redacting the stage gain neutralization is used in tuned amplifiers.
19. State the merits of using push-pull configuration. (May 2018) (Apr/May 2018)

- Efficiency is high. (78.5\%)
- Figure of merit is high.
- Distortion is less
- Ripple present in the output due to power supply is multiplied.

20. List the disadvantages of push-pull amplifier.

- Two identical transistors are needed.
- Centre taping is required in transformer.
- Transformers used are bulky and expensive.
- If the parameters of the two transistors differ, there will be unequal amplification of the two halves of signal which introduces more distortion.

In class A mode of means, the output current flows throughout the entire period of input cycle and the Q-point is chosen at the midpoint of A.C load line and biased.
22. Give two applications of class-C power amplifier.

- Used in radio and TV transmitters.
- Used to amplify the high frequency signals.
- Tuned amplifiers.

23. What is multistage amplifier?

Multistage cascading permits several single-stage amplifiers to be combined into one circuit. Multistage cascading can produce an amplifier with large gain, high input resistance and low output resistance. The smallsignal behavior of a multistage amplifier can be modeled by cascading an appropriate number of small-signal two-port amplifier models.
24. A multistage amplifier employs five stages each of which has a power gain of 30 . What is the total gain of the amplifier in dB. (Nov/Dec 2018)
Given that,
The power gain of each stage in a five-stage amplifier is,

$$
\mathrm{A}_{\mathrm{V}_{\mathrm{n}}}=30, \mathrm{n}=1 \text { to } 5
$$

## Total gain, $\mathrm{Av}_{\mathrm{v}}=$ ?

The overall gain, $\mathrm{A}_{v}$ of an n -stage amplifier is given as,

$$
A_{v}=A_{v_{1}} X A_{v_{2}} X A_{v_{3}} X \ldots . . . A_{v_{n}}
$$

Here, $\mathrm{n}=5$

$$
\begin{aligned}
\mathrm{A}_{\mathrm{v}} & =\mathrm{A}_{\mathrm{v} 1} \times \mathrm{A}_{\mathrm{v} 2} \times \mathrm{A}_{\mathrm{v} 3} \times \mathrm{A}_{\mathrm{v} 4} \times \mathrm{A}_{\mathrm{v}} \\
& =30 \times 30 \times 30 \times 30 \times 30 \\
\mathrm{~A}_{\mathrm{v}} & =243 \times 10^{5} \\
\text { Total gain, } \mathrm{A}_{\mathrm{v}} & =243 \times 10^{5}
\end{aligned}
$$

$$
A v=147.71 \mathrm{~dB}
$$

25. CMRR of an amplifier is 100 dB , calculate common mode gain if the differential gain is $\mathbf{1 0 0 0}$ (Nov/Dec 2016)
$\mathrm{CMRR}=\mathrm{A}_{\mathrm{d}} / \mathrm{A}_{\mathrm{C}}, 100=1000 / \mathrm{A}_{\mathrm{c}}, \mathrm{A}_{\mathrm{c}}=10$
26. Define conversion efficiency of power amplifier? (Nov/Dec 2016)

It is a measure of an active device in converting the d.c power of the supply into the ac power delivered to load. It is also referred theoretical efficiency or collector circuit efficiency

- Mathematically, collector circuit efficiency,

$$
\eta_{c}=\frac{\text { a.c.power delivered to the load }}{\text { power supplied by the d.c.source to output circuit }}
$$

27. A tuned circuit has a resonant frequency of 1600 KHz and a bandwidth of 10 KHz . What is the value of its $Q$ factor? (May 2017)

$$
\mathrm{Q}_{\text {factor }}=\frac{\text { resonant frequency }}{\text { bandwidth }}=\frac{1600}{10}=160
$$

28. What is thermal runaway? (Nov/Dec 2017)

Thermal runaway occurs in situations where an increase in temperature changes the conditions in a way that causes a further increase in temperature, often leading to a destructive result. It is a kind of uncontrolled positive feedback.

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29. Compare the characteristics of CE, CB, CC amplifiers (May/June 2016) (Nov/Dec 2017)
30. 

| S.No | Common Emitter Amplifier | Common Base Amplifier | Common Collector <br> Amplifier |
| :---: | :--- | :--- | :--- |
| 1 | In this case emitter is <br> common to both input and <br> output | In this case base is common <br> to both input and output | In this case collector is <br> common to both input <br> and output |
| 2 | $180^{0}$ phase shift occurs | No phase shift occurs | No phase shift occurs |
| 3 | Input impedance: Low | Very low | Very high |
| 4 | Output impedance: High | Very high | Low |

31. A multistage amplifier employs five stages each of which has a power gain of 30 . What is the total gain of the amplifier in dB? (Nov/Dec 2017)
Solution:
Absolute gain of each stage $=30 \quad$ No. of stages $=5$
Power gain of one stage in $\mathrm{dB}=10 \log 1030=14.77$
$\therefore$ Total power gain $=5 \times 14.77=73.85 \mathrm{~dB}$
32. What is cross over distortion? (Apr/May 2018)

Crossover distortion is the term given to a type of distortion that occurs in push-pull class $A B$ or class $B$ amplifiers. It happens during the time that one side of the output stage shuts off, and the other turns on.
33. Determine the input impedance of a differential amplifier (emitter coupled) with $R_{B}=3.9 \mathrm{~K} \Omega$ and $\mathbf{Z}_{\mathrm{B}}=\mathbf{2 . 4}$ K $\Omega$. (April/May 2019)

$$
\begin{aligned}
Z_{i}= & R_{B} \| Z_{B} \\
Z_{i}= & \frac{R_{\underline{B}} \times Z_{\underline{B}}}{R_{B}+Z_{B}} \\
Z_{i} & =\frac{3.9 \times 10^{3} \times 2.4 \times 10^{3}}{3.9 \times 10^{3}+2.4 \times 10^{3}}
\end{aligned}
$$

The input impedance of a differential amplifier (emitter coupled), $Z_{i}=1.49 \Omega$
34. A single tuned amplifier provides a band width of 10 KHz at a frequency of 1 MHz . Find the circuit $Q$. (April/May 2019)

$$
\begin{aligned}
f_{O} & =B W \times Q_{O} \\
Q_{O} & =\frac{f_{0}}{B W} \\
Q_{O} & =\frac{1 \times 10^{6}}{10 \times 10^{3}}
\end{aligned}
$$

$$
Q_{O}=100
$$

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## BIMOS cascade amplifier, Differential amplifier

1. Explain the operation of cascade amplifier.

- The cascade amplifier consists of a common emitter amplifier stage in series with a common base amplifier stage.
- It solves the low impedance problem of a common base circuit.
- It gives the high input impedance of a CE amplifier as well as good voltage gain and high frequency response of CB circuit.
- For DC bias $\mathrm{I}_{\mathrm{C} 1}=\mathrm{I}_{\mathrm{E} 1}, \mathrm{I}_{\mathrm{E} 2}=\mathrm{I}_{\mathrm{C} 1}$

- Ac equivalent circuit for cascade amplifier is drawn by shorting dc supply and capacitors.

- A simplified h parameter equivalent circuits for cascade amplifier is drawn by replacing transistor with their equivalents


Analysis of second stage (CB)
a) Current gain $\left(\mathrm{A}_{\mathrm{i} 2}\right)$

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$$
\mathrm{A}_{\mathrm{i} 2}=\frac{\mathrm{h}_{\mathrm{fe}}}{1+\mathrm{h}_{\mathrm{fe}}}
$$

b) Input resistance $\left(\mathrm{R}_{\mathrm{i} 2}\right)$

$$
\mathrm{R}_{\mathrm{i} 2}=\frac{\mathrm{h}_{\mathrm{ie}}}{1+\mathrm{h}_{\mathrm{fe}}}
$$

c) Voltage gain $\left(\mathrm{A}_{\mathrm{v} 2}\right)$

$$
A_{v 2}=\frac{A_{i 2} R_{\mathrm{L} 2}}{\mathrm{R}_{\mathrm{i} 2}}
$$

Analysis of first stage (CE)
a) Current gain $\left(\mathrm{A}_{i 1}\right)$

$$
\mathrm{A}_{\mathrm{i} 1}=-\mathrm{hfe}
$$

b) Input resistance $\left(\mathrm{R}_{\mathrm{i} 1}\right)$

$$
\mathrm{R}_{\mathrm{i} 1}=\text { hie }
$$

c) Voltage gain $\left(\mathrm{A}_{\mathrm{v} 1}\right)$

$$
A_{v 1}=\frac{A_{i 1} R_{L 1}}{R_{i 1}}
$$

## 2. BIMOS cascade amplifier (or coupling amplifier):

* To get faithful amplification, amplifier should have desired voltage gain, current gain and it should match its input impedance with the connected source impedance. Similarly, output impedance must match with the load impedance.
* Normally, these requirements of the amplifier cannot be obtained in a single stage amplifier, which is due to the limitation of the parameters of transistor or FET or whatever device used.
* Under these situations, more than one amplifier stages are cascaded such that input and output stages provide impedance matching requirements with some amplification and remaining middle stages provide most of the amplification.

Therefore, for making cascading following reasons,

* The amplification of a single stage amplifier is not sufficient.
* When input and output impedance is not of the correct magnitude, for a particular application two or more amplifier stages are connected in cascaded fashion or coupling. This is known as multistage amplifier.


Figure: Block diagram of cascade amplifier

From the above figure, $V_{i 1}, V_{i 2}, V_{i 3}$ the input ofinggspeed cobthird stages and $V_{o 1,}, V_{o 2}, V_{o 3}$ are the output of the three stages. Therefore, $\frac{V o 3}{V_{i 1}}$ is the overall voltage gain of 3 stage amplifier which is given as follows:

$$
\begin{align*}
A_{v} & =\frac{V_{03}}{V_{i 1}}  \tag{1}\\
& =\frac{V_{03}}{V_{i 3}} \cdot \frac{V_{i 3}}{V_{i 2}} \cdot \frac{V_{i 2}}{V_{i 1}} \tag{2}
\end{align*}
$$

From the figure, we know that,
$V_{o 1}=V_{i 2} ; V_{o 2}=V_{i 3}$; put this into the above equation, we get

$$
\begin{equation*}
A_{v}=\frac{V_{03}}{V_{i 3}} \cdot \frac{V_{o 2}}{V_{i 2}} \cdot \frac{V_{o 1}}{V_{i 1}} \tag{3}
\end{equation*}
$$

Already we know that,

$$
\text { Voltage gain }(\mathrm{A})=\frac{\text { output voltage }}{\text { Input voltage }}=\frac{V_{o}}{V_{i}}
$$

$$
\begin{equation*}
A_{v}=A_{v 3} . A_{v 2} . A_{v 1} \tag{4}
\end{equation*}
$$

Therefore, the voltage gain of multistage amplifier is the product of individual gains of the each stage. Then the multistage amplifier is shown below.


Figure: Multistage amplifier
Voltage gain: The resultant voltage gain of the multistage amplifier is the product of the voltage gains of the various stages or individual stages.

$$
\begin{equation*}
\text { (i.e.,) } \quad A_{v}==A_{v 1} \cdot A_{v 2} \cdot A_{v 3} \cdot A_{v 4} \cdot \ldots \ldots . A_{v n \text {. }} \tag{5}
\end{equation*}
$$

$=$ Then, Voltage gain of $n^{\text {th }}$ stage is as follows:

$$
\begin{equation*}
A_{v 1}=\frac{A_{i n} R_{l n}}{R_{i n}} . \tag{6}
\end{equation*}
$$

Where, $R_{l n}=$ Effective load resistance of $n^{\text {th }}$ stage.
$R_{i n}=$ Input resistance / impedance of $1^{\text {st }}$ stage.

## Selection of cascading amplifier configuration:

From the above discussion, the multistage amplifier is divided into three parts:
i) Input stage
ii) Middle stage and
iii) Output stage.

* In the above, the input stage must be designed with input impedance matches with the source impedance.
* Similarly, the output stage designed must be the output impedance matches with the load impedance.
* Then, middle stage is designed with our desired voltage and current gain.

Anyhow, to select the cascading configuration, the following considerations are important since we normally use these three configurations.

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## Common mode and Difference mode analysis

3. Draw the circuit diagram and explain the working of a differential amplifier using FET. Derive the expression for differential mode gain and common mode gain.(May 2017)

- Normally, analysis in amplifier depends on both AC and DC analysis.
- In the above two, the d.c signals determines the operating values for the transistors and used as biasing.
- Similarly, a.c signals are used as input signals, which determine the output of the differential amplifier.
- The dual input, balanced output differential amplifier is also called Symmetrical Differential Amplifier.


## * DC ANALYSIS:

- DC analysis means using D.c voltage as biasing voltage and keeping it constant (to obtain suitable operating point).


## * AC ANALYSIS:

- For performing AC analysis, we must apply AC input signals as an input. So, we can calculate the following:
A. Differential mode gain $\left(\mathrm{A}_{\mathrm{d}}\right)$.
B. Common mode gain $\left(\mathrm{A}_{\mathrm{c}}\right)$.
C. Input resistance ( $\mathrm{R}_{\mathrm{i}}$ ).
D. Output resistance $\left(\mathrm{R}_{\mathrm{o}}\right)$.

The above can be obtained by using h-parameters.

## A. Differential gain ( $\mathbf{A}_{d}$ )

- To obtain the Differential mode gain, the two input signals must be different from each other.
- Here, we take the two a.c input signals as equal in magnitude but having $180^{\circ}$ phase shift between them.
- Then, the magnitude of each a.c input voltage $\mathrm{V}_{\mathrm{S} 1}$ and $\mathrm{V}_{\mathrm{S} 2}$ is $\frac{\mathrm{V}_{\mathrm{s}}}{2}$.
- For the a.c purposes, emitter terminal can be grounded which is shown in figure below with small signal analysis.



## Figure (1): AC Equivalent for differential operation (half circuit concept)

- The circuit which can be analyzed by considering only one transistor is called Half circuit concept of analysis.


Figure(2): Approximate hybrid model
 apply the Kirchhoff's voltage law in input side,

$$
\begin{array}{r}
\frac{\mathrm{v}_{\mathrm{S}}}{2}=\mathrm{i}_{\mathrm{b}} \mathrm{R}_{\mathrm{S}}+\mathrm{i}_{\mathrm{b}} \mathrm{~h}_{\mathrm{ie}} \\
\frac{\mathrm{v}_{\mathrm{S}}}{2}=\mathrm{i}_{\mathrm{b}}\left(\mathrm{Rs}+\mathrm{h}_{\mathrm{ie}}\right) \quad \ldots \ldots  \tag{2}\\
\mathrm{i}_{\mathrm{b}}=\frac{\mathrm{V}_{\mathrm{S}}}{2\left(\mathrm{R}_{\mathrm{S}}+\mathrm{h}_{\mathrm{ie}}\right)} \quad \ldots \ldots \ldots .
\end{array}
$$

- Similarly, applying the Kirchhoff's voltage law to output loop, we get

$$
\begin{equation*}
\mathrm{V}_{\mathrm{o}}=-\mathrm{I}_{\mathrm{b}} \mathrm{~h}_{\mathrm{fe}} \cdot \mathrm{R}_{\mathrm{C}} . \tag{4}
\end{equation*}
$$

- Put the value of $\mathrm{I}_{\mathrm{b}}$ in equation (4) from (3), we get,

$$
\begin{equation*}
\mathrm{V}_{\mathrm{o}}=\frac{-\mathrm{h}_{\mathrm{fe}} V_{\mathrm{s}} \mathrm{Re}_{\mathrm{c}}}{2\left(\mathrm{R}_{\mathrm{S}}+\mathrm{h}_{\mathrm{ie}}\right)} \ldots \ldots . \tag{5}
\end{equation*}
$$

- Then,,$\underline{\mathrm{V}_{\mathrm{o}}}=\frac{-\mathrm{h}_{\mathrm{Fe}} \cdot \mathrm{R}_{\mathrm{C}}}{2\left(\mathrm{R}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ie}}\right)}$
- Negative sign indicates that $180^{\circ}$ phase difference between input and output. If the input signals are equal and are out of phase by $180^{\circ}$, we get
- Differential mode signal $\mathrm{V}_{\mathrm{d}}=\mathrm{V}_{1}-\mathrm{V}_{2}=\left(\frac{\mathrm{V}_{\mathrm{S}}}{2}\right)-\left(-\frac{\mathrm{V}_{\mathrm{S}}}{2}\right)=\mathrm{V}_{\mathrm{S}}$

Where, $\mathrm{V}_{\text {sis }}$ differential input voltage.

- Differential voltage gain $A_{d}=\frac{V_{0}}{V_{s}}$

$$
\mathrm{A}_{\mathrm{d}}=\frac{\mathrm{w}_{\mathrm{fe}} \mathrm{R}_{\mathrm{G}} \text { Tree....... }}{2\left(\mathrm{R}_{\mathrm{S}}+\mathrm{h}_{\mathrm{ie}}\right)} \ldots \ldots .
$$

- When the output of differential amplifier is measured with reference to ground, it is called unbalanced output.
- The output across the collectors of $Q_{1}$ and $Q_{2}$ to be perfectly matched then $A_{d}$ for balanced output is twice than that of $\mathrm{A}_{\mathrm{d}}$ for unbalanced output. Therefore

$$
\begin{equation*}
\mathrm{A}_{\mathrm{d}}=\frac{\mathrm{h}_{\mathrm{fe}} \mathrm{R}_{\mathrm{C}}}{\left(\mathrm{R}_{\mathrm{S}}+\mathrm{h}_{\mathrm{ie}}\right)} \ldots \ldots \ldots \ldots \ldots \ldots \tag{9}
\end{equation*}
$$

## B. Common mode gain (Ac)

- In common mode, the both transistor's input magnitude and phases are also inphase with each other.
- Let us assume that input signals are having the same magnitude $\mathrm{V}_{\mathrm{s}}$ and are in same phase.
- Common mode voltage $\mathrm{V}_{\mathrm{C}}=\frac{\mathrm{V}_{1}+\mathrm{V}_{2}}{2}=\frac{\mathrm{V}_{\mathrm{S}}+\mathrm{V}_{\mathrm{S}}}{2}=\mathrm{V}_{\mathrm{S}}$ $\qquad$
- If suppose, the output is expressed as, $\mathrm{V}_{\mathrm{o}}=\mathrm{A}_{\mathrm{C}} . \mathrm{V}_{\mathrm{S}}$
- Common mode gain $A_{C}=\frac{v_{0}}{V_{S}}$
- In this mode, both the emitter current $\mathrm{I}_{\mathrm{e} 1}=\mathrm{I}_{\mathrm{e} 2}=\mathrm{I}_{\mathrm{e}}$ of $\mathrm{TQ}_{1}, \mathrm{TQ}_{2}$ flows through $\mathrm{R}_{\mathrm{E}}$ in the same direction, with same magnitude.
- Hence, the total current flowingthTred. Boinnearly $2 \mathrm{I}_{\mathrm{e}}$


Figure(1): A.C. Equivalent Circuit for Common Mode Configuration

- Then the approximate hybrid model for the above circuit can be obtained and is used to obtain the $\mathrm{A}_{\mathrm{d}}$.


Figure(2): Approximate Hybrid model

- As the current through $\mathrm{R}_{\mathrm{E}}$ is $2 \mathrm{I}_{\mathrm{e}}$, for simplicity of derivation, we have to assume the $\mathrm{I}_{\mathrm{e}}$ and effective emitter resistance as $2 \mathrm{R}_{\mathrm{E}}$.
- Current through $\mathrm{R}_{\mathrm{C}}=$ Load current $\mathrm{I}_{\mathrm{L}}$
- Effective emitter $=2 \mathrm{R}_{\mathrm{E}}$
- Current through emitter resistance $=\mathrm{I}_{\mathrm{L}}+\mathrm{I}_{\mathrm{b}}$
- Current through $\mathrm{h}_{\mathrm{oe}}=\left(\mathrm{I}_{\mathrm{L}}-\mathrm{h}_{\mathrm{fe}} . \mathrm{I}_{\mathrm{b}}\right)$
- Now, applying Kirchhoff's voltage law to input side,


Figure (3): Input side

$$
\begin{align*}
& -\mathrm{I}_{\mathrm{b}} \mathrm{R}_{\mathrm{S}}+\mathrm{I}_{\mathrm{b}} \mathrm{~h}_{\mathrm{ie}}+2 \mathrm{R}_{\mathrm{E}}\left(\mathrm{I}_{\mathrm{L}}+\mathrm{I}_{\mathrm{b}}\right)=-\mathrm{V}_{\mathrm{S}} \\
& \mathrm{I}_{\mathrm{b}} \mathrm{R}_{\mathrm{S}} \mathrm{I}_{\mathrm{b}} \mathrm{he}_{\mathrm{ie}}-2 \mathrm{R}_{\mathrm{E}}\left(\mathrm{I}_{\mathrm{L}}+\mathrm{I}_{\mathrm{b}}\right)=\mathrm{V}_{\mathrm{S}}^{\ldots} \ldots  \tag{15}\\
& \text { While, } \quad \mathrm{V}_{\mathrm{o}}=-\mathrm{I}_{\mathrm{L}} . \mathrm{R}_{\mathrm{C}} \ldots \ldots \tag{15a}
\end{align*}
$$

$\qquad$

- Negative sign is due to the assumed direction of current. Similarly apply KVL to output side.

$$
\begin{equation*}
\frac{-\left(\mathrm{I}_{\mathrm{L}}-\mathrm{h}_{\mathrm{F}} \mathrm{C}_{\mathrm{L}}^{\mathrm{L}}\right)}{\mathrm{h}_{\mathrm{oe}}}-2 \mathrm{R}_{\mathrm{E}}\left(\mathrm{I}_{\mathrm{L}}+\mathrm{I}_{\mathrm{b}}\right)-\mathrm{ILR}_{\mathrm{L}}=0 . \tag{16}
\end{equation*}
$$



$$
\begin{equation*}
\mathrm{I}_{\mathrm{b}}\left[\frac{\mathrm{~h}_{\mathrm{he}}}{\mathrm{~h}_{\mathrm{oe}}}-2 \mathrm{R}_{\mathrm{E}}\right]=\mathrm{I}_{\mathrm{L}}\left[\frac{1}{\mathrm{~h}_{\mathrm{oe}}}+2 \mathrm{R}_{\mathrm{E}}+\mathrm{R}_{\mathrm{C}}\right] \tag{18}
\end{equation*}
$$



Figure (4): Output side

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- Multiplying both sides by $h_{o e}$, then

$$
\begin{align*}
& \mathrm{I}_{\mathrm{b}}\left[\mathrm{~h}_{\mathrm{fe}}-2 \mathrm{R}_{\mathrm{E}} \mathrm{~h}_{\mathrm{oe}}\right]=\mathrm{I}_{\mathrm{L}}\left[1+\mathrm{h}_{\mathrm{oe}}\left(2 \mathrm{R}_{\mathrm{E}}+\mathrm{R}_{\mathrm{C}}\right)\right]  \tag{19}\\
& \frac{\mathrm{I}_{\mathrm{L}}}{\mathrm{I}_{\mathrm{b}}}=\frac{\left[\mathrm{h}_{\mathrm{fe}}-2 \mathrm{R}_{\mathrm{E}} \mathrm{~h}_{\mathrm{oe}}\right]}{\left[1+\mathrm{h}_{\mathrm{oe}}\left(2 \mathrm{R}_{\mathrm{E}}+\mathrm{R}_{\mathrm{c}}\right)\right]} .  \tag{20}\\
& \mathrm{I}_{\mathrm{b}}=\frac{\mathrm{L}\left[1+\mathrm{h}_{\mathrm{oe}}\left(2 \mathrm{REE}_{\mathrm{E}}+\mathrm{Rc}\right)\right]}{\left[\mathrm{h}_{\mathrm{Fe}}-2 \mathrm{RE}_{\mathrm{o}} \mathrm{e}\right]} \tag{21}
\end{align*}
$$

$\qquad$

- Putting this Ib in equation (15),

$$
\begin{array}{r}
\mathrm{V}_{\mathrm{S}}=\frac{\mathrm{I}_{\mathrm{L}}\left[1+\mathrm{h}_{\mathrm{oe}}\left(2 \mathrm{R}_{\mathrm{E}}+\mathrm{R}_{\mathrm{C}}\right)\right]\left[\mathrm{R}_{\mathrm{S}}+\mathrm{h}_{\mathrm{ie}}+2 \mathrm{R}_{\mathrm{E}}\right]+2 \mathrm{R}_{\mathrm{E}}}{\left[\mathrm{~h}_{\mathrm{fe}}-2 \mathrm{R}_{\mathrm{E}} \mathrm{~h}_{\mathrm{oe}}\right]} \\
\frac{\mathrm{V}_{\mathrm{S}}}{\mathrm{I}_{\mathrm{L}}}=\frac{\left[1+\mathrm{h}_{\mathrm{oe}}\left(2 \mathrm{R}_{\mathrm{E}}+\mathrm{R}_{\mathrm{c}}\right)\right]\left[\mathrm{R}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ie}}+2 \mathrm{R}_{\mathrm{E}}\right]+2 \mathrm{R}_{\mathrm{E}}}{\left[\mathrm{~h}_{\mathrm{fe}}-2 \mathrm{R}_{\mathrm{E}} \mathrm{~h}_{\mathrm{oe}}\right]} \ldots \text { (22) } \tag{22}
\end{array}
$$

- Then, find LCM and adjusting the terms,

$$
\begin{gathered}
\frac{V_{s}}{I_{L}}=\frac{2 R_{E}\left(1+h_{f e}\right)+R_{s}\left(1+2 R_{E} h_{o e}\right)+h_{i e}\left(1+2 R_{E} h_{o e}\right)+h_{o e} R_{C}\left(2 R_{E}+R_{s}+h_{o e}\right)}{\left[h_{f e}-2 R_{E} h_{o e}\right]} \\
\frac{V_{s}}{I_{L}}=\frac{2 R_{E}\left(1+h_{f e}\right)+\left(R_{s}+h_{i e}\right)\left(1+2 R_{E} h_{o e}\right)+h_{o e} R_{c}\left(2 R_{E}+R_{s}+h_{o e}\right)}{\left[h_{f e}-2 R_{E} h_{o e}\right]} \ldots(23)
\end{gathered}
$$

Actually $h_{o e} R_{c} \ll 1$. Neglecting the terms,

$$
\begin{align*}
& \frac{\mathrm{V}_{\mathrm{S}}}{\mathrm{I}_{\mathrm{L}}}=\frac{2 \mathrm{R}_{\mathrm{E}}\left(1+\mathrm{h}_{\mathrm{fe}}\right)+\left(\mathrm{R}_{\mathrm{S}}+\mathrm{h}_{\mathrm{ie}}\right)\left(1+2 \mathrm{R}_{\mathrm{E}} \mathrm{hee}\right)}{\left[\mathrm{h}_{\mathrm{fe}}-2 \mathrm{RE}_{\mathrm{E}} h_{\mathrm{oe}}\right]} .  \tag{24}\\
& \mathrm{I}_{\mathrm{L}}=\frac{\mathrm{V}_{\mathrm{S} .}\left[\mathrm{h}_{\mathrm{fe}}-2 \mathrm{R}_{\mathrm{E}} h_{o e}\right]}{2 \mathrm{R}_{\mathrm{E}}\left(1+\mathrm{h}_{\mathrm{fe}}\right)+\left(\mathrm{R}_{\mathrm{S}}+\mathrm{h}_{\mathrm{ie}}\right)\left(1+2 \mathrm{R}_{\mathrm{E}} h_{o e}\right)} . \tag{25}
\end{align*}
$$

Putting this $\mathrm{I}_{\mathrm{L}}$ in equation (15a),

$$
\begin{align*}
& \mathrm{V}_{\mathrm{o}}=-\mathrm{I}_{\mathrm{L}} \cdot \mathrm{R}_{\mathrm{C}} \tag{26}
\end{align*}
$$

Hence the common mode gain can be written as,

$$
\begin{equation*}
A_{c}=\frac{V_{o}}{V_{S}}=\frac{\left[2 R_{E} h_{o e}-h_{f e}\right] R_{c}}{2 R_{E}\left(1+h_{f e}\right)+\left(R_{s}+h_{i e}\right)\left(1+2 R_{E} h_{o e}\right)} \cdots \cdots . \tag{27}
\end{equation*}
$$

In practice, $h_{o e}$ is neglected, because the expression for $\mathrm{Ac}_{\mathrm{c}}$ can be further modified as,

$$
\begin{equation*}
\mathrm{A}_{\mathrm{C}}=\frac{-\mathrm{h}_{\mathrm{fe}} \mathrm{R}_{\mathrm{C}}}{\mathrm{R}_{\mathrm{S}}+\mathrm{h}_{\mathrm{ie}}+2 \mathrm{R}_{\mathrm{E}}\left(1+\mathrm{h}_{\mathrm{fe}}\right)} \tag{28}
\end{equation*}
$$

The above expression is same whether the output is balanced or unbalanced.

## COMMON MODE REJECTION RATIO (CMRR):

$$
\mathrm{CMRR}=\left|\frac{\mathrm{A}_{\mathrm{d}}}{\mathrm{~A}_{\mathrm{C}}}\right|
$$

From equation (8) and (28),

$$
\begin{equation*}
\mathrm{CMRR}=\left|\frac{2 \frac{\frac{\mathrm{~h}}{\mathrm{Fe}} \mathrm{R}_{\mathrm{C}}}{\left(\mathrm{R}_{\mathrm{S}}^{+\mathrm{h}_{\mathrm{ie}}}\right)}}{\frac{\mathrm{h}_{F \mathrm{e}} \mathrm{R}_{\mathrm{C}}}{\left(\mathrm{R}_{\mathrm{S}}+\mathrm{h}_{\mathrm{ie}}+2 \mathrm{R}_{\mathrm{E}}\left(1+\mathrm{h}_{F \mathrm{e}}\right)\right.}}\right| \ldots \ldots \tag{29}
\end{equation*}
$$

This is CMRR for dual input balanced output differential amplifier circuit.
For balanced case,

$$
\mathrm{CMRR}=\left|\frac{\left(\mathrm{Rs}+\mathrm{h}_{\mathrm{ie}}+2 \mathrm{Re}_{\mathrm{E}}\left(1+\mathrm{hfe}_{\mathrm{fe}}\right)\right.}{\left(\mathrm{Rs}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ie}}\right)}\right|
$$

For unbalanced case,

$$
\mathrm{CMRR}=\left|\frac{\left(\mathrm{R}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ie}}+2 \mathrm{R}_{\mathrm{E}}\left(1+\mathrm{h}_{\mathrm{fe}}\right)\right.}{2\left(\mathrm{R}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ie}}\right)}\right|
$$

## C. Input Impedance ( $\mathbf{R i}_{\mathbf{i}}$ :

$\mathrm{R}_{\mathrm{i}}$ is defined as the equivalent resistance existing between any one of the input and the ground when other input terminal is grounded.

$$
R_{i}=\frac{V_{S}}{I_{b}}
$$

Put the $V s$ and $I_{b}$ from the above discussion, $\mathrm{R}_{\mathrm{i}}=2\left(\mathrm{R}_{\mathrm{S}}+\mathrm{h}_{\mathrm{i}}\right)$.
For one transistor and input pair, the resistance is $\mathrm{Rs}_{\mathrm{s}}+\mathrm{h}_{\mathrm{i}}$.
Hence for dual input circuit, the total input resistance is $2\left(\mathrm{R}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ie}}\right)$, as the 2 circuits are perfectly matched.
This input resistance is not dependent on whether output is balanced or unbalanced.

## D) OUTPUT IMPEDANCE Ro:

- It is defined as the equivalent resistance between one of the output terminals with respect to ground.
- The resistance between output terminal with respect to ground is $\mathrm{R}_{\mathrm{C}}$.

$$
\mathrm{R}_{\mathrm{O}}=\mathrm{R}_{\mathrm{C}}
$$



## Changes to be made for FET is

$$
\begin{aligned}
& \text { BJT FET } \\
& \text { Rc Rd } \\
& \mathrm{re}=1 \\
& A \underset{d}{\substack{g_{V 0}^{m} \\
=V_{i n}}}=\frac{R_{d}}{V_{g_{m d}}}=g_{m d} R{ }_{d}
\end{aligned}
$$

## EnggTree.com

4. Draw a differential amplifier and its ac equivalent circuit. $(O R)$ Explain the operation of basic emitter coupled differential amplifier (or) Explain the function of differential amplifier with neat circuit. (A/M 2010) (M/J 2012) (OR) Explain the common mode and differential mode operation of the differential amplifier (May/June2016 Nov/Dec-2017, May-2018) (OR)
Explain the working of a single ended input differential amplifier. (Nov/Dec 2018)

## * DIFFERENTIAL AMPLIFIER BASIC BLOCK DIAGRAM:

- The differential amplifier amplifies the difference between two applied input signals $\mathrm{V}_{\text {in1 }}$ and $\mathrm{V}_{\text {in2 }}$ (voltage signals). Hence, it is called as Difference amplifier.


Fig: block diagram of differential amplifier

- In an ideal amplifier, the output voltage $\mathrm{V}_{\mathrm{o}}$ is proportional to the difference between the two input signals. Therefore we can write,

$$
\begin{equation*}
\mathrm{V}_{\mathrm{o}} \alpha\left(\mathrm{~V}_{\mathrm{in} 1}-\mathrm{V}_{\mathrm{in} 2}\right) \tag{1}
\end{equation*}
$$

## * DIFFERENTIAL GAIN $A_{d}$ :

- From the above equation, we can write the differential gain $A_{d}$ is [Generally gain is nothing but the output parameter (may be voltage, current, etc.) to input parameter].
- Therefore, $\quad V_{o}=A_{d}\left(V_{i n 1}-V_{i n 2}\right)$ $\qquad$
Where $\quad A_{d}=$ Differential gain constant
- This $\mathrm{A}_{\mathrm{d}}$ is thegain with which differential amplifier amplifies the difference between two input signal is called Differential gain.
- The difference between the two inputs $\left(\mathrm{V}_{\mathrm{in} 1} \sim \mathrm{~V}_{\mathrm{in} 2}\right)$ is generally called difference voltage and denoted as $\mathrm{V}_{\mathrm{d}}$.
- output foreThere voltage is $\mathrm{V}_{\mathrm{o}}=\mathrm{A}_{\mathrm{d}} . \mathrm{V}_{\mathrm{d}}$.
- Therefore the differential gain can be expressed as,

$$
\begin{equation*}
\mathrm{A}_{\mathrm{d}}=\frac{V_{o}}{V_{d}} \tag{4}
\end{equation*}
$$

* COMMON MODE GAIN $A_{c}$ : If we apply two input voltages which are equal in all the respect to the differential amplifier i.e., $V_{1}=V_{2}$ then, ideally the output voltage $V_{o}$ is $\left(V_{1} \sim V_{2}\right)$. $A_{d}$, must be zero.
- In this mode the applied input signals, phase and frequency must be in same.
- But the output voltage of the practical diferggiaterendefiner not only depends on the difference voltage but also depends on the average common level of the two inputs.
- Such an average level of the two input signal is called common mode signal which is denoted as $\mathrm{V}_{\mathrm{c}}$.
$\mathrm{V}_{\mathrm{c}}=\frac{V_{1+}+V_{2}}{2}$.
- In practical, the differential amplifier produces the output voltage proportional to each common mode signal. The gain which it amplifies the common mode signal to produce the output is called common mode gain of the differential amplifier denoted as $\mathrm{A}_{\mathrm{c}}$.
$\mathrm{A}_{\mathrm{c}}=\frac{V_{o}}{V_{c}}$
- So that total output of any differential amplifier can be expressed as,
$\mathrm{V}_{\mathrm{o}}=\mathrm{A}_{\mathrm{d}} . \mathrm{V}_{\mathrm{d}}+\mathrm{A}_{\mathrm{c}} . \mathrm{V}_{\mathrm{c}}$


## * COMMON MODE REJECTION RATIO:

- In differential amplifier, if both transistors input the same, then that differential amplifier is called as common mode differential amplifier.
- In common mode operation, the output is zero.
- But due to many disturbance in signals, noise signals appear as a common input signal to both the input terminals of the differential amplifier.
- Such a common signal should be rejected by the differential amplifier(CMRR).
- Thus, the ability of a differential amplifier to reject a common mode signal is expressed by a ratio called common mode rejection ratio.
- CMRR is defined as the ratio of the differential mode gain $\left(\mathrm{A}_{\mathrm{d}}\right)$ to common mode voltage gain $\left(\mathrm{A}_{\mathrm{c}}\right)$.
$\operatorname{CMRR}=\frac{|A d|}{\left|A_{c}\right|}=\rho$.
- In ideal case the CMRR is infinite, because the common mode gain is nearly or exactly zero. But in practical, it is not infinite.
- But $\rho$ is very large one, since $A_{d}$ is very large and $A_{c}$ is very small. The CMRR can be expressed in $d B$ also.

CMRR in $\mathrm{dB}=20 \log \frac{|A d|}{\left|A_{c}\right|} \mathrm{dB}$. $\qquad$

- The total output voltage is,
$\mathrm{V}_{\mathrm{o}}=\mathrm{A}_{\mathrm{d}} . \mathrm{V}_{\mathrm{d}}+\mathrm{A}_{\mathrm{c}} . \mathrm{V}_{\mathrm{c}}$
Where, $\quad V_{o}=$ Total output voltage of differential amplifier, $\mathrm{A}_{\mathrm{d}}=$ Differential mode gain of differential amplifier,
$\mathrm{A}_{\mathrm{c}}=$ Common mode gain of infggentiebacolifier,
$\mathrm{V}_{\mathrm{d}}=$ Differential mode voltage.
- From equation (10), $V_{o}$ can be written as,

$$
\left.\begin{array}{c}
\mathrm{V}_{\mathrm{o}}=\mathrm{A}_{\mathrm{d}} \cdot \mathrm{~V}_{\mathrm{d}}\left[1+\frac{\mathrm{Ac} \cdot V_{c}}{\text { Ad} \cdot V_{d}}\right] \ldots \ldots . . . . \\
\mathrm{V}_{\mathrm{o}}=\mathrm{A}_{\mathrm{d}} \cdot \mathrm{~V}_{\mathrm{d}}\left[1+\frac{1}{1} \cdot \frac{V_{c}}{\frac{A}{d}^{A}}\right] \\
V_{d} \tag{13}
\end{array}\right] \ldots .
$$

- Therefore, from the above equation, the CMRR is practically very large, though both $V_{c}$ and $V_{c}$ components are present.
- The output is proportional to the difference in signal only. Then the common mode component is greatly rejected.


## EMITTER COUPLED DIFFERENTIAL AMPLIFIER:

- The transistorized differential amplifier is an emitter and emitter follower circuit. So this is called as Emitter coupled differential amplifier.



## Figure(1): Emitter biased circuit

- Figure(1) shows the emitter coupled biased circuit. The transistor $\mathrm{TQ}_{1}$ and $\mathrm{TQ}_{2} u$ used in the figure are identical in characteristics and also having exactly matched characteristics.
- Then the two collector resistances $\mathrm{R}_{\mathrm{C} 1}$ and $\mathrm{R}_{\mathrm{C} 2}$ are equal while the two emitter resistances $\mathrm{R}_{\mathrm{E} 1}$ and $\mathrm{R}_{\mathrm{E} 2}$ are also equal.

Therefore $\mathrm{R}_{\mathrm{C} 1}=\mathrm{R}_{\mathrm{C} 2}$ and $\mathrm{R}_{\mathrm{E} 1}=\mathrm{R}_{\mathrm{E} 2}$

- In this the magnitude of $\mathrm{V}_{\mathrm{CC}}$ and $-\mathrm{V}_{\mathrm{EE}}$ are also same. Therefore the differential amplifier can be obtained by using such two emitter biased circuits.
- This emitter biased circuit can be obtained by connecting the $E_{1}$ of $\mathrm{TQ}_{1}$ with $\mathrm{E}_{2}$ of $\mathrm{TQ}_{2}$.
- Because of this connection the $\mathrm{R}_{\mathrm{E} 1}$ is parallel with $\mathrm{R}_{\mathrm{E} 2}$.
- The applied input $\mathrm{V}_{\mathrm{s} 1}$ is connected with b国qg Treendorm input is connected with the base of $\mathrm{TQ}_{2}$.
- Both input voltages in Base is with respect to ground. Then its balanced output is taken in between the respective collector terminals of both transistors $\left(\mathrm{TQ}_{1}\right.$ and $\left.\mathrm{TQ}_{2}\right)$.
- This amplifier is called Emitter coupled Differential Amplifier. In this circuit, the two collector resistance $\mathrm{R}_{\mathrm{C}}$ used are also same.
- Then the dual input differential balanced output differential amplifier is shown below. Because, none of the output terminal is grounded, the output is taken between two output terminals.
- So it is called as Balanced Differential Amplifier and it is shown in figure (2).


Figure (2): Balanced differential amplifier

- For studying the operation of differential amplifier, the following modes are used.
(i) Differential mode, and (ii) Common mode.


## i) Differential mode operation:

- In this mode, both inputs are different in either magnitude or phase like $180^{\circ}$ phase. This opposite phase can be obtained from the Center tap Transformer.
- That is assume that the sine wave on the base of $\mathrm{TQ}_{1}$ is positive going while on the base of $\mathrm{TQ}_{2}$ is negative going.
- With a positive going signal on the base of $\mathrm{TQ}_{1}$, if amplified, a negative going signal develops and appears on the collector of $\mathrm{TQ}_{1}$.
- Due to positive going signal, current through $\mathrm{R}_{\mathrm{E}}$ also decrease and hence a positive going current wave is developed across $\mathrm{R}_{\mathrm{E}}$.
- Due to negative going signal on the baseEqfggTreex.oumified positive going signal develops on the collector of $\mathrm{TQ}_{2}$ and anegative going signal develops across $\mathrm{R}_{\mathrm{E}}$, because of emitter follower action of TQ2.
- So. The signal voltage across $\mathrm{R}_{\mathrm{E}}$ due to effect of $\mathrm{TQ}_{1}$ and $\mathrm{TQ}_{2}$ are equal in magnitude and $180^{\circ}$ out of phase due to method pair of transistors.
- Hence these two signals cancel each other and there is no signal across the emitter resistance.
- Hence there is no AC signal current flowing through the emitter resistance. Hence $\mathrm{R}_{\mathrm{E}}$ in this case does not introduce negative feedback.
- While $\mathrm{V}_{\mathrm{o}}$ is the output taken across collector of $\mathrm{TQ}_{1}$ and collector of $\mathrm{TQ}_{2}$, the two outputs on collector $\mathrm{C}_{1}$ and $\mathrm{C}_{2}$ are equal in magnitude but opposite in polarity.
- And $\mathrm{V}_{\mathrm{o}}$ is the difference between these two signals. Hence, the different output $\mathrm{V}_{0}$ is twice as large as the signal voltage from collector to ground.


Figure (3): Differential mode

## COMMON MODE OPERATION:

- In common mode the signals applied to the base of the both transistor $\mathrm{TQ}_{1}$ and $\mathrm{TQ}_{2}$ are in same phase, frequency and also in magnitude.


Figure (4): common mode

- In phase signal voltages at the bases of $\mathrm{TQ}_{1}$ and $\mathrm{TQ}_{2}$ causes in phase signal voltages to appear across $\mathrm{R}_{\mathrm{E}}$ which add together.
- Hence $R_{E}$ causes a signal current and provides negative feedback.
- This feedback reduces the common mode gain of differential amplifier.


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5. Explain the analysis of Differential amplifier. With neat sketch explain the BJT differential amplifier with active load and derive for $A_{d}$, $A_{c}$, and CMRR How CMRR improved (Nov/Dec 2015)(Nov/Dec 2016,May-2018) (OR)

Deduce the expression for Emitter currents in a differential amplifier under large signal operation. (April/May 2019)

- Normally, analysis in amplifier depends on both AC and DC analysis.
- In the above two, the d.c signals determines the operating values for the transistors and used as biasing.
- Similarly, a.c signals are used as input signals, which determine the output of the differential amplifier.
- The dual input, balanced output differential amplifier is also called Symmetrical Differential Amplifier.


## * DC ANALYSIS:

- DC analysis means using D.c voltage as biasing voltage and keeping it constant (to obtain suitable operating point).
- For obtaining DC analysis, we must obtain operating point values i.e., $\mathrm{I}_{\mathrm{CQ}}$ and $\mathrm{V}_{\mathrm{CQ}}$ for the transistors used.
- In DC analysis, the supply voltage d.c is taken as biasing voltage and the applied input a.c signals of both $\mathrm{V}_{\mathrm{s} 1}$ and $\mathrm{V}_{\mathrm{s} 2}$ are to be zero.


Figure (1): DC Equivalent circuit

## To obtain DC analysis following assumptiשnfgg $\ddagger$ feectokqn:

1) Assuming $R_{S 1}=R_{S 2}$ (source resistances of both sides) and is simply denoted by $R_{S}$.
2) The transistor used $\mathrm{TQ}_{1}$ and $\mathrm{TQ}_{2}$ both are matched in their ideal identical characteristics.
3) Emitter resistances connected in both $R_{E 1}$ and $R_{E 2}$ must be the same.
i.e., $R_{E 1}=R_{E 2}=R_{E}$

$$
\text { Hence } \quad R_{\mathrm{E}}=\mathrm{R}_{\mathrm{E} 1} \| \mathrm{R}_{\mathrm{E} 2}=\frac{\mathrm{R}_{\mathrm{E} 1} \cdot \mathrm{R}_{\mathrm{E} 2}}{\left[\mathrm{R}_{\mathrm{E} 1}+\mathrm{R}_{\mathrm{E} 2}\right]}
$$

The collector resistances of both transistors also must be in same value.
i.e., $\mathrm{R}_{\mathrm{C} 1}=\mathrm{R}_{\mathrm{C} 2}=\mathrm{R}_{\mathrm{C}}$

The magnitude of $\left|\mathrm{V}_{\mathrm{CC}}\right|=\left|\mathrm{V}_{\mathrm{EE}}\right|$ are measured with respect to ground.

- Because of the above identical characteristics of both transistors, there is no necessity for finding out the operating point of each transistors.
- So, simply finding out the operating point to one is enough ( $\mathrm{I}_{\mathrm{CQ}}$ and $\mathrm{V}_{\mathrm{CEQ}}$ ).
- For finding out the $\mathrm{I}_{\mathrm{CQ}}$ and $\mathrm{V}_{\mathrm{CE}}$, the DC analysis diagram is needed.


Figure(2): DC analysis diagram

$$
\begin{gather*}
-\mathrm{I}_{\mathrm{B}} \mathrm{Rs}_{\mathrm{s}}-\mathrm{V}_{\mathrm{BE}}-2 \mathrm{I}_{\mathrm{E}} \mathrm{Re}_{\mathrm{E}}=-\mathrm{V}_{\mathrm{EE}} \ldots . . . .  \tag{1}\\
-\mathrm{I}_{\mathrm{B}} \mathrm{R}_{\mathrm{S}}-\mathrm{V}_{\mathrm{BE}}-2 \mathrm{I}_{\mathrm{E}} \mathrm{R}_{\mathrm{E}}+\mathrm{V}_{\mathrm{EE}}=0 \tag{2}
\end{gather*}
$$

But, $\quad \mathrm{I}_{\mathrm{C}}=\beta \mathrm{I}_{\mathrm{B}} \quad$ and $\quad \mathrm{I}_{\mathrm{C}} \approx \mathrm{I}_{\mathrm{E}}$. $\qquad$

- According to equation (3), $\quad I_{B}=\frac{\underline{I} C}{\beta}=\frac{\underline{L E}}{\beta}$
- Putting the value of equation (4) in (2),we get,

$$
\begin{align*}
& -{ }_{\beta}^{{ }^{\mathrm{IE}}} \mathrm{R}_{\mathrm{S}}-\mathrm{V}_{\mathrm{BE}}-2 \mathrm{I}_{\mathrm{E} R \mathrm{E}}+\mathrm{V}_{\mathrm{EE}}=0  \tag{5}\\
& -\mathrm{I}_{\mathrm{E}}\left[\frac{\mathrm{RS}}{\beta}+2 \mathrm{R}_{\mathrm{E}}\right]+\mathrm{V}_{\mathrm{EE}}-\mathrm{V}_{\mathrm{BE}}=0  \tag{6}\\
& \mathrm{I}_{\mathrm{E}}\left[\frac{\mathrm{RS}}{\beta}+2 \mathrm{R}_{\mathrm{E}}\right]=\mathrm{V}_{\mathrm{EE}}-\mathrm{V}_{\mathrm{BE}} \\
& \mathrm{IE}=\frac{-\mathrm{KEE}-\mathrm{VBE}}{\left[\frac{\beta}{\beta}+2 \mathrm{R}_{\mathrm{E}}\right.}  \tag{8}\\
& \text { In practice, } \frac{\mathrm{RS}}{\beta} \ll 2 \mathrm{R}_{\mathrm{E}}
\end{align*}
$$

$$
\mathrm{E}=\frac{\mathrm{V}_{\mathrm{EE}}-\mathrm{V}_{\mathrm{BE}}}{2 \mathrm{RE}_{\mathrm{E}}} \ldots \ldots \ldots . . \mathrm{Eng} \mathrm{n} \text { Tree.com }
$$

- From the above equation (1), we can observe the following points.
i. $\quad \mathrm{R}_{\mathrm{E}}\left(\right.$ Emitter resistance) determines the emitter circuit of $\mathrm{TQ}_{1}$ and $\mathrm{TQ}_{2}$ for the known value of $V_{E E}$.
ii. Then, the collector resistance $\left(\mathrm{R}_{\mathrm{L}}\right)$ is independent of current that flows through Emitter terminals of $\mathrm{TQ}_{1}$ and $\mathrm{TQ}_{2}$.

The collector voltage, $\mathrm{V}_{\mathrm{C}}=\mathrm{V}_{\mathrm{CC}}-\mathrm{I}_{\mathrm{C}} \mathrm{R}_{\mathrm{C}}$.

- Neglecting the drop across $\mathrm{R}_{\mathrm{S}}$, we can obtain the emitter voltage of $\mathrm{TQ}_{1}$ as approximately equal to $V_{b E}$.
- Then, $\quad \mathrm{V}_{\mathrm{CE}}=\mathrm{V}_{\mathrm{C}}-\mathrm{V}_{\mathrm{E}}=\left(\mathrm{V}_{\mathrm{CC}}-\mathrm{I}_{\mathrm{C}} \mathrm{R}_{\mathrm{C}}\right)-\mathrm{V}_{\mathrm{BE}}$. $\qquad$
$\mathrm{V}_{\mathrm{CE}}=\mathrm{V}_{\mathrm{CC}}+\mathrm{V}_{\mathrm{BE}}-\mathrm{I}_{\mathrm{C}} \mathrm{R}_{\mathrm{C}}$
- Hence, $\mathrm{I}_{\mathrm{E}}=\mathrm{I}_{\mathrm{C}}=\mathrm{I}_{\mathrm{CQ}}$ while $\mathrm{V}_{\mathrm{CE}}=\mathrm{V}_{\mathrm{CEQ}}$ for given values of $\mathrm{V}_{\mathrm{CC}}$ and $\mathrm{V}_{\mathrm{EE}}$.
- Therefore operating point $(\mathrm{Q})$ can be obtained from equation (10) and (12).


## * AC ANALYSIS:(Nov/Dec 2016)

- For performing AC analysis, we must apply AC input signals as an input. So, we can calculate the following:
E. Differential mode gain $\left(\mathrm{A}_{\mathrm{d}}\right)$.
F. Common mode gain $\left(\mathrm{A}_{\mathrm{c}}\right)$.
G. Input resistance $\left(\mathrm{R}_{\mathrm{i}}\right)$.
H. Output resistance $\left(\mathrm{R}_{\mathrm{o}}\right)$.

The above can be obtained by using h-parameters.

## D. Differential gain ( $\mathrm{Ad}_{\mathrm{d}}$ )

- To obtain the Differential mode gain, the two input signals must be different from each other.
- Here, we take the two a.c input signals as equal in magnitude but having $180^{\circ}$ phase shift between them.
- Then, the magnitude of each a.c input voltage $\mathrm{V}_{\mathrm{S} 1}$ and $\mathrm{V}_{\mathrm{S} 2} \frac{\mathrm{~V}_{\mathrm{S}}}{2}$.
- For the a.c purposes, emitter terminal can be grounded which is shown in figure below with small signal analysis.



## Figure (1): AC Equivalent for differential operation (half circuit concept)

- The circuit which can be analyzed by considering only one transistor is called Half circuit concept of analysis.


Figure(2): Approximate hybrid model

- For obtaining the differential mode gain $\left(\mathrm{A}_{\mathrm{d}}\right)$ from the above hybrid model, we have to apply the Kirchhoff's voltage law in input side,
$\frac{\mathrm{V}_{\mathrm{S}}}{2}=\mathrm{i}_{\mathrm{b}} \mathrm{R}_{\mathrm{S}}+\mathrm{i}_{\mathrm{b}} \mathrm{h}_{\mathrm{ie}}$

$$
\begin{align*}
& \frac{\mathrm{V}_{\mathrm{S}}}{2}=\mathrm{i}_{\mathrm{b}}\left(\mathrm{Rs}+\mathrm{h}_{\text {ie }}\right)  \tag{2}\\
& \mathrm{i}_{\mathrm{b}}=\frac{\mathrm{V}_{\mathrm{S}}}{2\left(\mathrm{Rs}_{\mathrm{S}}+\mathrm{h}_{\mathrm{ie}}\right)} \tag{3}
\end{align*}
$$

- Similarly, applying the Kirchhoff's voltage law to output loop, we get
$\mathrm{V}_{\mathrm{o}}=-\mathrm{I}_{\mathrm{b}} \mathrm{h}_{\mathrm{fe}} . \mathrm{R}_{\mathrm{C}}$
- Put the value of $\mathrm{I}_{\mathrm{b}}$ in equation (4) from (3), we get,

$$
\begin{equation*}
\mathrm{V}_{\mathrm{o}}=\frac{-\mathrm{h}_{\mathrm{fe}} \mathrm{~V}_{\mathrm{s}} \mathrm{Rc}_{\mathrm{c}}}{2\left(\mathrm{R}_{\mathrm{S}}+\mathrm{h}_{\mathrm{ie}}\right)} \ldots \ldots . \tag{5}
\end{equation*}
$$

- Then,,$\frac{\mathrm{V}_{\mathrm{o}}}{\mathrm{V}_{\mathrm{s}}}=\frac{-\mathrm{h}_{\mathrm{Fe}} \cdot \mathrm{R}_{\mathrm{C}}}{2\left(\mathrm{Rs}_{\mathrm{S}}+\mathrm{h}_{\mathrm{ie}}\right)}$
- Negative sign indicates that $180^{\circ}$ phase difference between input and output. If the input signals are equal and are out of phase by $180^{\circ}$, we get
- Differential mode signal $\mathrm{V}_{\mathrm{d}}=\mathrm{V}_{1}-\mathrm{V}_{2}=\left(\frac{\mathrm{V}_{\mathrm{s}}}{Z} n \mathrm{ng}_{2} \frac{\mathrm{~V}_{s}}{4}\right) r$ ēd.con ...(7)

Where, $\mathrm{V}_{\text {S }}$ is differential input voltage.

- Differential voltage gain $A_{d}=\frac{\mathrm{V}_{0}}{\mathrm{~V}_{\mathrm{s}}}$

$$
\begin{equation*}
A_{d}=\frac{\mathrm{h}_{\mathrm{fe}} \mathrm{R}_{\mathrm{C}}}{2\left(\mathrm{R}_{\mathrm{S}}+\mathrm{h}_{\mathrm{ie}}\right)} \ldots \ldots \ldots \tag{8}
\end{equation*}
$$

- When the output of differential amplifier is measured with reference to ground, it is called unbalanced output.
- The output across the collectors of $\mathrm{Q}_{1}$ and $\mathrm{Q}_{2}$ to be perfectly matched then $\mathrm{A}_{d}$ for balanced output is twice than that of $\mathrm{A}_{\mathrm{d}}$ for unbalanced output. Therefore

$$
\begin{equation*}
A_{d}=\frac{h_{\mathrm{fe}} \mathrm{R}_{\mathrm{C}}}{\left(\mathrm{R}_{\mathrm{S}}+\mathrm{h}_{\mathrm{ie}}\right)} \cdots \tag{9}
\end{equation*}
$$

## E. Common mode gain (Ac)

- In common mode, the both transistor's input magnitude and phases are also inphase with each other.
- Let us assume that input signals are having the same magnitude $\mathrm{V}_{\mathrm{S}}$ and are in same phase.
- Common mode voltage $\mathrm{V}_{\mathrm{C}}=\frac{\mathrm{V}_{1}+\mathrm{V}_{2}}{2}=\frac{\mathrm{V}_{\mathrm{S}}+\mathrm{V}_{\mathrm{S}}}{2}=\mathrm{V}_{\mathrm{S}}$ $\qquad$ .(10)
- If suppose, the output is expressed as, $\mathrm{V}_{\mathrm{o}}=\mathrm{A}_{\mathrm{C}} . \mathrm{V}_{\mathrm{S}}$
- Common mode gain $A_{C}=\frac{V_{0}}{V_{S}}$
- In this mode, both the emitter current $\mathrm{I}_{\mathrm{e} 1}=\mathrm{I}_{\mathrm{e} 2}=\mathrm{I}_{\mathrm{e}}$ of $\mathrm{TQ}_{1}, \mathrm{TQ}_{2}$ flows through $\mathrm{R}_{\mathrm{E}}$ in the same direction, with same magnitude.
- Hence, the total current flowing through $\mathrm{R}_{\mathrm{E}}$ is nearly $2 \mathrm{I}_{\mathrm{e}}$



## Figure(1): A.C. Equivalent Circuit for Common Mode Configuration

- Then the approximate hybrid model for the above circuit can be obtained and is used to obtain the $A_{d}$.


Figure(2): Approximate Hybrid model

- As the current through $\mathrm{R}_{\mathrm{E}}$ is $2 \mathrm{I}_{\mathrm{e}}$, for simplicity of derivation, we have to assume the $\mathrm{I}_{\mathrm{e}}$ and effective emitter resistance as $2 \mathrm{R}_{\mathrm{E}}$.
- Current through $\mathrm{R}_{\mathrm{C}}=$ Load current $\mathrm{I}_{\mathrm{L}}$
- Effective emitter $=2 \mathrm{R}_{\mathrm{E}}$
- Current through emitter resistance $=\mathrm{I}_{\mathrm{L}}+\mathrm{I}_{\mathrm{b}}$
- Current through $\mathrm{h}_{\mathrm{oe}}=\left(\mathrm{I}_{\mathrm{L}}-\mathrm{h}_{\mathrm{fe}} . \mathrm{I}_{\mathrm{b}}\right)$
- Now, applying Kirchhoff's voltage law to input side,


Figure (3): Input side

$$
\begin{align*}
& -\mathrm{I}_{\mathrm{b}} \mathrm{R}_{\mathrm{S}}+\mathrm{I}_{\mathrm{b}} \mathrm{~h}_{\mathrm{ie}}+2 \mathrm{R}_{\mathrm{E}}\left(\mathrm{I}_{\mathrm{L}}+\mathrm{I}_{\mathrm{b}}\right)=-\mathrm{V}_{\mathrm{S}}  \tag{14}\\
& \mathrm{I}_{\mathrm{b}} \mathrm{R}_{\mathrm{S}} \mathrm{I}_{\mathrm{b}} \mathrm{~h}_{\mathrm{ie}}-2 R_{E}\left(\mathrm{I}_{\mathrm{L}}+\mathrm{I}_{\mathrm{b}}\right)=\mathrm{V}_{\mathrm{S}} \ldots \ldots \ldots .  \tag{15}\\
& \text { While, } \quad \mathrm{V}_{\mathrm{o}}=-\mathrm{I}_{\mathrm{L}} \cdot \mathrm{R}_{\mathrm{C}} \tag{15a}
\end{align*}
$$

- Negative sign is due to the assumed direction of current. Similarly apply KVL to output side.


Figure (4): Output side

$$
\begin{align*}
& =-\left(\mathrm{I}_{\mathrm{L}^{-}}=\mathrm{h}_{\mathrm{h}} \mathrm{~h}_{\mathrm{e}} \mathrm{I}_{\mathrm{b}}\right)-2 \mathrm{R}_{\mathrm{E}}\left(\mathrm{I}_{\mathrm{L}}+\mathrm{I}_{\mathrm{b}}\right)-\mathrm{I}_{\mathrm{L}} \mathrm{R}_{\mathrm{C}}=0 \ldots .  \tag{16}\\
& \underset{h_{o e}}{\frac{-I_{\mathrm{L}}}{}}+\frac{\mathrm{h}_{\mathrm{Fe}} \mathrm{I}_{\mathrm{b}}}{\mathrm{~h}_{\mathrm{oe}}}-2 \mathrm{I}_{\mathrm{L}}^{\mathrm{R}} \underset{\mathrm{E}}{ }-2 \mathrm{I}_{\mathrm{b}}^{\mathrm{R}} \underset{\mathrm{E}}{ }-\underset{\mathrm{L}}{\mathrm{I}_{\mathrm{C}} \mathrm{R}_{\mathrm{C}}}=0 \ldots  \tag{17}\\
& \mathrm{~b}_{\mathrm{h}}\left[\frac{\mathrm{~h}_{\mathrm{Fe}}}{\mathrm{~h}_{\mathrm{oe}}}-2 \mathrm{R}_{\mathrm{E}}\right]=\mathrm{I}_{\mathrm{L}}\left[\frac{1}{\mathrm{~h}_{\mathrm{oe}}}+2 \mathrm{R}_{\mathrm{E}}+\mathrm{R}_{\mathrm{C}}\right]
\end{align*}
$$

- Multiplying both sides by $h_{o e}$, then
$\mathrm{I}_{\mathrm{b}}\left[\mathrm{h}_{\mathrm{fe}}-2 \mathrm{R}_{\mathrm{E}} \mathrm{h}_{\mathrm{oe}}\right]=\mathrm{I}_{\mathrm{L}}\left[1+\mathrm{h}_{\mathrm{oe}}\left(2 \mathrm{R}_{\mathrm{E}}+\mathrm{R}_{\mathrm{C}}\right)\right]$

$$
\begin{align*}
& \frac{\mathrm{I}_{\mathrm{L}}}{\mathrm{I}_{\mathrm{b}}}=\frac{\left[\mathrm{h}_{\mathrm{f}} \mathrm{En}\right. \text { g g fltee.com }}{\left[1+\mathrm{h}_{o e}\left(2 \mathrm{R}_{\mathrm{E}}+\mathrm{R}_{\mathrm{c}}\right)\right]}  \tag{20}\\
& \mathrm{I}_{\mathrm{b}}=\frac{\mathrm{L}\left[1+\mathrm{h}_{\mathrm{og}}\left(2 \mathrm{R}_{\mathrm{E}}+\mathrm{R} \mathrm{C}\right)\right]}{\left[\mathrm{h}_{\mathrm{Fe}}-2 \mathrm{R}_{\mathrm{E}} \mathrm{~h}_{\mathrm{oe}}\right]} \tag{21}
\end{align*}
$$

- Putting this $\mathrm{I}_{\mathrm{b}}$ in equation (15),

$$
\begin{array}{r}
\mathrm{V}_{S}=\frac{\mathrm{I}_{\mathrm{L}}\left[1+\mathrm{h}_{\mathrm{oe}}\left(2 \mathrm{R}_{\mathrm{E}}+\mathrm{R}_{\mathrm{C}}\right)\right]\left[\mathrm{R}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ie}}+2 \mathrm{R}_{\mathrm{E}}\right]+2 \mathrm{R}_{\mathrm{E}}}{\left[\mathrm{~h}_{\mathrm{fe}}-2 \mathrm{R}_{\mathrm{E}} \mathrm{~h}_{\mathrm{oe}}\right]} \\
\frac{\mathrm{V}_{S}}{\mathrm{I}_{\mathrm{L}}}=\frac{\left[1+\mathrm{h}_{\mathrm{oe}}\left(2 \mathrm{Re}_{\mathrm{E}}+\mathrm{R}_{\mathrm{C}}\right)\right]\left[\mathrm{R}_{s}+\mathrm{h}_{\mathrm{ie}}+2 \mathrm{R}_{\mathrm{E}}\right]+2 \mathrm{R}_{\mathrm{E}}}{\left[\mathrm{~h}_{\mathrm{fe}}-2 \mathrm{Re}_{\mathrm{oe}}\right]} \ldots(22) \tag{22}
\end{array}
$$

- Then, find LCM and adjusting the terms,

$$
\begin{gather*}
\frac{V_{S}}{I_{L}}=\frac{2 R_{E}\left(1+h_{f e}\right)+R_{s}\left(1+2 R_{E} h_{o e}\right)+h_{i e}\left(1+2 R_{E} h_{o e}\right)+h_{o e} R_{C}\left(2 R_{E}+R_{s}+h_{o e}\right)}{\left[h_{f e}-2 R_{E} h_{o e}\right]} \\
\frac{V_{S}}{\mathrm{I}_{\mathrm{L}}}=\frac{2 R_{E}\left(1+h_{f e}\right)+\left(R_{s}+h_{i e}\right)\left(1+2 R_{E} h_{o e}\right)+h_{o e} R_{C}\left(2 R_{E}+R_{s}+h_{o e}\right)}{\left[h_{f e}-2 R_{E} h_{o e}\right]} \ldots \text { (23) } \tag{23}
\end{gather*}
$$

- Actually $h_{o e} R_{C} \ll 1$. Neglecting the terms,

$$
\begin{align*}
& \frac{V_{S}}{I_{L}}=\frac{2 R_{E}\left(1+h_{f e}\right)+\left(R_{s}+h_{\text {ie }}\right)\left(1+2 R_{E h_{o e}}\right)}{\left[h_{\text {fe }}-2 R_{E E} h_{o e}\right]} \ldots . .  \tag{2}\\
& I_{L}=\frac{V_{s .}\left[h_{f e}-2 R_{E h_{o e}}\right]}{2 R_{E}\left(1+h_{f e}\right)+\left(R_{s}+h_{i e}\right)\left(1+2 R_{E} h_{o e}\right)} \ldots . .( \tag{25}
\end{align*}
$$

- Putting this $\mathrm{I}_{\mathrm{L}}$ in equation (15a),

$$
\begin{align*}
& \mathrm{V}_{\mathrm{o}}=-\mathrm{I}_{\mathrm{L}} \cdot \mathrm{R}_{\mathrm{C}} \tag{26}
\end{align*}
$$

- Hence the common mode gain can be written as,

$$
\begin{equation*}
A_{c}=\frac{V_{o}}{V_{S}}=\frac{\left[2 R_{E h_{o e}}-h_{f e}\right] R_{c}}{2 R_{E}\left(1+h_{f e}\right)+\left(R_{s}+h_{\text {ie }}\right)\left(1+2 R_{E} h_{o e}\right)} \cdots \cdots \tag{27}
\end{equation*}
$$

- In practice, $h_{o e}$ is neglected, because the expression for $A_{c}$ can be further modified as,

$$
\begin{equation*}
\mathrm{Ac}_{\mathrm{C}}=\frac{-\mathrm{h}_{\mathrm{fe}} \mathrm{Rc}_{\mathrm{c}}}{\mathrm{R}_{\mathrm{S}}+\mathrm{h}_{\mathrm{ie}}+2 \mathrm{R}_{\mathrm{E}}\left(1+\mathrm{h}_{\mathrm{fe}}\right)} \ldots . \tag{28}
\end{equation*}
$$

- The above expression is same whether the output is balanced or unbalanced.


## COMMON MODE REJECTION RATIO (CMRR):

- $\quad$ CMRR $=\left|\left.\right|_{A_{C}} ^{\underline{A}_{d}}\right|$
- From equation (8) and (28),

$$
\begin{equation*}
\text { CMRR } \xlongequal[=]{=}\left|\frac{\operatorname{lgg} \text { Treee.tơße }\left(1+\mathrm{h}_{\mathrm{fe}}\right)}{2\left(\mathrm{Rs}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ie}}\right)}\right| \tag{30}
\end{equation*}
$$

- This is CMRR for dual input balanced output differential amplifier circuit.
- For balanced case,

$$
C M R R=\left|\frac{\left(\mathrm{Rs}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ie}}+2 \mathrm{R}_{\mathrm{E}}\left(1+\mathrm{h}_{\mathrm{fe}}\right)\right.}{\left(\mathrm{Rs}+\mathrm{h}_{\mathrm{ie}}\right)}\right|
$$

- or unbalanced case,

$$
C M R R=\left|\frac{\left(\mathrm{Rs}_{\mathrm{s}}+\mathrm{h}_{\mathrm{ie}}+2 \mathrm{Re}_{\mathrm{E}}\left(1+\mathrm{h}_{\mathrm{fe}}\right)\right.}{2\left(\mathrm{Rs}+\mathrm{h}_{\mathrm{ie}}\right)}\right|
$$

## C. Input Impedance ( $\mathbf{R}_{\mathbf{i}}$ ):

- $\mathrm{R}_{\mathrm{i}}$ is defined as the equivalent resistance existing between any one of the input and the ground when other input terminal is grounded.

$$
R_{i}=\frac{V_{S}}{I_{b}}
$$

- Put the $V s$ and $I_{b}$ from the above discussion, $\mathrm{R}_{\mathrm{i}}=2\left(\mathrm{R}_{\mathrm{S}}+\mathrm{h}_{\mathrm{ie}}\right)$.
- For one transistor and input pair, the resistance is $\mathrm{R}_{\mathrm{S}}+\mathrm{h}_{\mathrm{i}}$.
- Hence for dual input circuit, the total input resistance is $2\left(\mathrm{R}_{\mathrm{S}}+\mathrm{h}_{\mathrm{i}}\right)$, as the 2 circuits are perfectly matched.
- This input resistance is not dependent on whether output is balanced or unbalanced.


## D) OUTPUT IMPEDANCE Ro:

- It is defined as the equivalent resistance between one of the output terminals with respect to ground.
- The resistance between output terminal with respect to ground is $\mathrm{R}_{\mathrm{C}}$.
$\mathrm{R}_{\mathrm{O}}=\mathrm{R}_{\mathrm{C}}$


## 6. Explain the FET input stages.

## * FET parameters:

- The following are the parameters of FET as an amplifier.

1. The transcondutance ' $g_{m}$ '
2. The dynamic resistance ' $r_{d}$ ' and
3. The amplification factor $\mu$.

## - Transcondutance:

$\checkmark$ It is defined as the ratio of change in drain current to the change in gate source voltage at a constant drain source voltage.

$$
g_{m}=\frac{\Delta I_{D}}{\Delta V_{G S}} / D_{D S}=\text { Constant }
$$

$\checkmark$ It is expressed in mill amperes per volt or micro mhos. It is sometimes referred to as the common source forward trans admittance.

## - Dynamic Drain Resistance or output Resistance:

$\checkmark$ The drain resistance is defined as the ratio of change in drain source voltage $V_{D S}$ to the change in drain current $I_{D}$ at a constant gate source voltage.

$$
r_{d}=\frac{\Delta V_{D S}}{\Delta I_{D}} / \Delta V V_{G S}
$$

$\checkmark$ The reciprocal of drain resistance is the drain conductance, it is called sometimes as common source output conductance.

## - Amplification factor:

$\checkmark$ Amplification factor is defined as the ratio of change in drain source voltage to the change in gate source voltage at a constant drain current.

$$
\mu=\frac{\Delta V D S}{\Delta V_{G S}} / \Delta I{ }_{D}
$$

## - Relation between FET parameters:

$\checkmark$ We know that $\mu=\frac{\Delta V D S}{\Delta V_{G S}}$
$\checkmark$ Multiplying the numerator and the denominator on the R.H.S by $\Delta I_{D}$, We have

$$
\mu=\frac{\Delta V_{\underline{ } \text { S }}}{\Delta V_{G S}} \times \frac{\Delta I_{D}}{\Delta I_{D}}=\frac{V_{D S}}{I_{D}} \times \frac{I_{D}}{V_{G S}}=g_{m} \mathrm{x} r_{d}
$$

$\checkmark$ Therefore $\mu=g_{m} \times r d$ is the relation between the parameters of a FET.

## - FET configurations:

$\checkmark$ There are three types of configurations in the FET amplifier, they are:

- Common source configuration
- Common drain configuration
- Common gate configuration
$\checkmark$ A FET can be connected in any one of the three configurations. The common drain circuit also called source follower circuit.

7. Draw the circuit diagram of a single tuned amplifier and obtained expression for its gain ,resonant and cut off frequency (May/June 2016), (Nov/Dec2015)
(OR)
Illustrate the behavior of a MOSFET based amplifier circuit tuned load. Also deduce expression for voltage gain at Centre frequency, $Q$ and bandwidth. (April/May 2019)

## SINGLE TUNED CAPACITIVE COUPLED TUNED AMPLIFIER

- Tuned amplifiers are amplifiers that are designed to reject a certain range of frequencies below a lower cut off frequency $\omega_{\mathrm{L}}$ and above a upper cut off frequency $\omega_{\mathrm{H}}$ and allows only a narrow band of frequencies.

- The output across the tuned circuit is coupled to the next stage through the coupling capacitor. The tuned circuit is formed by $L$ and $C$ resonates at the frequency of operation.


Equivalent circuit of single tuned amplifier


Here $\mathrm{C}_{\mathrm{i}}$ and $\mathrm{C}_{\text {eq }}$ represent input and output circuits capacitance respectively. They can be given as
$\mathrm{C}_{\mathrm{i}}=\mathrm{C}_{\mathrm{be}}+\mathrm{C}_{\mathrm{bc}}(1-\mathrm{A})$ where A is the voltage gai⿷匚gth
$\mathrm{C}_{\mathrm{eq}}=\mathrm{C}_{\mathrm{be}}((\mathrm{A}-1) / \mathrm{A})+\mathrm{C}$ where C is the tuned circuit capacitance
The $g_{c e}$ is represented as the output resistance of current of generator $\mathrm{gmV}_{\mathrm{be}}$
$\mathrm{g}_{\mathrm{ce}}=\left(1 / \mathrm{r}_{\mathrm{ce}}\right)=\mathrm{h}_{\mathrm{ce}}-\mathrm{gm} * \mathrm{~h}_{\mathrm{ce}}=\mathrm{h}_{\mathrm{ce}}=\left(1 / \mathrm{R}_{0}\right)$
The admittance of the inductor along with resistor R is given by
$Y=\frac{1}{R+j \omega L}$
Multiplying numerator and denominator by $R+j \omega L$ we get
$Y=\frac{R-j \omega L}{R^{2}+\omega^{2} L^{2}}=\frac{R}{R^{2}+\omega^{2} L^{2}}-\frac{j \omega L}{R^{2}+\omega^{2} L^{2}}=\frac{R}{R^{2}+\omega^{2} L^{2}}-\frac{j \omega^{2} L}{\omega\left(R^{2}+\omega^{2} L^{2}\right)}=\frac{1}{R_{P}}+\frac{1}{j \omega L P}$
Where $R{ }_{P}=\frac{R+2 \omega L 2^{2}, ~ a n d ~}{R}{ }_{P}=\frac{R^{2}+\omega^{2} L^{2}}{\omega^{2} L}$
The LP and RP are in shunt quality factor of the coil at resonance is given by

$$
\begin{gathered}
\mathrm{Qo}=\mathrm{WoL} / \mathrm{R} \\
L_{P}=\frac{R^{2}+\omega^{2} L^{2}}{\omega^{2} L}
\end{gathered}
$$

Dividing numerator and denominator terms by $\omega^{2} L$,

$$
L_{P}=\frac{R^{2} / \omega^{2} L+L}{1}
$$

Hence, The output circuit of the amplifier can be modified as


Equivalent circuit of the output part of the tuned amplifier
Taking $R_{1}$ as the parallel combination of $R_{0}, R_{P}$ and $R_{i}$ i.e.

$$
\frac{1}{R_{t}}=\frac{1}{R_{0}}+\frac{1}{R_{P}}+\frac{1}{R_{i}}
$$

The output circuit can be modified as shown in fig.

$$
\boldsymbol{Q}_{e}=\frac{\text { Susceptance of inductance L C'capacitance C }}{\text { Conductance shunt resistance } \mathrm{R}_{\mathrm{t}}}
$$



Simplified output circuit of the tuned amplifier

Where Z is the impedance of $\mathrm{C}, \mathrm{L}$ and $\mathrm{R}_{\mathrm{t}}$ inparallel. The admittance $\mathrm{Y}=(1 / \mathrm{Z})$ is given by

$$
\left.Y=\frac{1}{Z}=\frac{1}{R}+\frac{1}{j \omega L} \text { Eng } \omega \text { Tree } \frac{1}{R} \frac{1}{R} \varphi 1+\frac{R_{t}}{j \omega L}+j \omega C R_{t}\right]
$$

Multiplying numerator and denominator by $\omega_{0}$

$$
\begin{gathered}
Y=\frac{1}{R_{t}}\left[1+\frac{R_{t} \omega_{0}}{j \omega L \omega_{0}}+\frac{j \omega \omega_{0} C R_{t}}{\omega_{0}}\right] \\
\frac{R_{t}}{L \omega_{0}}=\omega_{0} C R_{t}=Q_{e} \\
Y=\frac{1+j Q_{e}\left[\frac{\omega}{\omega_{0}}-\frac{\omega_{0}}{\omega}\right]}{R_{t}} \\
Z=\begin{array}{r}
Y \\
Y
\end{array} \frac{R_{t}}{1+j Q_{e}\left[\frac{\omega}{\omega_{0}}-\frac{\omega_{0}}{\omega}\right]}
\end{gathered}
$$

Let $\delta$ the fractional frequency variation.

$$
\begin{gathered}
\delta=\frac{\omega-\omega_{0}}{\omega_{0}}=\frac{\omega}{\omega_{0}}-1=\frac{\omega}{\omega_{0}}=1+\delta \\
Z=\frac{R_{t}}{1+j Q_{e}\left[(1+\delta)-\left(\frac{1}{1+\delta}\right)\right]}=\frac{R_{t}}{1+j Q_{e}\left[\frac{1+\delta^{2}+2 \delta-1}{1+\delta}\right]} \\
Z=\frac{R_{0}}{1+j 2 Q_{e} \delta\left[\frac{2}{1+\delta}\right]}
\end{gathered}
$$

Frequency close to resonance $\omega_{0}, \delta \ll 1$

$$
Z=\frac{R_{t}}{1+j 2 Q_{e} \delta}
$$

At resonance $\omega=\omega_{0}, \delta=0$

$$
\begin{gathered}
Z=R_{t}=R_{0} \text { parallel } R_{P} \text { Parallel } R \\
R_{P}=\frac{\omega_{0 L^{2}}}{R}=\frac{\omega_{0} L}{\omega_{0} C R} \\
V_{b^{\prime} e}=V_{i} \frac{r_{b^{\prime} e}}{r_{b b^{\prime}}+r_{b^{\prime} e}} \\
V_{0}=-g_{m} V_{b^{F} e} Z=-g_{m}\left(V_{i} \frac{r_{b^{F} e}}{r_{b b F}+r_{b F_{e}}}\right) Z
\end{gathered}
$$

Voltage gain with out considering the source resistance is given by

$$
\begin{aligned}
A_{v} & \left.=\frac{V_{\text {En }}}{}=\underset{\substack{\text { ng } \\
i}}{-y_{m}} \underset{r_{b b F}+r_{b F_{e}}}{ }\right) Z
\end{aligned}
$$

$$
\begin{gathered}
A_{v}=-g_{m}\left(\frac{r_{b^{F}}}{r_{b b F}+r_{b F_{e}}}\right) * \frac{R_{t}}{1+j 2 Q_{e} \delta} \\
A_{v}(\text { at resonance })=-g_{m}\left(\frac{r_{b_{e}}}{r_{b b F}+r_{b F_{e}}}\right) * R_{t}
\end{gathered}
$$

$$
\left|\frac{A_{v}}{A_{v}(\text { at resonance })}\right|=\frac{1}{\sqrt{1+\left(2 \delta Q_{e}\right)^{2}}}
$$

$$
\begin{gathered}
2 \delta=\frac{1}{Q_{e}} \\
\Delta \omega=\frac{1}{R_{t} C} \mathrm{rad} / \mathrm{sec}
\end{gathered}
$$

Gain $\frac{A v}{A_{\nu}(\text { at resonance })}$ plotted against $\delta$

8. Draw the frequency response of an ideal and a practical tuned amplifier and discuss their characteristics. (Nov/Dec 2018)
The amplifier that amplifies a particular frequency and rejects other frequencies are termed as tuned amplifiers.


Figure (1): Ideal Tuned Circuit
Basically the tuned amplifier amplify the signal within a narrow frequency band that is centered about a frequency $f_{0}$. The signal between the lower and higher cut-off frequencies is amplified. The resonant frequency of an ideal tuned circuit is expressed as,

$$
f_{0}=\frac{1}{2 \pi \sqrt{L C}} \quad(\text { or }) \omega_{0}=\frac{1}{\sqrt{L C}} \quad\left[\text { since } \omega_{0}=2 \pi \mathrm{f}_{0}\right]
$$

Figures 2(a), 2(b) illustrates the ideal response and actual response curve of a tuned amplifier circuit respectively.

From the figure 2(b), it is observed that at higher and lower cut-off frequencies, the curve decreases and is maximum at resonant frequency ( $\mathrm{f}_{0}$ ).

(a) Ideal Response

(b) Actual Response Curve

The behavior of tuned circuit at various frequencies is,

1. At frequencies above resonant frequency, the circuit behaves as capacitive load due to which the current leads the applied voltage.
2. At frequencies below resonant frequency, the circuit behaves as inductive load due to which the current lags behind the applied voltage.
3. At resonant frequency, the circuit behaves as resistive load since the inductive and capacitive effects are nullified.

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9. Explain briefly about gain and frequency response of single-tuned amplifier.
$>$ The voltage gain of an amplifier depends upon current gain $(\beta)$, input resistance $\left(\mathrm{R}_{\mathrm{i}}\right)$ and effective or a.c load resistance.
$>$ The voltage gain is given by the relation,

$$
\mathrm{A}_{\mathrm{v}}=\beta \times \frac{r_{L}}{R_{i}}
$$

$>$ The a.c load resistance of a parallel resonant circuit (i.e., tuned circuit) is given by the relation,

$$
\mathrm{R}_{\mathrm{L}}=\mathrm{Z}_{\mathrm{p}}=\frac{\mathrm{L}}{\mathrm{CR}}
$$

Where, $\mathrm{L}=$ value of inductance,

$$
\begin{aligned}
& \mathrm{C}=\text { value of capacitance, and } \\
& \mathrm{R}=\text { value of effective resistance of the inductor. }
\end{aligned}
$$

> Voltage gain of a voltage amplifier is given by the relation,

$$
\mathrm{A}_{\mathrm{v}}=\beta \times \frac{\frac{\mathrm{L}}{\mathrm{CR}}}{R_{i}}
$$

$>$ We know that the value of the quantity $\frac{\mathrm{L}}{\mathrm{CR}}$ (changes above or below the resonant called impedance of the tuned circuit) is very high at the resonant frequency and it decreases as the frequency changes above or below the resonant frequency.
$>$ Therefore voltage gain of a tuned amplifier is very high at the resonant frequency and it decreases as the frequency changes above or below the resonant frequency.
$>$ The above facts are shown in the form of a voltage gain versus frequency plot shown in figure below.


## Figure: Frequency response curve

$>$ Such a plot is called Frequency response curve of a tuned voltage amplifier.
$>$ The bandwidth $(\mathrm{BW})$ of an amplifier is equal to the frequency difference between the point A and B on either side of the resonant frequency, where the value of voltage gain drops to $1 / \sqrt{2}$ of its maximum value of resonance.
> Thus bandwidth,

$$
\mathrm{BW}=\Delta \mathrm{f}=\mathrm{f}_{2}-\mathrm{f}_{1}=\frac{f_{o}}{Q_{o}} \quad \text { EnggTree.com }
$$

Where $Q_{o}$ is the quality factor (or Q -factor) of the tuned circuit.

## Neutralization methods

## 10. Describe any one method of neutralization used in tuned amplifier?

Briefly explain Hazel line neutralization used in tuned amplifiers for stabilization (May/June 2016)(Nov/Dec 2016,May-2018)

## STABILITY OF TUNED AMPLIFIER

Stability of tuned amplifier is achieved by neutralization

## i). Hezeltine neutralization <br> ii). Neutrodyne neutralization

* In a tuned RF amplifier the transistor are used at the frequency near to their unity gain bandwidth. To amplify the narrow band of high frequencies.
* At this frequency inter-junction capacitor $\mathrm{b} / \mathrm{w}$ base and collector of transistor (Cbc)of transistor becomes dominant
* As a reactance of Cbc at Rf is low and its provide feedback path from a collector to base.
* If some feedback signal reaches the input from output in a positive manner with proper phase shift then the circuit is unstable, generating its own oscillation.

Amplifier, it was necessary to reduce stage gain to a level that ensures the circuit stability


This can be achieved in several ways
i) favoring the stability factor of the tuned circuits
ii) loose coupling $\mathrm{b} / \mathrm{w}$ stages
iii) Increase looser element into the element.

* To achieve stability the professor Hazettile introduced a circuit in which the troublesome effects of the $\mathrm{c}_{\mathrm{bc}}$ was neutralized by introducing a signal coupled through the $\mathrm{C}_{\mathrm{bc}}$.


## HAZELTINE NEUTRALIZATION:-

* This is the neutralization technique employed in tuned RF amplifier to maintain stability .
* The undesired effect of collector to baEinggacraeceofthe transistor is neutralized by introducing a signal which cancels the signal coupled through the collector to base capacitance
* This is achieved by a small variable capacitance $\left(\mathrm{C}_{\mathrm{N}}\right)$ is connected from the bottom of coil to the base of the transistor .It introduce a signal to the base of the transistor such that it cancels out the signal fed to the base by Cbc
* By properly adjusted Cn exactly neutralized achived.
* Modified version of Hazeltine neutralization called neutron dyneneutralization.



## NEUTRODYNE NEUTRALIZATION:-

* In a neutrodyne neutralization technique, Cn is connected to the centre trapped to the secondary coil.
* Hence it is connected with Vcc which ensures that it is insensitivity to any variation is supply voltage Vcc. Hence provided higher neutralization for the tuned amplifier.
* In principle, the circuit functions are the same manner as the hazeltine neutralizing capacitor does not have the supply voltage across it.



## Power amplifiers -Types (Oualitative analysis).

## 11. Write a short notes on Power amplifier.(Nov/Dec 2017)

- A power amplifier is an amplifier, which is capable to providing a large amount of power to the load such as loudspeaker, or motor etc.
- It is essential in almost all electronic systemggheeeadare amount of power is required to be supplied to the load.
- The power amplifier, is used as a last stage in a electronic system. For example, a public address system (PAS) consists of a microphone, a multistage amplifier, a power amplifier and a loudspeaker.
- The microphone converts the sound waves into electrical signal, which is of very low voltage (usually of few millivolts).
- This signal is insufficient to drive the loudspeaker. Therefore this signal is first raised to a sufficiently high value (a few volts) by passing it through a multistage small-signal (or voltage) amplifier.
- This signal is then used to drive the power amplifier, because it is incapable of delivering a large amount of power to the loudspeakers.
- A power amplifier is more commonly known as audio amplifier. The audio amplifiers are used in public address system, tape recorders, stereo systems, television receivers, radio receivers, broadcast transmitters etc.
- It will be interesting to know that a power amplifier dies not actually amplify the power. As a matter of fact, it takes power from the d.c. power supply connected to the output circuit and converts it into useful a.c. signal power.
- The power is fed to the load. The type of a.c. power developed, at the output of a power amplifier, is controlled by the input signal.
- Thus we can say that actually a power amplifier is a d.c. to a.c. power converter, whose action is controlled by the input signal.
- The power amplifiers, are also known as large signal amplifiers.
- The term 'large signal' for the power amplifiers arises because these amplifiers use a large part of their a.c. load line for operation.
- It is in contrast to the small signal amplifiers, which use only $10 \%$ of their a.c. load line for operation. The small signal amplifiers are commonly known as voltage amplifiers.


## 12. Explain in detail the various types of power amplifier. (OR) Explain with circuit diagram class B power amplifier and derive for its efficiency (Nov/Dec2015)(May 2017)(Nov/Dec-2017) i. Class-A amplifier:

- A class-A amplifier is one in which the operating point and the input signal are such that the current in the output circuit, flows at all times.
- A class-A amplifier operates essentially over a linear portion of its characteristics.
- In class-A operation, the transistor stays in the active region throughout the a.c cycle.
- The point and the input signal are such as to make the output current flows for $360^{\circ}$.
- Voltage gain: The voltage gain for a class-A amplifier may be obtained in the same way as the small-signal amplifier. It is given by the relation,

$$
A_{v}=\frac{r_{L}}{r_{e}}
$$

$r_{L}=$ A.C. load resistance whose value is equal to the parallel combination of collector resistance ( $R_{c}$ ) and load resistance ( $R_{L}$ ).
$r_{e}=\mathrm{A} . \mathrm{C}$. emitter diode resistance.

- Current gain: the current gain of atrmogigioneetbontio of a.c. collector current ( $i_{c}$ ) to the a.c. base current ( $i_{b}$ ).

$$
A_{i}=\frac{i c}{i_{b}}=\beta
$$

- Power gain: The a.c. input power to the base of transistor,

$$
P_{i n}=V_{i n} \cdot i_{b}
$$

And the a.c. output power from the collector.

$$
P_{o}=-V_{o} . i_{c}
$$

- The negative sign in the above equation indicates that the phase of input signal is reversed at the output.

$$
\text { Power gain, } \begin{aligned}
A_{p} & =\frac{P_{o}}{P_{i n}}=\frac{-V_{o} \cdot i_{c}}{V_{i n} \cdot \dot{b}}=-\frac{V_{o}}{V_{i n}} \mathrm{x}^{\frac{i_{c}}{i_{b}}} \\
& =-A_{v} \cdot A=-\frac{r_{L}}{r_{e}} \times \beta
\end{aligned}
$$

Where $\quad A_{v}=$ voltage gain, and

$$
A_{i}=\text { current gain. }
$$

- The overall efficiency or circuit efficiency of the amplifier circuit is defined as the ratio of a.c. power delivered to the load to the total power supplied by the d.c. source.
- Mathematically, the overall efficiency,

$$
\eta_{o}=\frac{\text { a.c.power delivered to the load }}{\text { Total power supplied by the d.c. source }}=\frac{V_{C E Q} \cdot I_{C Q}}{2 V_{C C} \cdot I_{C Q}}
$$

- Maximum value of overall efficiency,

$$
\eta_{o(\max )}=\frac{V_{C E Q} \cdot I_{C O}}{2\left(V_{C E Q} \cdot I_{C Q}\right)}=0.25=25 \%
$$

- The collector efficiency of the amplifier circuit is defined as the ratio of a.c. power delivered to the load, to the power supplied by thed.c. source to the transistor.
- Mathematically, collector circuit efficiency,

$$
\eta_{c}=\frac{\text { a.c.power delivered to the load }}{\text { power supplied by the d.c.source to the transistor }}
$$

- Maximum value of collector efficiency,

$$
\eta_{c(\text { max })}=\frac{V_{C E O I} I_{C O}}{2\left(V_{C E Q} I I_{C Q}\right)}=0.5=50 \%
$$



Figure: classification of amplifiers based on the biasing condition

## ii. Class-B amplifier:

- A class-B amplifier is one in which the operating point is at an extreme end of its characteristics, so that the quiescent power is very small.
- Hence either the quiescent current or the quiescent voltage is approximately one half a cycle.
- In class-B operation, the transistor stays in the active region only for half the cycle. The Q-point is fixed at the cut-off point of the characteristics.
- The output current flows for $180^{\circ}$.
- D.C. input power: the input power comes from the d.c. source (i.e., the $V C C$ supply) and is given by the relation,

$$
P_{i n(d c)}=V_{C C} \cdot I_{d c}
$$

Where $I_{d c}$ is the average value of current drawn from the $V C c$ supply.

- D.C. power loss in load resistor: Its value is given by the relation,

$$
\mathrm{P}_{\mathrm{RL}(\mathrm{dc})}=\mathrm{I}_{\mathrm{dc}}^{2} \cdot \mathrm{R}_{\mathrm{L}}
$$

- A.C. output power in load resistor: Its value is given by the relation,
$P_{o(a c)}=\mathrm{I}^{2} \cdot \mathrm{R}_{\mathrm{L}}=\mathrm{V}^{2} / \mathrm{R}_{\mathrm{L}}$
Where $\quad I=$ the r.m.s. value of a.c. output current,
$\mathrm{V}=$ Ther.m.s. value of a.c. output voltage, and
$V_{P}=$ The peak value of a.c. output voltage.
- Power dissipated within the resistor: Its value is given by the relation,

$$
\mathrm{P}_{\mathrm{c}(\mathrm{dc})}=\mathrm{P}_{\mathrm{in}(\mathrm{dc})}-\mathrm{P}_{\mathrm{RL}(\mathrm{dc})}-P_{o(a c)}
$$

- Overall efficiency: $\eta_{o}=\frac{P_{o(a c)}}{P_{i n(d c)}}=\frac{P_{o}}{V_{C C} \cdot I_{d c}}$
- Maximum value of overall efficiency,

$$
\eta_{o}=\frac{P_{o(a c)}}{P_{i n(d c)}}=\frac{{ }^{\frac{1}{4}} V_{C P} \cdot I_{C P}}{V_{C C} \cdot I_{d c}}=0.785=78.5 \%
$$

## iii. Class-AB amplifier:

- A class-AB amplifier is one operating point between class A and class B.
- Hence the output signal is zero for part but less than one-half of an input sinusoidal signal cycle.
- The output current flows for more than $180^{\circ}$ but less than $360^{\circ}$.
- a.c. power delivered to the load resistor,

$$
P_{o(a c)}=V_{C} \cdot I_{C}=\left(\frac{V \underline{P}}{\sqrt{2}}\right) \cdot\left(\frac{I \underline{p}}{\sqrt{2}}\right)=\frac{V_{P \cdot L \underline{P}}}{2}
$$

- And total power dissipation of the two transistors,

$$
\begin{aligned}
2 P_{C(d c)} & =P_{i n(d c)}-P_{o(a c)}=V_{C} r \cdot l-\frac{V_{P \cdot} \underline{I p}}{2} \\
& =V{ }_{C C} \cdot \frac{2 I_{p}}{\pi}-\frac{V_{P \cdot L} \underline{p}}{2} \\
& =2 I_{P}\left(\frac{V C C}{\pi}-\frac{V_{p}}{4}\right)
\end{aligned}
$$

- Overall efficiency,

$$
\eta_{o}=\frac{P^{o(a c)}}{P_{i n(d c)}}=\frac{\frac{V_{P . P}}{2}}{V_{C C}^{2} \cdot \frac{2 I_{P}}{\pi}}=\frac{\pi}{4} \cdot \frac{V}{V_{C C}}=0.785 \stackrel{V}{\frac{P}{V C}}
$$

- For the largest possible output signal, the peak value of the output voltage is equal to the $V C C$ supply (i.e., $V_{P}=V_{C C}$ ). In the case, the overall efficiency is maximum, and its value,

$$
\eta_{o(\max )}=0.785=78.5 \%
$$

- The value of collector efficiency is equal to the overall efficiency, whose maximum value is also $78.5 \%$.


## iv. Class-C amplifier:

- A class-C amplifier is one in which the operating point is chosen so that the output current (or voltage) is zero for more than one-half of an input sinusoidal signal cycle.
- In class-C amplifier, the Q-point is fixed beyond the extreme end of the characteristics. The output current remains zero for more than half cycle.
- The unturned audio or video voltage atigigite. ©canstive load is operated as small signal amplifier under class-A operation.
- class-B amplifiers are mostly used for power amplification in push-pull arrangement.
- class-AB and class-B operation are used with unturned power amplifiers, whereas class-C operation is used with tuned radio frequency amplifiers.


## Additional Questions:

## Explain briefly about push-pull amplifier <br> * Introduction:

- This means one in on and another one is off.
- It needs same type of transistors( i.e., NPN or PNP ).
- Also it needs two transformers in both input and output sides.
- One is input transformer and other is called output transformer.
- Input is applied to input driver transformer's primary winding.
- Both transformers (input and output) is centre tapped one.
- Both are NPN means voltage $\mathrm{V}_{\mathrm{CC}}$ is positive.
- Both are PNP means voltage $\mathrm{V}_{\mathrm{CC}}$ is negative.


## * Basic principle of operation:



Figure: Basic operation diagram

- During the positive half cycle of the applied input $\mathrm{Q}_{1}$ is only under ON condition. The positive half cycle is across the load.
- Similarly, During the Negative half cycle of the applied input $\mathrm{Q}_{2}$ is only under ON condition. So the Negative half cycle is across the load.


## * Push-pull class-B amplifier:



Figure: Push-pull amplifier- class-B

- In the above circuit, both transistors is of NPN type.
- If both are PNP, the supply voltage must be $-\mathrm{V}_{\mathrm{CC}}$. but basic diagram is same.
- Input driver transfer driver circuit drives the circuit, then the input signal is applied to the primary of the driver transformer.
- The centre tap on the secondary of the driver transformer is grounded. The centre tap on the primary of the output transformer is connected to the supply voltage $+\mathrm{V}_{\mathrm{CC}}$.
- Whenever the input signal is under positive half cycle, when point A is positive with respect to B , then the transistor $\mathrm{Q}_{1}$ is in the active region. But $\mathrm{Q}_{2}$ is under in OFF condition now.So the load gets this positive voltage drop output across it.
- Then, point B is positive with respect to A under negative half cycle. So, $\mathrm{Q}_{1}$ is in the OFF condition.so the load gets voltage in negative across it due to negative voltage. This is shown in the waveform.
- For the output transformer, the number of turns of each half of the primary is $\mathrm{N}_{1}$. But in the secondary, it is $\mathrm{N}_{2}$.
- Hence, the total number of turns in primary side of output transformer is $2 \mathrm{~N}_{1}$.
- Then turns ratio is $2 \mathrm{~N}_{1}: \mathrm{N}_{2}$.
- D.C operation:
$\checkmark$ The Q-point is adjusted on the X-axis such that, $\mathrm{V}_{\text {CEQ }}=\mathrm{V}_{\text {CC }}$ and $\mathrm{I}_{\text {CEQ }}$ is zero. The coordinates of the Q-point are $\left(\mathrm{V}_{\mathrm{CC}}, 0\right)$. There is no d.c base bias voltage.
- D.C power input:
$\checkmark$ Each transistor output is in the form of half rectified waveform. Hence, if $\mathrm{I}_{\mathrm{m}}$ is the peak value of the output current of each transistor, the dc or $A_{V}$ value is $\frac{I_{m}}{\pi}$, due to half rectified waveform.
$\checkmark$ Then, two currents drawn by the two transistors, form the A.C supply are in the same direction.
$\checkmark$ Therefore, the total D.C or average current drawn from the A.C supply is algebraic sum of the individual average current drawn by each transistor,

$$
\begin{equation*}
\mathrm{I}_{\mathrm{dc}}=\frac{I_{m}}{\pi}+\frac{I_{m}}{\pi}=\frac{2 I_{m} \ldots}{\pi} \tag{1}
\end{equation*}
$$

$\checkmark$ The total d.c power input is given by,

$$
\begin{align*}
& \mathrm{P}_{\mathrm{dc}}=\mathrm{V}_{\mathrm{CC}} * \mathrm{I}_{\mathrm{dc}},  \tag{2}\\
& \mathrm{P}_{\mathrm{dc}}=\frac{{ }_{2}}{\pi} \mathrm{~V}_{\mathrm{CC}} \cdot \mathrm{I}_{\mathrm{m} \ldots} \tag{3}
\end{align*}
$$



Figure: Waveform output

- A.C operation:
$\checkmark$ When A.C signal is applied to the input driver transformer, for positive half cycle $\mathrm{Q}_{1}$ transistor is under ON condition. Then, its current flow path is shown in the following diagram.

(i) + ve half cycle

(ii) - ve half cycle

Figure: current path
$\checkmark$ From the above figure, when $\mathrm{Q}_{1}$ conducts, lower half of the primary of the input transformer does not carry any current. Hence. Only $\mathrm{N}_{1}$ number of turns carry the current.
$\checkmark$ While, when $\mathrm{Q}_{2}$ conducts, upper half of the primary does not carry any current. Therefore again only $\mathrm{N}_{1}$ number of turns carry the current.
$\checkmark$ Hence, the reflection on the primary can be written as,

$$
\begin{equation*}
\mathrm{R}_{\mathrm{L}}^{\prime}=\frac{R_{L}}{{ }_{\mathrm{n} . \mathrm{n}}} \ldots \ldots . \text { (4) and } \mathrm{n}=\frac{N_{2}}{N_{1}} \tag{5}
\end{equation*}
$$

$\checkmark$ Note that the step down turns ratio is $2 \mathrm{~N}_{1}: \mathrm{N}_{2}$ but while calculating the reflected load, the ratio n becomes $\mathrm{N}_{2}: \mathrm{N}_{1}$.
$\checkmark$ So each transistor shares equal load which is the reflected load $\mathrm{R}_{\mathrm{L}}{ }^{\prime}$.
$\checkmark$ The slope of the a.c load line is $\underset{\mathrm{RL}^{\prime}}{\text { Ehgghine由eodmoad line istheverticalline passing through the }}$ Q on the X -axis. The load lines are shown below.


Figure: load lines for push-pull class B amplifier
$\checkmark$ The slope of the a.c load line (magnitude of slope) can be represented in terms of $\mathrm{V}_{\mathrm{m}}$ and $\mathrm{I}_{\mathrm{m}}$, $\frac{1}{\mathrm{RL}^{\prime}}=\frac{I m}{V_{m}}$

$$
\begin{equation*}
\mathrm{R}_{\mathrm{L}}{ }^{\prime}=\frac{V_{m}}{I_{m}} . \tag{6}
\end{equation*}
$$

Here, $\mathrm{V}_{\mathrm{m}}=$ peak value of the collector circuit

- A.C power output:
$\checkmark$ As $I_{m}$ and $V_{m}$ are the peak values of the output current and the output voltage respectively.
Then

$$
\mathrm{V}_{\mathrm{rms}}=\frac{V_{m}}{\sqrt{2}} \ldots . \text { (8) andI } \mathrm{I}_{\mathrm{rms}}=\frac{I_{m}}{\sqrt{2}} \ldots \ldots \text { (9) }
$$

The power output is, $\mathrm{P}_{\mathrm{ac}}=\mathrm{V}_{\mathrm{rms}} . \mathrm{I}_{\mathrm{rms}}$

$$
\begin{align*}
= & \mathrm{I}_{\mathrm{rms}} \cdot \mathrm{R}_{\mathrm{L}}{ }^{\prime} \cdot \mathrm{I}_{\mathrm{rms}} \\
& =\mathrm{I}_{\mathrm{rms}}{ }^{2} \cdot \mathrm{R}_{\mathrm{L}}^{\prime} \cdots  \tag{10}\\
& =\mathrm{V}_{\mathrm{rms}}^{2} / \mathrm{R}_{\mathrm{L}}{ }^{\prime}
\end{align*}
$$

- Efficiency: The efficiency of class-B amplifier can be calculated as follows:

$$
\begin{align*}
\mathbf{\%} \boldsymbol{\eta} & =\frac{P_{1 a c}}{P_{d c}} \times 100 \ldots \ldots . . . . . . . . . .  \tag{11}\\
& =\frac{\frac{V_{m I_{m}}}{2}}{V_{C C} \cdot I_{m}} * 100 \ldots \ldots . \\
& =\frac{\pi V m}{4 V C C} * 100 \ldots \ldots . . \tag{12}
\end{align*}
$$

## - Maximum efficiency:

$\checkmark$ As the peak value of the collector voltage $\mathrm{V}_{\mathrm{m}}$ increases, the efficiency also increases.
$\checkmark$ Then the maximum value of $\mathrm{V}_{\mathrm{m}}$ is possible which is equal to $\mathrm{V}_{\mathrm{CC}}$.

$$
\begin{aligned}
\% \eta_{\max } & =\frac{P_{a c} * 100}{P_{d c}} \\
& =\frac{\pi V m}{4 V c C} * 100=78.5 \%
\end{aligned}
$$

 voltage if Vs1=70mV peak to peak at 1 Khz and $V \mathrm{~m} 2=40 \mathrm{mV}$ peak to peak at 1 Khz of dual input balanced output differential amplitude $\mathbf{h}_{\mathrm{ie}}=\mathbf{2 . 8} \mathrm{K} \Omega$.(Nov/Dec 2016)


1. Operating point value are $I_{C Q}, V_{C E Q}$. Apply KVL to input side.

$$
-I_{B} R s-V_{B E}-2 R_{E} I_{E}+V_{E E}=0
$$

$$
\begin{gathered}
\frac{-I_{E}}{\beta} R s-V_{B E}-2 R_{E} I_{E}+V_{E E}=0 \\
I_{E}=\frac{V_{E E}-V_{B E}}{2 R_{E}+\frac{R_{S}}{\beta}} \\
\beta=h_{f e}=100 \\
I_{E}=\frac{15-0.7}{2 \times 6.8 \times 10^{3}+\frac{100}{100}}=1.051 \mathrm{~mA} \\
I_{C}=I_{E}=1.051 \mathrm{~mA}
\end{gathered}
$$

$$
V_{C E}=V_{C C}+V_{B E}-I_{C} R_{C}=15+0.7-1.051 \times 10^{-3} \times 4.7 \times 10^{3}
$$

$$
\therefore V_{C E Q}=10.758 \mathrm{~V}
$$

Differential gain, Al

$$
=\frac{h_{f e} \underline{R_{C}}}{R_{S}+h_{i e}}
$$

$$
A_{d}=\frac{100 \times 4.7 \times 10^{3}}{100+2.8 \times 10^{3}}=162.068
$$

Common mode gain,

$$
=\frac{h_{f e} \underline{R}_{c}}{2 R_{E}\left(1+h_{f e}\right)+R_{s}+h_{i e}}
$$

$$
A_{C}=\frac{100 \times 4.7 \times 10^{3}}{2 \times 6.8 \times 10^{3}(1+100)+100+2.8 \times 10^{3}}
$$

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$$
\begin{gathered}
C M R R=\frac{A_{d}}{A_{c}}=\frac{162.068}{0.3414}=474.652 \\
\therefore C M R R=20 \log (474.652)=53.527 \mathrm{~dB}
\end{gathered}
$$

Output voltage, $\quad V_{o}=A_{d} V_{d}+A_{c} V_{c}$

$$
\begin{aligned}
& \quad V_{d}=V_{s 1}-V_{s 2}=70-40=30 \mathrm{mV}(P-P) \\
& V_{c}=\frac{V_{s 1}+V_{s 2}}{2}=\frac{70+40}{2}=55 \mathrm{mV}(P-P) \\
& V_{o}=162.068 \times 30 \times 10^{-3}+55 \times 10^{-3} \times 0.3414 \\
& =4.86204+0.0187 \\
& =4.88 \mathrm{~V}(\text { Peak }- \text { Peak })
\end{aligned}
$$

14. A parallel resonant circuit has a capacitor of 250 pF in one branch and inductance of 1.2 mH and a resistance of $10 \Omega$ in parallel branch. Find (1). Resonant frequency (2). Impedance of the circuit at resonance (3). Q-factor of the circuit. (Nov/Dec 2018)
Solution:
i. Resonant frequency of the parallel tuned circuit is defined as,

$$
f_{r}=\frac{1}{2 \pi} \sqrt{\frac{f_{r}=\frac{1}{2 \pi} \sqrt{\frac{1}{L C}-\frac{R^{2}}{L^{2}}}}{1.25 \times 10^{-3} \times 250 \times 10^{-12}}-\frac{10 \times 10}{\left(1.25 \times 10^{-3}\right)^{2}}}
$$

$f_{r}=\frac{1}{2 \pi} \times 178836.493=284.7 \times 10^{3} \mathrm{~Hz}$

$$
\mathbf{f}_{\mathrm{r}}=284.7 \mathrm{KHz}
$$

ii. Impedance of the circuit, $\mathrm{Z}_{\mathrm{r}}$ is given by,

$$
\begin{aligned}
& \quad Z_{r}=\frac{L}{R C}=\frac{1.25 \times 10^{-3}}{250 \times 10^{-12} \times 10} \\
& \mathrm{Z}_{\mathrm{r}}=500000 \\
& \mathbf{Z}_{\mathbf{r}}=\mathbf{5 0 0} \mathbf{~ K} \mathbf{\Omega}
\end{aligned}
$$

iii.Q-factor of the circuit is defined as,

$$
\begin{gathered}
Q=\frac{2 \pi f_{r} L}{R}=\frac{2 \pi \times 284.7 \times 10^{3} \times 1.25 \times 10^{-3}}{10}=\frac{2236.02}{10}=223.6 \\
\mathbf{Q}=\mathbf{2 2 3 . 6}
\end{gathered}
$$

15. Compare voltage and power amplifiers. (Evqdyefeel8dm

| Voltage Amplifier |  | Power Amplifier |  |
| :---: | :--- | :---: | :--- |
| 1. | The amplitude of input A.C signal is small | 1. | The amplitude of A.C signal is large. |
| 2. | The collector current is low (about 1 mA ) | 2. | The collector current is very high (greater <br> than 100 mA ) |
| 3. | RC coupling is used. | 3. | Transformer coupling is used |
| 4. | The A.C power output is low | 4. | The A.C power output is high |
| 5. | Heat dissipation is less | 5. | Heat dissipation is high |
| 6. | The size of power transistor is small | 6. | The size of power transistor is large |
| 7. | Current gain is low | 7. | Current gain is high |
| 8. | Output impedance is high | 8. | Output impedance is low |

## 16. Explain the self-biasing of a JFET. (Nov/Dec 2018)

- Self-bias is the most common type of JFET bias. Recall that a JFET must be operated such that the gate source junction is always reverse-biased.
- The condition requires a negative $\mathrm{V}_{\mathrm{GS}}$ for an n-channel JFET and a positive $\mathrm{V}_{\mathrm{GS}}$ for p -channel JFET. This can be achieved using the self-bias arrangement shown in Fig. 1
- The gate resistor, $\mathrm{R}_{\mathrm{G}}$, does not affect the bias because it has essentially no voltage drop across it; and therefore the gate remains at 0 V .
- $\mathrm{R}_{\mathrm{G}}$ is necessary only to isolate an A.C. signal from ground in amplifier applications.
- The voltage drop across resistor, $\mathrm{R}_{S}$ makes gate source junction reverse biased.


Fig 1: self-bias circuit for JFET
Step 1: Obtain expression for $\mathrm{V}_{\mathrm{GS}}$

- For the $n$-channel FET in Fig. 1(a), $I_{S}$ produces a voltage drop across $R_{S}$ and makes the source positive with respect to ground. Since $I_{S}=I_{D}$ and $V_{G}=0$, then $V_{S}=I_{S} R_{S}=I_{D} R_{S}$. The gate to source voltage is, $\mathrm{V}_{\mathrm{GS}}=\mathrm{V}_{\mathrm{G}}-\mathrm{V}_{\mathrm{S}}=0-\mathrm{I}_{\mathrm{D}} \mathrm{R}_{\mathrm{S}}=-\mathrm{I}_{\mathrm{D}} \mathrm{R}_{\mathrm{S}}$
- For the p-channel FET in Fig. 1(b), Is produces a voltage drop across $\mathrm{R}_{\mathrm{S}}$ and makes the source negative with respect to ground. Since $I_{S}=I_{D}$ and $V_{G}=0$, then $V_{S}=-I_{S} R_{S}=-I_{D} R_{S}$ the gate to source voltage is $\mathrm{V}_{\mathrm{GS}}=\mathrm{V}_{\mathrm{G}}-\mathrm{V}_{\mathrm{S}}=0-\left(-\mathrm{I}_{\mathrm{D}} \mathrm{R}_{\mathrm{S}}\right)=+\mathrm{I}_{\mathrm{D}} \mathrm{R}_{\mathrm{S}}$
- In the following D.C. analysis, the n-channel JEEnggnireeicom is used to for illustration.
- For D.C. analysis we can replace coupling capacitors by open circuits and we can also replace the resistor $\mathrm{R}_{\mathrm{G}}$ by a short circuit equivalent, since $\mathrm{I}_{\mathrm{G}}=0$. This is illustrated in Fig.2.


Fig 2: Simplified self-bias circuit for dc analysis
Step 2: Calculate $I_{D Q}$

$$
I_{D}=I_{D S S}\left[1-\frac{V_{G S}}{V_{P}}\right]
$$

Substituting value of $\mathrm{V}_{\mathrm{GS}}$ in above equation we get,

$$
I_{D}=I_{D S S}\left[1-\frac{-I_{D} R S^{2}}{V_{P}}\right]^{2}=I_{D S S}\left[1+\frac{I_{D} R S_{S}}{V_{P}}\right]^{2}
$$

Step 3: Calculate $V_{D S}$
Applying KVL to the output circuit we get,

$$
\begin{aligned}
& V S+V_{D S}+I_{D} R_{D}-V_{D D}=0 \\
& \qquad V_{D S}=V_{D D}-V_{S}-I_{D} R_{D}=V_{D D}-I_{D} R s-I_{D} R_{D}=V_{D D}-I_{D}\left(R_{s}+R_{D}\right)
\end{aligned}
$$

## UNIT-V FEEDBACK AMPLIFIERS AND OSCILLATORS

## PART-A

## FEEDBACK AMPLIFIERS

1. Define feedback and feedback factor. Define Positive feedback and Negative feedback.

Feedback: The process of injecting a fraction of the output voltage of an amplifier into the input so that it becomes a part of the input is known as feedback.

Feedback Factor: Feedback factor is defined as the ratio of feedback signal (Voltage/Current) to the amplifier output which is given as input to the feedback network. Hence, it is also called as feedback ratio and is denoted by $\beta$.
i.e., $\beta=\frac{V_{f}}{V_{o}} ; \quad V_{f}$-Feedback Voltage $\quad V_{o}$ - Amplifier Output Voltage

Positive feedback: If the feedback voltage is in-phase to the input from the source, i.e., feedback signal in-phase with the original input signal. It is called positive feedback.

Negative feedback: If the feedback voltage is opposite (out of phase) to the input from the source, i.e., feedback signal opposes the original input signal. It is called negative or degenerative feedback.

## Advantages of negative feedback

2. Mention/List the advantages of negative feedback circuits. (Nov/Dec2015), (May/June2016)
$>$ In negative feedback amplifiers, the voltage gain of the amplifier remains stable.
$>$ High input resistance of a voltage amplifier can be made larger
> Low output resistance of a voltage amplified can be lowered
$>$ Frequency response improves
$>$ Significant improvement in the linearity of operation
$>$ The transfer gain of the amplifier with feedback can be stabilized against variation in the h parameters.
3. Write the disadvantages of negative feedback in amplifier circuits and how it can be overcome? (April/May 2015) The main disadvantage of using negative or degenerative feedback in amplifier is Reduction in Gain.
The required Gain can be attained by increasing the number of amplifier stages
4. What are the effects of a negative feedback?
a) Reduces noise
b) Reduces distortion
c) Reduces gain
d) Increases band width
e) The gain becomes stabilized with respect to changes in the amplifier active device parameters like $h_{f e}$.
f) The non-linear distortion is reduced there by increasing the signal handling capacity or the dynamic range of the amplifier.
5. What is the condition required for satisfactory operation of a negative feedback amplifier? (Apri//May 2019) The open-loop voltage gain must be much greater than the required closed-loop gain. Overall Voltage Gain with -ve feedback (Closed-loop Gain), $A_{v f}=\frac{A_{v}}{1+\beta A_{v}}$

$$
A_{v f}=\frac{A_{v}}{\beta A_{v}} \quad\left\{\text { Since, } \beta A_{v} \gg 1\right\}
$$

Therefore, $A_{v f}=\frac{1}{\beta}$
\{Where $A_{v}$ is the voltage gain without a feedback and $\beta$ is the feedback factor is due to negative feedback the gain is reduced by factor $1+\beta A_{v}$ \}

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6. With negative feedback the bandwidth of the amplifier increases- True/False?

True.
Bandwidth of amplifier with feedback is greater than bandwidth of amplifier without feedback.

## Voltage / current, Series, Shunt feedback

7. Mention the four connections in Feedback.
a. Voltage series feedback.
b. Voltage shunts feedback.
c. Current series feedback.
d. Current shunt feedback.
8. Explain the voltage series feedback.

In this case, the feedback voltage is derived from the output voltage and fed in series with input signal. The input of the amplifier and the feedback network are in series is also known as series parallel in parallel, hence this configuration is also known as series parallel feedback network.
9. Explain the voltage shunt feedback.

The input of amplifier and the feedback network are in parallel and known as parallel -parallel feedback network. This type of feedback to the ideal current to voltage converter, a circulating having very low input impedance and very low output impedance.

## 10. Explain the current series feedback.

When the feedback voltage derived from the load current and is fed in series with the input signal, the feedback is said to be current series feedback, the inputs of the amplifier and the feedback network are in series and the output are also in series. This configuration is also called as series-series feedback configuration.

## 11. Explain the current shunt feedback.

When the feedback voltage is derived from the load current and a fed in parallel with the input signal, the feedback is said to be current shunt feedback. Here in the inputs of the amplifier and the feedback network are in parallel and the outputs are in series. This configuration is also known as parallel series feedback.
12. Which is the most commonly used feedback arrangement in cascaded amplifier and why? (Nov/Dec-2013-R13) A voltage series feedback s commonly used in cascaded amplifiers. Since, it has high input impedance and low output impedance that is needed for cascaded amplifiers.

## Positive feedback (Oscillators)

## 13. What is Oscillator?

Oscillator is an electronic device which generates electrical oscillations (i.e., repeated waveforms) of required frequency. It is used for converting DC energy into AC energy of the desired frequency.
\{An oscillator is a circuit which generates an alternating voltage without any input signal. Instead of external input signal, it uses feedback path through which it provides its own input signal.
It is used for converting DC energy into AC energy of the desired frequency.]

## 14. What are sustained Oscillations?

Electrical oscillations in which amplitude does not change with time are called sustained oscillations. It is called as undamped oscillations.

## 15. What is frequency of Oscillations?

The frequency at which circuit satisfies both the Barkhausen conditions i.e. $|A \beta|=1$ and $\angle A \beta=0^{\circ}$ or $360^{\circ}$ simultaneously is called frequency of oscillations
16. Classify the various oscillators based on the output waveforms, circuit components, operating frequencies and feedback used.

According to the nature of waveform generated.

1. Sinusoidal or Harmonic Oscillators
2. Non-sinusoidal or Relaxation oscillators

Based on circuit components. (Nov/Dec 2017)
According to the frequency determining networks,

1. RC oscillators (Phase-shift Oscillator and Wien Bridge Oscillator)
2. LC oscillators (Hartley Oscillator and Colpitts Oscillator)
3. Crystal oscillators

## According to the frequency of the Generated Signals

1. AFO (Audio Frequency Oscillators) - upto 20 KHz
2. RFO (Radio Frequency Oscillators) -20 KHz to 30 MHz
3. VHFO (Very High Frequency Oscillators) -30 MHz to 300 MHz
4. UHFO (Ultra High Frequency Oscillators) - 300 MHz to 3 GHz
5. MFO (Microwave Frequency Oscillators) - above 3 GHz
6. What are the types of sinusoidal oscillator? [or] Mention the different types of sinusoidal oscillator?
a) RC phase shift Oscillator.
b) Wein bridge Oscillator.
c) Hartley Oscillator
d) Colpitts Oscillator
e) Crystal Oscillator

## 18. Name two low frequency oscillators?

a) RC phase shift oscillator.
b) Wein bridge oscillator.

## 19. Name three high frequency oscillators?

The high frequency oscillators are
a) Hartley oscillator.
b) Colpitts oscillator.
c) Crystal oscillator

## Condition for oscillations

20. Write the conditions for a Oscillator. (OR)

State. Barkhausen criterion (Barkhausen condition) for sustained oscillations. (Nov/Dec-2012,2011,09), (May/June2016) (Nov/Dec-2016) (May 2017)
The Barkhausen criterion for obtaining sustained oscillations,

1. The feedback voltage must be in-phase with the input, i.e., total phase-shift around the closed-loop must be $0^{\circ}$ or $360^{\circ}$, and
2. Magnitude of the loop gain must be unity i.e., $|A \beta|=1$

Where, A - Open loop Gain of the system \& $\beta$ - Feedback ratio.

## Phase Shift and Wien bridge oscillator (RC oscillators)

21. Why an RC phase shift oscillator is called so?

An RC network products $180^{\circ}$ phase shift. Hence it is called RC phase shift oscillator.
22. List the advantages of phase shift oscillator. (May/June-2012)

- The phase shift oscillator does not required conductance or transformers.
- It is suitable for the low frequency range i.e., from a few hertz to several 100 kHz . The upper frequency is limited because the impedance of RC network may become so small that it loads the amplifier heavily.

23. Write the disadvantages of Phase shift oscillator.
1.It is necessary to change the C or R in all the three RC networks simultaneously for changing the frequency of oscillations. This is practically difficult.
24. It is not suitable for high frequencies.

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24. Which oscillator uses both positive and negative feedback?

Wien bridge oscillator.

## Hartley and Colpitts oscillators. (LC oscillators)

25. Distinguish between LC and RC oscillator.

| LC Oscillator | RC Oscillator |
| :--- | :--- |
| It operates at high frequencies | It operates at low frequencies |
| It is suitable for RF only | It is suitable for AF only |
| Frequency is variable | The frequency is constant. <br> It is known as fixed frequency oscillator. |

26. Write the main drawback of LC oscillators.
27. The frequency stability is not very good.
28. They are too bulky and expensive and cannot be used to generate low frequencies.
29. What is the advantage of a colpitts oscillator compared to a phase shift oscillator? (Nov/Dec 2015)
ii) The advantage of colpitts oscillator is the frequency of oscillation is very high.
iii) We can vary the frequency of oscillation.

## Crystal oscillators.

28. What is piezo electric effect? (May/June-2013)

The piezo electric crystal exhibits a property, that is, if a mechanical stress is applied across one face, an electrical potential is developed across the opposite face. The inverse is also true. This phenomenon is called piezo-electric effect.
29. Why Quartz crystal is commonly used in crystal oscillator?

Quartz crystals are generally used in crystal oscillator because of their great mechanical strength, simplicity of manufacture and abeyance to the piezo electric effect accurately.
30. What are the advantages of crystal oscillators? (NOV/DEC 2012)

The advantages of crystal oscillators are
a) Excellent frequency stability.
b) High frequency of operation
c) Automatic amplitude control.
d) It is suitable for only low power circuits
e) Large amplitude of vibrations may crack the crystal.
f) It large in frequency is only possible replacing the crystal with another one by different frequency.
31. An oscillator operating at 1 MHz has a stability of 1 in $10^{4}$. What will be the minimum value of frequency generated? (April/May 2019)
The typical frequency stability of oscillators that do not use CRYSTAL is about 1 in $10^{4}$.
The minimum value of frequency generated might be 100 KHZ or lower than 1 MHZ for the oscillator operating at 1 MHZ .
\{If the crystal is used, the frequency stability can be improved to better than 1 in $10^{6}$, which gives a $\pm 1 \mathrm{~Hz}$ variation in the output of a 1 MHz oscillator. $\}$
32. How does an oscillator differ from an amplifier? (or) Differentiate oscillator \& amplifier. [Nov/Dec 2013] [Nov/Dec 2016]

| S.No. | Oscillators | Amplifiers |
| :---: | :--- | :--- |
| 1 | They are self-generating circuits. <br> They generate waveforms like sine, square and triangular <br> waveforms of their own without having input signal. | They are not self-generating circuits. <br> They need a signal at the input and they just increase <br> the level of the input waveform. |
| 2 | It has infinite gain | It has finite gain |
| 3 | Oscillator uses positive feedback. | Amplifier uses negative feedback. |

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## 33. Compare RC Phase-Shift Oscillators and Wien Bridge Oscillator.

| 5 F . | RC phase shifl oscillator | Wen bridge oscillator |
| :---: | :---: | :---: |
| 1. | It is a phase shift osdrlator tued for lew freguency ramges | If is also a phase shith wecthater used for fow frequentif range. |
| 2 | The feedback netrour' is RC network with three RC sections: | The feedhach network is lead-lag network whtuch is called When bridge circuit. |
| 3. | The feedback netrork introduces $18 \%$ phase shift. | The feedbach network docs not introciuce any phase shift |
| 4 | Op-amp is used in an inverting mode. | Op-amp is used in non-inverting mode. |
| 5. | Op-amp circuit introduces $180^{\circ}$ phase shift. | Op-amp cricuit does not introduce any phase shift. |
| 6. | The frequency of oscillations is, $\mathrm{f}=\frac{1}{2 \pi R C \cdot \sqrt{6}}$ | The frequency of oscillations is, $f=\frac{1}{2 \pi \mathrm{KC}}$ |
| 7. | The amplifier gain condition is $\|\mathrm{A}\| \geq 29$ | The amplifier gain condition is, $\|A\| \geq 3$ |
| 8. | The frequency variation is difficult. <br> canned with <br> CamScanrier | Mounting the two capactors on common shaft and varying their values, frequency can be varied. |

## 34. Classification of Oscillators



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PART-B

## Advantages of negative feedback \& positive feedback

## 1. What is meant by feedback? What are the types of feedback and effects of negative feedback? (May/June-2012) (Nov/Dec 2017)

## Negative feedback

If $\beta$ is negative, the voltage feedback subtracts from the input yielding a lower output and reduced voltage gain. Hence this feedback is known as negative feedback.

## Positive feedback

If the phase of the voltage feedback is such as to increase the input, then $\beta$ is positive and the result is positive feedback.

## Increase Stability:

The voltage gain due to a negative feedback is given by

$$
\begin{equation*}
A_{v f}=\frac{A_{v}}{1+\beta A_{v}} \ldots \tag{1}
\end{equation*}
$$

Where $A_{v}$ is the voltage gain without a feedback and $\beta$ is the feedback factor is due to negative feedback the gain is reduced by factor $1+\beta A_{v}$

If $\beta A_{v} \gg 1$ then $\quad A_{{ }_{y}}=\frac{A_{v}}{\beta A_{v}}=\frac{1}{\beta}$
Hence the gain of the amplifier with feedback has been stabilized against such problems as ageing of a transistor or a transistor being re-placed by a transistor with a different value of $\beta$.

## Sensitivity of transfer gain:

The fractional change in amplification with feedback divided by the fractional change without feedback is called the sensitivity of the transfer gain
$\underset{d A_{v f}}{\text { From equ } 1}$

$$
\begin{aligned}
& =\frac{\left(1+\beta A_{v}\right)-A_{v} \beta}{\left(1+\beta A_{v}\right) \cdot .^{2}}=\frac{1}{\left(1+\beta A_{v}\right) \cdot .^{2}} \\
d A_{v} & \frac{d A_{v f}}{d A_{v}}=\frac{1}{\left(\left(1+\beta A_{v}\right)^{2}\right)} \\
d A_{v f} & =\frac{d A_{v}}{\left(1+\beta A_{v}\right)^{2}}
\end{aligned}
$$

Dividing both side by $A_{v f}$

$$
\frac{d A_{v f}}{A_{v f}}=\frac{d A_{v}}{\left(\left(1+\beta A_{v}\right)^{2}\right) \cdot A_{v f}}
$$

Instead of $A_{v f} \operatorname{sub} \frac{A_{v}}{1+\beta A_{v}}$ in above equation

$$
\begin{aligned}
\frac{d A_{v f}}{A_{v f}} & =\frac{d A_{v}}{\left(\left(1+\beta A_{v}\right)^{2}\right) \cdot\left(\frac{A_{v}}{1+\beta A_{v}}\right)} \\
& =\frac{d A_{v}}{A_{v}\left(1+\beta A_{v}\right)}
\end{aligned}
$$

Taking absolute value of the resultant equation we get
$\left.\frac{d A_{v f}}{A_{v f}}=\frac{1}{\left|1+\beta A_{v}\right|} \right\rvert\, \frac{d A_{v}}{A_{v}}$ .3

Sensitivity $=\frac{\frac{\left|d A_{v f}\right|}{A_{v f}}}{\left\lvert\, \frac{d A_{v}}{A_{v} \mid}\right.}=\frac{1}{\left|1+\beta A_{v}\right| \ldots \ldots . . . . . . . . . . . . . . . . . . . . . ~} 4$
The densitivity is reciprocal of sensitivity. Hence

$$
D=1+A_{v} \beta \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots . . \ldots
$$

## Frequency distortion

From equ 1 we find that for a negative feedback amplifier having $A_{v} \beta \gg 1$ the gain withfeedback is $A_{v f}=1 / \beta$. If the feedback network does not contain any reactive elements the gain is not function of frequency.

## Reduction in noise

There are many sources of noise is an amplifier. If the noise present at the output is N and the amplifier gain is A. then the noise present in the amplifier with negative feedback is
$\mathrm{N} 1=\frac{N}{1+\beta A_{v}}$.

## Reduction in distortion

Let us assume that the distortion in the absence of feedback is D . Because the effect of feedback the distortion present at the input is equal to
$D_{f}=\frac{D}{1+\beta A_{v}}$

## Bandwidth

If the bandwidth of an amplifier without feedback is given by
$\mathrm{Bw}_{\mathrm{f}}=\mathrm{BW}\left(1+\beta A_{v}\right)$
In curve a source the frequency response of an amplifier without feedback when a negative feedback is introduced the gain of the amplifier decreases.


## Frequency response of an amplifier with and without feedback

Obtain curve C. from fig we can observe that there is decrease in the lower cutoff frequency and increase in upper cutoff frequency hence the bandwidth increases. Therefore $\beta$ increases Bandwidth also increases Loop Gain

A loop gain is used to describe the product of voltage gain $A_{v}$ and feedback factor $\beta$. The amount of feedback introduced into an amplifier may be expressed in decibels according to the following definition.
$\mathrm{F}=$ feedback in db

$$
\begin{aligned}
& =20 \log \frac{A_{v f}}{A_{v}} \\
= & 20 \log \frac{1}{1+\beta A_{v}}
\end{aligned}
$$

## 2. Advantages of Negative feedback in amplifiers. (Nov/Dec 2018)

The advantages of negative feedback in amplifiers are listed as follows.

1. The negative feedback amplifiers, the voltage gain of an amplifier remains stable.
2. It reduces the non-linear distortion produced in large signal amplifiers.
3. It improves the frequency response of the amplifier.
4. It increases the stability of the circuit.
5. Negative feedback increases the input impedance and decreases the output impedance of the amplifier.
6. It decreases the noise voltage in the amplifier.
7. Negative feedback amplifier is less sensitive to variations in amplifier parameters.
8. It increases the amplifier bandwidth.
9. The input and output impedances of feedback amplifier can be adjusted to desired value.
10. It has less phase, amplitude and frequency distortion.
11. Amplifier with negative feedback operates linearly.
12. Operating point of amplifier can be stabilized.

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3. With proper mathematical derivation, proven that bandwidth increases in a negative feedback amplifier. (April/May 2019)

The negative feedback increases amplifier bandwidth which can be proven mathematically as below

## ADDITIONAL EFFECTS OF NEGATIVE FEEDBACK

## Decibels of Feedback

Negative feedback can be measured in decibels. A statement that 40 dB of feedback has been applied to an amplifier means that the amplifier gain has been reduced by 40 dB (that is, by a factor of 100). Thus,

$$
A_{\mathrm{CL}}=A_{v}-40 \mathrm{~dB}=\frac{A_{v}}{100}
$$

## Bandwidth

Consider the typical gain-frequency response of an amplifier, as illustrated in Fig. Without negative feedback, the amplifier open-loop gain $\left(A_{v}\right)$ falls off to its lower 3 dB frequency $\left(f_{1(\mathrm{OLL})}\right)$, as illustrated. This is usually due to the impedance of bypass capacitors increasing as the frequency decreases. Similarly, the open-loop upper cutoff frequency $\left(f_{2(\mathrm{OL})}\right)$ is produced by transistor cutoff, by shunting capacitance, or by a combination of both.
the circuit open-loop bandwidth is given by

$$
\mathrm{BW}_{\mathrm{OL}}=f_{2(\mathrm{OL})}-f_{1(\mathrm{OL})}
$$

Now look at the typical frequency response for the same amplifier when negative feedback is used. The closed-loop gain $\left(A_{\mathrm{CL}}\right)$ is much smaller than the open-loop gain, and $A_{\text {CL }}$ does not begin to fall off (at high or low frequen-


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cies) until $A_{v}$ (open-loop gain) falls substantially. Consequently, $f_{1(\mathrm{CL})}$ is much lower than $f_{1(\mathrm{OL})}$, and $f_{2(\mathrm{CL})}$ is much higher than $f_{2(\mathrm{OL})}$. So the circuit bandwidth with negative feedback (the closed-loop bandwidth) is much greater than the bandwidth without negative feedback.

$$
\begin{aligned}
\mathrm{BW} & f_{\mathrm{CL}} \\
A_{\mathrm{CL}}-f_{1(\mathrm{CL})} & =\frac{A_{v}}{1+A_{v} B}
\end{aligned}
$$

It can be shown that there is a $90^{\circ}$ phase shift associated with the openloop gain at frequencies below $f_{1(\mathrm{OL})}$ and above $f_{2(\mathrm{OL})}$. Thus, above Eq. must be rewritten as
or

$$
\begin{aligned}
A_{\mathrm{CL}} & =\frac{-j A_{v}}{1-j A_{v} B} \\
\left|A_{\mathrm{CL}}\right| & =\frac{A_{v}}{\sqrt{\left[1+\left(A_{v} B\right)^{2}\right]}}
\end{aligned}
$$

When $A_{v}=1 / B$,

$$
\begin{aligned}
\left|A_{\mathrm{CL}}\right| & =\frac{1 / B}{\sqrt{[1+1]}}=\frac{A_{\mathrm{CL}}}{\sqrt{2}} \\
& =A_{\mathrm{CL}}-3 \mathrm{~dB}
\end{aligned}
$$

Thus, for a negative feedback amplifier designed to have the widest possible bandwidth, the cutoff frequencies would occur when the open-loop gain falls to the equivalent of $1 / B$. Thus, $f_{2(\mathrm{CL})}$ occurs when

$$
A_{v}=1 / B \approx A_{\mathrm{CL}}
$$

So, for example, the cutoff frequencies for a negative feedback amplifier designed for a closed-loop gain of 100 would occur when the open-loop gain falls to 100. It is seen that

## negative feedback increases amplifier bandwidth.

The upper cutoff frequency for an amplifier is usually greater than 20 kHz , and the lower cutoff frequency is around 100 Hz or lower. So $f_{2} \gg f_{1}$, and consequently,

$$
\mathrm{BW}=f_{2}-f_{1} \approx f_{2}
$$

This means that the amplifier bandwidth is essentially equal to the upper cutoff frequency.

Now refer to Fig.
once again. The amplifier gain multiplied by the upper cutoff frequency is a constant quantity. This is known as the gainbandwidth prodiuct. Therefore,

$$
\begin{align*}
& A_{\mathrm{CL}} \times f_{2(\mathrm{CL})}=A_{v} \times f_{2(\mathrm{OL})} \\
\text { or } & f_{2(\mathrm{CL})}=\frac{A_{v} f_{2(\mathrm{OL})}}{A_{\mathrm{CL}}}
\end{align*}
$$

Thus the closed-loop upper cutoff frequency for a negative feedback amplifier can be calculated from the open-loop upper cutoff frequency, the openloopgain, and the closed-loop gain.

## TYPES OF NEGATIVE FEEDBACK AMPLIFIER

4. Explain the various types of feedback amplifier (May 2017)
(OR)
With a neat block diagram, explain the operation of Current Shunt Feedback Amplifier.
(OR)
Determine $\mathbf{R i f}_{\mathrm{if}}, \mathbf{R}_{\mathbf{o f}}, \mathbf{A}_{\mathbf{v}}, \mathbf{A}_{\mathbf{v f}}$ for the following feedback amplifier
A. Voltage series feedback amplifier (Series-Shunt feedback amplifier) (Nov/Dec (May 2017)
B. Current Series Feedback Amplifier (Shunt-Series feedback amplifier)
C. Current Shunt Feedback Amplifier (Series-Series feedback amplifier) (May 2017)
D. Voltage Shunt Feedback Amplifier (Shunt-Shunt feedback amplifier)
(OR)
Discuss the effect of voltage series feedback and derive the expression for input resistance, output resistance and voltage gain.
(OR)
Discuss about the following feedback configurations of amplifiers and obtain the feedback factor and closed loop gain.
(April/May 2018-R13)
A. Shunt-Shunt Feed Back
B. Series-Series Feed Back
C. Shunt-Series Feed Back
D. Series-Shunt Feed Back

Feedback amplifier, the output signal sampled may be either voltage or current and sampled signal can be mixed either is series or in shunt with the input

The four types of amplifiers, they are
$>$ Voltage series feedback amplifier (Series-Shunt feedback amplifier)
(Nov/Dec 2016) (May 2017)
$>$ Current Series Feedback Amplifier (Shunt-Series feedback amplifier)
$>$ Current Shunt Feedback Amplifier (Series-Series feedback amplifier)
(May 2017)
$>$ Voltage Shunt Feedback Amplifier (Shunt-Shunt feedback amplifier)

## (A) VOLTAGE SERIES AMPLIFIER:

With proper mathematical derivation, proven that output resistance reduces in a negative feedback amplifier. Assume a series shunt feedback scheme. (April/May 2019)


- $\mathrm{R}_{\mathrm{i}}$ - input resistance
- $\mathrm{R}_{\mathrm{s}}$ - source resistance
- $\mathrm{R}_{\mathrm{L}}$ - load resistance
- $\mathrm{R}_{\mathrm{O}}$ - output resistance
- $A_{V}$ - voltage gain
- $R_{i} \gg R_{S}$ then $V_{i}=V_{s}$
- $R_{L} \gg R_{0}$ then $V_{o}=A_{V} V_{i}=A_{v} V_{s}$
- Amplifier provides a voltage output proportional to the voltage input
- The proportionality factor does not depend on magnitudes of the source an load resistance
- Hence it is called voltage amplifier


## Feedback Topology



## Input resistance

Step 1: equivalent circuit


## Step 2: obtain expression for $V_{s}$

Applying KVL to the input side we get,

$$
\begin{aligned}
& \mathrm{V}_{\mathrm{S}}-\mathrm{I}_{\mathrm{i}}-\mathrm{V}_{\mathrm{f}}=0 \quad \therefore \mathrm{~V}_{\mathrm{s}}=\mathrm{I}_{\mathrm{i}} \mathrm{R}_{\mathrm{i}}+\mathrm{V}_{\mathrm{f}}=\mathrm{I}_{\mathrm{i}} \mathrm{R}_{\mathrm{i}}+\beta \mathrm{V}_{\mathrm{o}} \\
& \therefore \mathrm{~V}_{\mathrm{f}}=\beta \mathrm{V}_{\mathrm{o}}
\end{aligned}
$$

## Step 3: obtain expression for $V_{o}$ in terms of $\mathbf{I}_{\mathbf{i}}$

The output voltage $\mathrm{V}_{\mathrm{o}}$ is given as

$$
\begin{aligned}
& V_{o}=\frac{A_{V} V_{i} R_{L}}{R_{O}+R_{\mathrm{L}}}=A_{V} V_{i} \text { where, } \quad A_{\nu}=\frac{A_{v} R_{L}}{R_{o}+R_{L}} \\
& \mathrm{~V}_{\mathrm{o}}=\mathrm{A}_{\mathrm{v}} \mathrm{I}_{\mathrm{i}} \mathrm{R}_{\mathrm{i}}
\end{aligned} \quad \therefore \mathrm{~V}_{\mathrm{i}}=\mathrm{I}_{\mathrm{i}} \mathrm{R}_{\mathrm{i}} .
$$

Step 4: obtain expression for $R_{\text {if }}$
Substituting value of $\mathrm{V}_{0}$ from above equation we get

$$
\begin{array}{ll}
V_{S}=I_{i} R_{i}+\beta A_{v} I_{i} R_{i} \\
R_{i f}=R_{i}\left(1+\beta A_{v}\right)
\end{array} \quad \therefore \mathrm{R}_{\mathrm{if}}=\mathrm{V}_{\mathrm{s}} / \mathrm{I}_{\mathrm{i}}=\mathrm{R}_{\mathrm{i}}+\beta \mathrm{A}_{\mathrm{v}} \mathrm{R}_{\mathrm{i}}
$$

## Output Resistance

## Step 1: Equivalent circuit



## Step 2: obtain expression for $I$ in terms of $V$

Applying KVL to the output side we get

$$
\mathrm{A}_{\mathrm{v}} \mathrm{~V}_{\mathrm{i}}+\mathrm{IR}_{0}-\mathrm{V}=0 \quad \therefore I=\frac{V-A_{V} V_{i}}{R_{0}}
$$

The input voltage is given as

$$
\mathrm{V}_{\mathrm{i}}=-\mathrm{V}_{\mathrm{f}}=-\beta \mathrm{V} \quad \therefore \mathrm{~V}_{\mathrm{s}}=0
$$

Substituting the $\mathrm{V}_{\mathrm{i}}$ from above equation we get

$$
I=\frac{V+A_{v} \beta V}{R_{0}}=\frac{V\left(1+\beta A_{V}\right)}{R_{0}}
$$

Step 3: obtain expression for $\mathbf{R}_{\text {of }}$

$$
R_{o f}=\frac{V}{I} \quad R_{o f}=\frac{R_{o}}{\left(1+\beta A_{v}\right)}
$$

Step 4: obtain expression for Rof

$$
\begin{aligned}
& \mathrm{R}_{\text {of }}^{\prime}= \mathrm{R}_{\mathrm{of}} \| \mathrm{R}_{\mathrm{L}}=\frac{R_{O f} \underline{X R_{L}}}{R O f}+\frac{\left(\frac{R_{O}}{\underline{O}}\right) \times R_{L}}{1+\beta A_{V}} \\
& \frac{R_{O}}{\left(1+\beta A_{V}\right)}+R_{L} \\
&=\frac{\mathrm{R}_{\underline{Q}} \underline{\mathrm{R}}_{\underline{\mathrm{L}}}}{\mathrm{R}_{\mathrm{O}}+\mathrm{R}_{\mathrm{L}}\left(1+\beta \mathrm{A}_{V}\right)}=\frac{\mathrm{R}_{\mathrm{O}} \underline{\mathrm{R}_{\mathrm{L}}}}{\mathrm{R}_{\mathrm{O}}+\mathrm{R}_{\mathrm{L}}+\beta \mathrm{A}_{V} \mathrm{R}_{\mathrm{L}}}
\end{aligned}
$$

Dividing numerator and denominator by $\left(\mathrm{R}_{\mathrm{o}}+\mathrm{R}_{\mathrm{L}}\right)$

$$
\begin{aligned}
& R^{\prime}=\frac{\frac{R_{o} R_{L}}{R_{o}+R_{L}}}{1+\frac{\beta A_{v} R_{L}}{R_{o}+R_{\mathrm{L}}}} \\
& \text { of } \\
& R_{o f}^{\prime}= \frac{R_{o}^{\prime}}{1+\beta A_{v}}
\end{aligned}
$$

## (B)CURRENT SERIES AMPLIFIER:



Norton's equivalent circuits of a current amplifier

- $\mathrm{R}_{\mathrm{i}}$ - input resistance
- $\mathrm{R}_{\mathrm{s}}$ - source resistance
- $\mathrm{R}_{\mathrm{L}}$ - load resistance
- $\mathrm{R}_{\mathrm{O}}$ - output resistance
- $\mathrm{A}_{\mathrm{I}}$ - current gain
- $\mathrm{R}_{\mathrm{s}} \gg \mathrm{R}_{\mathrm{i}}$ and $\mathrm{I}_{\mathrm{i}}=\mathrm{I}_{\mathrm{s}}$
- $\mathrm{R}_{0} \gg \mathrm{R}_{\mathrm{L}} \quad \mathrm{I}_{\mathrm{L}}=\mathrm{A}_{\mathrm{I}} \mathrm{I}_{\mathrm{i}}$
- Amplifier provides a current output proportional to the current input
- The proportionality factor does not independent on source and load resistance
- Hence it is called current amplifier


## Feedback Topology



## Input Resistance

## Step 1: equivalent circuit



Step 2: obtain expression for $\mathbf{V s}$
Applying KVL to the input side we get,

$$
\begin{aligned}
& \mathrm{V}_{\mathrm{S}}-\mathrm{I}_{\mathrm{i}} \mathrm{R}_{\mathrm{i}}-\mathrm{V}_{\mathrm{f}}=0 \quad \therefore \mathrm{~V}_{\mathrm{s}}=\mathrm{I}_{\mathrm{i}} \mathrm{R}_{\mathrm{i}}+\mathrm{V}_{\mathrm{f}}=\mathrm{I}_{\mathrm{i}} \mathrm{R}_{\mathrm{i}}+\beta \mathrm{I}_{\mathrm{o}} \\
& \therefore \mathrm{~V}_{\mathrm{f}}=\beta \mathrm{I}_{\mathrm{o}}
\end{aligned}
$$

Step 3: obtain expression for $\mathbf{I}_{\mathbf{o}}$ in terms of $\mathbf{V}_{\mathbf{i}}$
The output current $I_{0}$ is given by

$$
I_{o}=\frac{G_{m} V_{i} R_{o}}{R_{o}+R_{L}}=G_{M} V_{i} \text { where } G_{M}=\frac{G_{m} \underline{R_{o}}}{R_{o}+R_{L}}
$$

## Step 4: obtain expression for $\mathbf{R}_{\text {if }}$

Substituting value of $\mathrm{I}_{0}$ from above equation

$$
\begin{gathered}
V_{S}=I_{i} R_{i}+\beta G_{M} V_{i}=I_{i} R_{i}+\beta G_{M} I_{i} R_{i} \quad\left\{\text { Since, } V_{i}=I_{i} R_{i}\right\} \\
R_{i f}=V_{s} / I_{i}=R_{i}\left(1+\beta G_{M}\right)
\end{gathered}
$$

## Output Resistance

## Step 1: equivalent circuit



Step 2: obtain expression for $I$ in terms of $V$
Applying KVL to the output node we get

$$
I=\frac{V}{R_{o}}-G_{m} V_{i}
$$

The input voltage is given as $\mathrm{V}_{\mathrm{i}}=-\mathrm{V}_{\mathrm{f}}=-\beta \mathrm{I}_{\mathrm{o}}=\beta \mathrm{I}$
$\therefore \mathrm{I}_{\mathrm{o}}=-\mathrm{I}$
Substituting value of $\mathrm{V}_{\mathrm{i}}$ from above equation we get

$$
I=\frac{V}{R_{o}}-G_{m} \beta \mathrm{I} \quad \frac{V}{R_{o}}=I+G_{m} \beta \mathrm{I}=\mathrm{I}\left(1+G_{m} \beta\right)
$$

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Step 3: obtain expression for $R_{\text {of }}$

$$
\begin{gathered}
R_{o f}=\frac{V}{I}=R_{o}\left(1+G_{m} \beta\right) \\
R_{o f}^{\prime}=R_{o f} \| R_{L}=\frac{R_{o f} X R_{L}}{R_{o f}+R_{L}} \\
\left.=\frac{R_{o}\left(1+\beta G_{m}\right) R_{L}}{R_{o}(1+}\right)=\frac{R_{o} R_{L}\left(1+\beta G_{m}\right)}{R_{o}+R+\beta G_{m} R_{o}}
\end{gathered}
$$

Dividing numerator and denominator by $R_{o}+R_{L}$ we get

$$
\begin{gathered}
R_{f o}=\frac{\underline{R}_{L} \underline{R}_{o}\left(1+\beta G_{m}\right)}{R_{o}+R_{L} \underline{2}} \\
1+\frac{\beta G_{m} R_{o}}{R_{o}+R_{L}} \\
R_{o f}^{\prime}=\frac{R_{b}^{\prime}\left(1+\beta G_{m}\right)}{1+} \quad \therefore R_{o}^{\prime}=\frac{R_{o} R_{L}}{R_{o}+R} \text { and } G_{M}=\frac{G_{m} R}{R_{o}+R_{L}}
\end{gathered}
$$

## (C) VOLTAGE SHUNT AMPLIFIER



- $\mathrm{R}_{\mathrm{i}} \ll \mathrm{R}_{\mathrm{s}}$ and $\mathrm{R}_{\mathrm{o}} \ll \mathrm{R}_{\mathrm{s}}$
- Since $\mathrm{R}_{\mathrm{i}} \ll \mathrm{R}_{\mathrm{s}}$.
- $\mathrm{I}_{\mathrm{i}}=\mathrm{I}_{\mathrm{S}}$ and $\mathrm{R}_{\mathrm{o}} \ll \mathrm{R}_{\mathrm{L}}$, $\mathrm{V}_{\mathrm{o}}=\mathrm{R}_{\mathrm{m}} \mathrm{I}_{\mathrm{s}}$
- Where $R_{m}=V_{o} / I_{s}$ is the transfer or mutual resistance


## Feedback Topology



## Input Resistance

## Step 1: Equivalent Circuit



Step 2: obtain expression for $I_{s}$
Applying KCL at input node we get

$$
\mathrm{I}_{\mathrm{s}}=\mathrm{I}_{\mathrm{i}}+\mathrm{I}_{\mathrm{f}}=\mathrm{I}_{\mathrm{i}}+\beta \mathrm{V}_{\mathrm{o}} \quad \therefore \mathrm{I}_{\mathrm{f}}=\beta \mathrm{V}_{\mathrm{o}}
$$

## Step 3: obtain expression for $\mathbf{R}_{\text {if }}$

The output voltage $\mathrm{V}_{\mathrm{o}}$ is given by

$$
V=\frac{R_{m} I_{i} R_{o}}{R_{o}+R_{L}}=R_{M} I_{i} \quad \text { where } R_{M}=\frac{R_{m} \underline{R_{o}}}{R_{o}+R_{L}}
$$

Step 4: obtain expression for $\mathbf{R}_{\text {if }}$
Substituting value of $\mathrm{V}_{\mathrm{o}}$ from above equation we get

$$
I_{s}=I_{i}+\beta R_{M} I_{i}=I_{i}\left(1+\beta R_{M}\right)
$$

The input resistance with feedback $\mathrm{R}_{\mathrm{if}}$ is given by

$$
\begin{gathered}
R_{i f}=\frac{V_{i}}{I_{s}}=\frac{V_{i}}{I_{i}\left(1+\beta R_{M}\right)} \quad \therefore R_{i}=\frac{V_{i}}{I_{i}} \\
\therefore R_{f}=\frac{R_{i}}{\left(1+\beta R_{M}\right)}
\end{gathered}
$$

## Output Resistance

## Step 1: Equivalent Circuit



Step 2: obtain expression for $I$ in terms of $V$
Applying KVL to the output side we get

$$
\mathrm{R}_{\mathrm{m}} \mathrm{I}_{\mathrm{i}}+\mathrm{I} \mathrm{R}_{\mathrm{o}}-\mathrm{V}=0 \quad \therefore I=\frac{V-R_{m} I_{i}}{R_{o}}
$$

The input current is given as

$$
\mathrm{I}_{\mathrm{i}}=-\mathrm{I}_{\mathrm{f}}=-\beta \mathrm{V}
$$

Substituting $I_{i}$ in above equation we get

$$
I=\frac{V+R_{m} \beta V}{R_{o}}=\frac{V\left(1+R_{m} \beta\right)}{R_{o}}
$$

Step 4: obtain expression for $\boldsymbol{R}_{o f}^{\prime}$

$$
R_{o f}^{\prime}=R_{o f} \| R_{L}=\frac{R_{o f} X R_{L}}{R_{o f}+R_{L}}=\frac{\frac{R_{o} X R_{L}}{1+R_{m} \beta}}{\frac{R_{o}}{1+R_{m} \beta}+R_{L}}=\frac{R_{o} R_{L}}{R_{o}+R_{L}\left(1+R_{m} \beta\right)}
$$

Dividing numerator and denominator by $\left(\mathrm{R}_{\mathrm{o}}+\mathrm{R}_{\mathrm{L}}\right)$ we get

$$
\begin{gathered}
R_{f o}^{\prime}=\frac{\frac{R_{o} R_{L}}{R_{o}+R_{L}}}{1+\frac{\beta R_{m} R_{L}}{R_{o}+R_{L}}} \\
R_{f o}^{\prime}=\frac{R_{o}^{F}}{1+\beta R_{M}} \quad \text { where } R_{o}^{\prime}={ }_{R_{L} X R_{o f}}^{R_{L}+R_{o f}}
\end{gathered} \begin{gathered}
\text { and } R_{M}=\frac{R_{m} R_{L}}{\left(R_{o}+R_{L}\right)}
\end{gathered}
$$



- $\mathrm{R}_{\mathrm{i}} \ll \mathrm{R}_{\mathrm{s}}$ and $\mathrm{R}_{\mathrm{o}} \ll$ $\mathrm{R}_{\mathrm{s}}{ }^{\prime}$
- Since $R_{i} \ll R_{s}^{\prime}$
- $\mathrm{I}_{\mathrm{i}}=\mathrm{I}_{\mathrm{s}}$ and $\mathrm{R}_{\mathrm{o}} \ll$ $\mathrm{R}_{\mathrm{L}}, \mathrm{V}_{\mathrm{o}}=\mathrm{R}_{\mathrm{m}} \mathrm{I}_{\mathrm{s}}$

Feedback Topology



## Input Resistance <br> Step 1: Equivalent Circuit



## Step 2: obtain expression for $I_{\text {s }}$

Applying KCL to the input node we get

$$
\mathrm{I}_{\mathrm{s}}=\mathrm{I}_{\mathrm{i}}+\mathrm{I}_{\mathrm{f}}=\mathrm{I}_{\mathrm{i}}+\beta \mathrm{I}_{\mathrm{o}} \quad \therefore \mathrm{I}_{\mathrm{f}}=\beta \mathrm{I}_{\mathrm{o}}
$$

Step 3: obtain expression for $\mathbf{I}_{\mathbf{0}}$ in terms of $\mathbf{I}_{\mathbf{i}}$

$$
b=\frac{A_{i} I_{i} \underline{R_{o}}}{R_{o}+R_{L}}=A_{I} I_{i} \quad \text { where } A_{I}=\frac{A_{i} \underline{R_{o}}}{R_{o}+R_{L}}
$$

## Step 4: obtain expression for $\mathbf{R}_{\text {if }}$

Substituting value of $\mathrm{I}_{0}$ in above equation we get

$$
\mathrm{I}_{\mathrm{s}}=\mathrm{I}_{\mathrm{i}}+\beta \mathrm{A}_{\mathrm{I}} \mathrm{I}_{\mathrm{i}}=\mathrm{I}_{\mathrm{i}}\left(1+\beta \mathrm{A}_{\mathrm{I}}\right)
$$

The input resistance with feedback is given as

$$
\begin{gathered}
\stackrel{\text { EngqTATree. }_{i}}{\stackrel{\operatorname{com}_{i}}{=}} \overline{I_{s}}=\frac{R_{i}}{I_{i}\left(1+\beta A_{\mathrm{I}}\right)} \\
R_{i f}=\frac{R_{i}}{\left(1+\beta A_{I}\right)}
\end{gathered}
$$

## Output Resistance

Step 1: Equivalent Circuit


## Step 2: obtain expression for I in terms of $\mathbf{V}$

Applying KCL to the output node we get

$$
I=\frac{V}{R_{o}}-A_{i} I_{i}
$$

The input current is given as

$$
\begin{array}{ll}
\mathrm{I}_{\mathrm{i}}=-\mathrm{I}_{\mathrm{f}}=-\beta \mathrm{I}_{\mathrm{o}} & \therefore \mathrm{I}_{\mathrm{s}}=0 \\
\mathrm{I}_{\mathrm{i}}=\beta \mathrm{I} & \therefore \mathrm{I}=-\mathrm{I}_{\mathrm{o}}
\end{array}
$$

Substituting value of $\mathrm{I}_{\mathrm{i}}$ in above equation we get
$I=\frac{V}{R_{o}}-A_{i} \beta \mathrm{I} \quad \therefore \frac{V}{R_{o}}=I+A{ }_{i}^{\beta}=\mathrm{I}(1+\beta A)$
Step 3: obtain expression for $\mathbf{R}_{\text {of }}$

$$
\begin{gathered}
R_{o f}^{\prime}=R_{o f} \| R_{L}=\frac{R_{o f} X R_{L}}{R_{o f}+R_{L}} \\
=\frac{R_{o}\left(1+\beta A_{i}\right) R_{L}}{R_{o}\left(1+\beta A_{i}\right)+R_{L}} \quad \therefore=\frac{R_{o} R_{L}\left(1+\beta A_{i}\right)}{R_{o}+R_{L}+\beta A_{i} R_{o}}
\end{gathered}
$$

Dividing numerator and denominator by $\left(\mathrm{R}_{\mathrm{o}}+\mathrm{R}_{\mathrm{L}}\right)$ we get

$$
\begin{array}{r}
\text { EnggTree.com } \\
R_{o f}^{\prime}=\frac{\frac{R_{o} R_{L}\left(1+\beta A_{i}\right)}{R_{o}+R_{L}}}{1+\frac{\beta A_{i} R_{o}}{R_{o}+R_{L}}} \\
R_{o f}^{\prime}=\frac{R_{o}^{\prime}\left(1+\beta A_{i}\right)}{\left(1+\beta A_{I}\right)} \\
R_{o}^{\prime}=\frac{R_{o} \underline{R_{L}}}{R_{o}+R_{L}} \text { and } A_{I}=\frac{A_{\underline{i}} \underline{R}_{\underline{o}}}{R_{o}+R_{L}}
\end{array}
$$

## OSCILLATORS:

5. Explain the construction and working of the following oscillators and derive the expression for frequency of oscillation. Also, write about advantages and disadvantages.
A. Phase-Shift Oscillator (RC type Oscillator)
B. Wein Bridge Oscillator (RC type Oscillator)
C. Hartley Oscillator (LC type Oscillator)
D. Colpitts Oscillator (LC type Oscillator)
E. Crystal Oscillator

## (A) RC Phase Shift Oscillator:

Explain the construction and working of RC Phase-Shift oscillator and derive the expression for frequency of oscillation.

- It consists of an amplifier and feedback network consisting of resistors and capacitors.
- An amplifier can be BJT, FET or operational amplifier.


## Analysis of RC circuit:

- In this circuit output is taken across resistor R.

- The capacitive reactance $\mathrm{X}_{\mathrm{C}}$ is given by $X_{C}=\frac{1}{2 \pi f C} \Omega$ where f is frequency of the input.
- The total impedance of the circuit is,

$$
Z=R-j X_{C}=R-j\left(\frac{1}{2 \pi f C}\right) \Omega
$$

- The current ' $I$ ' flowing in the circuit is,

$$
I=\frac{V_{i}<0^{0}}{Z}=\frac{V_{i}<0^{0}}{|Z|<-\Phi^{0}}=\left|\frac{V_{i}}{Z}\right|<+\Phi^{0} \quad A
$$

$$
|Z|=\sqrt{R^{2}+X_{C}^{2}} \text { and } \Phi=\tan ^{-1} \frac{X_{C}}{R}
$$

- In this equation the current ' $I$ ' leads input voltage by angle $\Phi$
- The output voltage is drop across R hence $\mathrm{V}_{\mathrm{O}}=\mathrm{V}_{\mathrm{R}}=\mathrm{IR}$
- The output voltage is in phase with current hence it leads input voltage by angle $\Phi$
- Thus, RC circuit introduces a phase shift $\Phi$ between input and output which depends on $\mathrm{R}, \mathrm{C}$ and frequency f .


## RC Feedback Network for phase shift oscillator:

- In RC phase shift oscillator, amplifier introduces a phase shift of $180^{\circ}$
- Thus, the feedback network must introduce a phase shift of $180^{\circ}$ to satisfy Barkhausen condition.
- The RC feedback network consists of three RC sections, with each RC section contributing $60^{\circ}$ phase-shift.
- Hence in RC phase shift oscillator, the feedback network consists of three RC sections are shown in fig.
- In all the three sections, resistance values and capacitance values are same so that at a particular frequency, each section produces precisely $60^{\circ}$ phase-shift. This is the operating frequency of oscillator.



## Transistorized RC phase shift oscillator:

- The RC phase shift oscillator uses BJT amplifier stage which is single stage amplifier in common emitter configuration.
- A phase shift network has three RC sections
- The output of CE amplifier is connected as input to the RC phase shifting network
- The output of RC phase shifting network is connected as input to the amplifier
- Due to common emitter amplifier it introduces a phase shift of $180^{\circ}$ between its input and output
- The RC phase shift network contributes further $180^{\circ}$ phase shift so that phase shift around a loop is $360^{\circ}$

- From the fig. neglecting R1 and R2 we can write $\mathrm{h}_{\mathrm{ie}}=$ input impedance of amplifier stage
- Thus, to have all three resistance values in three RC section equal, resistance in the last section is selected as $R_{3}$ so that $R_{3}+h_{i e}=R$

$$
\mathrm{R}_{3}+\mathrm{h}_{\mathrm{ie}}=\mathrm{R} \text { i.e } \quad \mathrm{R}_{3}=\mathrm{R}-\mathrm{h}_{\mathrm{ie}}
$$

eq. 1

- If R1 and R2 are not neglected then, $\square$ $\mathrm{R} 3=\mathrm{R}-\left[\mathrm{R}_{1}\left\|\mathrm{R}_{2}\right\| \mathrm{h}_{\mathrm{ie}}\right]$ ----- eq. 2
- When gain $A$ of the amplifier stage and feedback factor $\beta$ are adjusted to give $|\mathrm{A} \beta|=1$, then the circuit works as an oscillator, satisfying both Barkhausen condition.


## Derivation for frequency of oscillation:

- Replacing the transistor by its approximate h-parameter model, the equivalent circuit of RC phase shift oscillator is shown in fig.

- It is known that $\mathrm{R}=\mathrm{h}_{\mathrm{ie}}+\mathrm{R}_{3}$ and replace current source by equivalent voltage source.
- The ratio of resistance $\mathrm{R}_{\mathrm{C}}$ to R is K . $\frac{R_{C}}{R}=K$
- The modified equivalent circuit is shown below


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- Applying KVL to the three loops

$$
I_{1} R_{C}-\frac{1}{j \omega C} I_{1}-R\left(I_{1}-I_{2}\right)-h_{f e} I_{b} R_{c}=0 \quad \text { and use } R_{C}=k R
$$

$\therefore I_{1}\left[k R+R+\frac{1}{j \omega C}\right]+I_{2} R=h_{\text {e }} I_{b} k R-\cdots--\cdots$ eq. 3

$$
\begin{aligned}
& -\frac{1}{j \omega C} I_{2}-R\left(I_{2}-I_{1}\right)-R\left(I_{2}-I_{3}\right)=0 \text { i.e } I_{1} R-I_{2}\left(2 R+\frac{1}{j \omega C}\right)+I_{3} R=0---- \text { eq. } 4 \\
& -\frac{1}{j \omega C} I_{3}-I_{3} R-R\left(I_{3}-I_{2}\right)=0 \quad \text { i.e } I_{2} R-I_{3}\left(2 R+\frac{1}{j \omega C}\right)=0--- \text { eq. } 5
\end{aligned}
$$

- Using $\mathrm{j} \omega=\mathrm{s}$ and Cramers's rule
- Solving the determinant we get,

$$
\begin{equation*}
D=-\left\{\frac{s^{3} C^{3} R^{3}(3 k+1)+s^{2} C^{2} R^{2}(4 k+6)+s R C(5+k)+1}{s^{3} C^{3}}\right\} \tag{eq. 6}
\end{equation*}
$$

- To find $\mathrm{I}_{3}$, find $\mathrm{D}_{3}$ as,

$$
\begin{align*}
& -(k+1) R-\frac{1}{s C} \quad R \quad h_{k} I_{b} k R \\
& D_{3}=\left\lvert\, \begin{array}{cccc}
R & -2 R-\frac{1}{s C} & 0 & \mid=k R^{3} h_{f e} I_{b}--------------\quad \text { eq. } 7 \\
0 & R & 0
\end{array}\right. \\
& I_{3}=\frac{\underline{D}_{3}}{D}=\frac{-k R^{3} h_{f e} I_{b} s^{3} C^{3}}{s^{3} C^{3} R^{3}(3 k+1)+s^{2} C^{2} R^{2}(4 k+6)+s R C(5+k)+1--}  \tag{eq. 8}\\
& \mathrm{I}_{3}=\text { Output current of the feedback circuit } \\
& \mathrm{I}_{\mathrm{b}}=\text { Input current of the amplifier } \\
& \mathrm{I}_{\mathrm{C}}=\mathrm{h}_{\mathrm{fe}} \mathrm{I}_{\mathrm{b}}=\text { input current of the feedback circuit }
\end{align*}
$$

$$
\begin{gathered}
\begin{array}{c}
\begin{array}{c}
\text { EnggTree.com } \\
\text { Output of the feedback circuit }
\end{array} \\
\text { Input to feedback circuit }
\end{array} \frac{\mathrm{I}_{3}}{\mathrm{I}_{\mathrm{C}}}=\frac{\mathrm{I}_{3}}{\mathrm{~h}_{\mathrm{fe}} \mathrm{I}_{\mathrm{b}}} \\
\mathrm{~A}=\frac{\text { Output of the amplifier }}{\text { Input to the amplifier }}=\frac{\mathrm{I}_{3}}{\mathrm{I}_{\mathrm{b}}}=\mathrm{h}_{\mathrm{fe}} \\
A \beta=h_{f e} X \frac{I_{3}}{h_{f e} I_{b}}=\frac{I_{3}}{I_{b}} \quad---- \text { eq. } 9
\end{gathered}
$$

From equation 8 and 9 ,

$$
A \beta=\frac{-k R^{3} h_{f e^{3}} C^{3}}{s^{3} C^{3} R^{3}(3 k+1)+S^{2} C^{2} R^{2}(4 k+6)+s R C(5+k)+1}----- \text { eq. } 10
$$

Using $\mathrm{s}=\mathrm{j} \omega \quad \mathrm{s}^{2}=\mathrm{j}^{2} \omega^{2}=-\omega^{2}, \quad \mathrm{~s}^{3}=\mathrm{j}^{3} \omega^{3}=-\mathrm{j} \omega^{3}$ and separating the real and imaginary part we get,

$$
A \beta=\frac{+j \omega^{3} k R^{3} C^{3} h_{f e}}{\left[1-4 k \omega^{2} C^{2} R^{2}-6 \omega^{2} C^{2} R^{2}\right]-j \omega\left[3 k \omega^{2} R^{3} C^{3}+\omega^{2} R^{3} C^{3}-5 R C-k R C\right.}
$$

Dividing numerator and denominator by $\mathrm{j} \omega^{3} \mathrm{R}^{3} \mathrm{C}^{3}$ and replacing $-1 / \mathrm{j}=+\mathrm{j}$

$$
A \beta=\frac{1}{-j\left\{\frac{1}{\omega^{3} R^{3} C^{3}}-\frac{4 k}{\omega R C}-\frac{6 h_{f e}}{\omega R C}\right\}-\left\{3 k+1-\frac{5}{\omega R^{2} C^{2}}-\frac{k}{\left.\omega^{2} R^{2} C^{2}\right\}}\right.}
$$

Replacing $1 / \omega$ RC by $\alpha$ for simplicity

$$
\begin{equation*}
A \beta=\frac{k h_{f e}}{\left[-3 k-1+5 \alpha^{2}+k \alpha^{2}\right]-j\left[\alpha^{3}-4 k \alpha-6 \alpha\right]} \tag{eq. 11}
\end{equation*}
$$

To satisfy Barkhausen criterion, $<\mathrm{A} \beta=0^{0}$ hence imaginary part of the denominator term must be 0

$$
\therefore \alpha^{3}-4 \mathrm{k} \alpha-6 \alpha=0 \text { i.e. } \alpha\left(\alpha^{2}-4 \mathrm{k}-6\right)=0
$$

$\therefore \alpha 2=4 \mathrm{k}+6(\alpha \neq 0)$ i.e. $\alpha=\sqrt{4 k+6} \quad----$ eq. 12
$\therefore \quad 1 / \omega \mathrm{RC}=\sqrt{4 k+6}$ i.e. $\omega=\frac{1}{R C \sqrt{4 k+6}}$ i.e. $f=\frac{1}{2 \pi \sqrt{4 k+6}}$
This is the required frequency of oscillations.
Substituting $\alpha=\sqrt{4 k+6}$ in equation 11 we get,

$$
A \beta=\frac{k h_{f e}}{-3 k-1+(4 k+6)(5+k)}=\frac{k h_{f e}}{4 k^{2}+23 k+29}
$$

But $|A \beta|=1 \quad$ i.e $\quad\left|\frac{k h_{f e} \text { EnggTree.com }}{4 k^{2}+23 k+29}\right|=1$

$$
\therefore h_{f e}=4 k+23 k+\frac{29}{k}
$$

This is the required $\mathrm{h}_{\mathrm{fe}}$ for the oscillations.

## Minimum value of $h_{f e}$ :

- For satisfying $\mathrm{A} \beta=1$, the expression for the value of $\mathrm{h}_{\mathrm{fe}}$ of the transistor used in RC phase shift oscillator is given by,

$$
\mathrm{h}_{\mathrm{fe}} \geq 4 \mathrm{k}+23+\frac{29}{k} \text { where } \mathrm{k}=\frac{R C}{R}
$$

- For minimum $\mathrm{h}_{\mathrm{fe}}$, find k for minimum $\mathrm{h}_{\mathrm{fe}}$ from the expression $\frac{d h f e}{d k}=0$

$$
\begin{array}{r}
\therefore \frac{d}{d k}\left[4 k+23+\frac{29}{k}\right]=0 \text { i.e. } 4-\frac{29}{k^{2}}=0 \quad \text { i.e. } k^{2}=\frac{29}{4} \\
\mathrm{k}=2.6925 \text { for minimum } \mathrm{h} \mathrm{fe}
\end{array}
$$

using in the expression of $\mathrm{h}_{\mathrm{f}}$,

$$
\mathrm{h}_{\mathrm{fe}}(\mathrm{~min})=4 \times 2.6925+23+\frac{29}{2.6925}=\mathbf{4 4 . 5 4}
$$

Thus for the circuit to oscillate, the transistor must be selected with $\mathrm{h}_{\mathrm{fe}}$ greater than 44.54

## Advantages:

- The circuit is simple to design
- Can produce output over audio frequency range
- Produces sinusoidal output waveform
- It is fixed frequency oscillator


## Disadvantages:

- To vary the frequency, values of R and C of all three sections are to be varied simultaneously which is practically difficult. Hence frequency cannot be varied
- Frequency stability is poor due to changes in the values of various components due to effect temperature, aging etc.

Explain the working of Wien Bridge Oscillator. Derive the expression for frequency of oscillation and condition for maintenance of oscillation.
(OR)
Design an oscillator to operate at a frequency of 10 KHz which gives an extremely pure sine wave output, good frequency stability and highly stabilized amplitude. Discuss the operation of this oscillator as an audio signal generator.

## Construction and operation - (Wien Bridge Oscillator Circuit)

$\checkmark$ Two stage amplifiers (non-inverting) and feedback network are used in Wien Bridge Oscillator.
$\checkmark$ Both amplifier and feedback network does not introduce any phase shift i.e. $0^{\circ}$ phase-shift around the loop in Wien Bridge Oscillator.
$\checkmark R_{1} \& C_{1}$ in series and $R_{2} \& C_{2}$ in parallel are frequency sensitive arms.
$\checkmark$ The output of Amplifier is applied as input to Feedback Network $\left(\mathrm{V}_{\text {in }}\right.$ between 1 and 3.
$\checkmark$ The output of Feedback Network $\left(\mathrm{V}_{\mathrm{f}}\right)$ taken between 2 and 4 is given as input to amplifier.
$\checkmark$ This Feedback Network is also known as Lead-Lag Network.


Basic circuit of Wien bridge oscillator


Feedback network of Wien bridge oscillator


Transistorised Wien bridge oscillator

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## Derive the expression for frequency of oscillation:

Analysis for frequency of oscillation:
$Z_{1}=R_{1}+\frac{1}{j \omega C_{1}} \Rightarrow Z_{1}=\frac{1+j \omega R_{1} C_{1}}{j \omega C_{1}}$
$Z_{2}=R_{2} \quad \frac{1}{j \omega C_{2}} \Rightarrow Z_{2}=\frac{R_{2} \times \frac{1}{j \omega C_{2}}}{R_{2}+\frac{1}{j \omega C_{2}}} \Rightarrow Z_{2}=\frac{R_{2}}{1+j \omega R_{2} C_{2}}$
$\beta=\frac{V_{f}}{V_{\text {in }}}$

$$
\begin{align*}
& I=\frac{V_{i n}}{Z_{1}+Z_{2}}  \tag{3}\\
& V_{f}=I Z_{2}  \tag{5}\\
& \operatorname{Sub}(4) \text { in (5) } \Rightarrow V_{f}=\frac{-Z_{2}}{Z_{1}+Z_{2}} V_{i n}
\end{align*}
$$

Sub (6) in (3)
$\Rightarrow \beta=\frac{Z_{2}}{Z_{1}+Z_{2}}$

Substitute (1) \& (2) in (7)
$\beta=\frac{\frac{R_{2}}{1+j \omega R_{2} C_{2}}}{\frac{1+j \omega R_{1} C_{1}}{j \omega C_{1}}+\frac{R_{2}}{1+j \omega R_{2} C_{2}}}$
Simplify the equation (8),
$\beta=\frac{j \omega R_{2} C_{1}}{\left(1-\omega^{2} R_{1} R_{2} C_{1} C_{2}\right)+j \omega\left(R_{1} C_{1}+R_{2} C_{2}+R_{2} C_{1}\right)}$
Rationalizing and Simplifying the equation (9),
$\beta=\frac{\omega^{2} R_{2} C_{1}\left(R_{1} C_{1}+R_{2} C_{2}+R_{2} C_{1}\right)+j \omega C_{1} R_{2}\left(1-\omega^{2} R_{1} R_{2} C_{1} C_{2}\right)}{\left(1-\omega^{2} R_{1} R_{2} C_{1} C_{2}\right)^{2}+\omega^{2}\left(R_{1} C_{1}+R_{2} C_{2}+R_{2} C_{1}\right)^{2}}$
To have zero phase shift, imaginary part of above equation must be zero.
$\left(1-\omega^{2} R_{1} R_{2} C_{1} C_{2}\right)=0$
$\omega\left(\omega^{2} R_{1} R_{2} C_{1} C_{2}\right)=0$ but $\omega$ can not be zero. So,
$\omega^{2} R_{1} R_{2} C_{1} C_{2}=0 \Rightarrow \omega^{2}=\frac{1}{R_{1} R_{2} C_{1} C_{2}}$

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$\Rightarrow \omega=\frac{1}{\sqrt{R_{1} R_{2} C_{1} C_{2}}}$
Frequency of Wien Bridge Oscillator, $f=\frac{1}{2 \pi \sqrt{R_{1} R_{2} C_{1} C_{2}}} \mathbf{H z}$
In pratice, $R_{1}=R_{2}=R$ and $C_{1}=C_{2}=C$ hence,
Frequency of Wien Bridge Oscillator, $\quad \boldsymbol{f}=\frac{\mathbf{1}}{2 \boldsymbol{\pi} \boldsymbol{R C}} \mathbf{H z}$

## Derive the condition for maintenance of oscillation:

Case (1): If $R_{1}=R_{2}=R$ and $C_{1}=C_{2}=C$ then use $\omega=\frac{1}{R C} H z$ in (10),
we get the magnitude of the feedback network as,
$\mathrm{Q}=\frac{3}{0+\frac{1}{R^{2} C^{2}}(3 R C)^{2}}=\frac{3}{9}=\frac{\mathbf{1}}{\mathbf{3}} \quad \Rightarrow \quad \mathrm{Q}=\frac{\mathbf{1}}{\mathbf{3}}$
As $|A \beta| \geq 1$ hence $|A| \geq 3$ for Wien Bridge Oscillator.
Thus, the gain of amplifier stage must be at least 3 to ensure sustained oscillations in Wien Bridge Oscillator.

Case (2): If $R_{1} \neq R_{2}$ and $C_{1} \neq C_{2}$ then use $\omega=\frac{1}{\sqrt{R_{1} R_{2} C_{1} C_{2}}}$ in (10) then
$\mathrm{Q}=\frac{R_{2} C_{1}}{R_{1} C_{1}+R_{2} C_{2}+R_{2} C_{1}} \quad \Rightarrow \therefore A \geq \frac{R_{1} C_{1}+R_{2} C_{2}+R_{2} C_{12}}{R_{2} C_{1}} \quad\{\because|A \beta| \geq 1\}$

## LC OSCILLATORS:

Outline the LC tuned Oscillator and deduce expression for amplifier Gain, feedback Gain and necessary condition for LC Oscillator in general.

(a) Basic circuit

(b) Equivalent circuit

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| Analysis of Amplifier stage |  |  |
| :--- | :--- | :---: |

## Analvsis of feedback stage



$$
\begin{aligned}
& \text { By voltage division in parallel circuit, } \\
& V_{f}=\frac{V_{o} Z_{1}}{Z_{1}+Z_{3}} \\
& \text { i.e. } \beta=\frac{V_{f}}{V_{o}}=\frac{Z_{1}}{Z_{1}+Z_{3}}
\end{aligned}
$$

But as feedback network introduces $180^{\circ}$ phase-shift, use negative sign

$$
Q=-\frac{Z_{1}}{Z_{1}+Z_{3}}
$$

Expression of the loop gain :

- According to Barkhausen condition loop gain $-A \beta$ is,

$$
-A \beta=-\frac{A_{\mathrm{v}} Z_{L} Z_{1}}{\left(R_{o}+Z_{L}\right)\left(Z_{1}+Z_{3}\right)}
$$

and $Z_{L}=\frac{\left(Z_{1}+Z_{3}\right) Z_{2}}{Z_{1}+Z_{2}+Z_{3}}$
$\therefore-A \beta=-\frac{A_{v} Z_{1} Z_{2}}{R_{o}\left(Z_{1}+Z_{2}+Z_{3}\right)+Z_{2}\left(Z_{1}+Z_{3}\right)}$
The impedances $Z_{1}, Z_{2}, Z_{3}$ are pure reactive elements either $L$ or $C$.
$\therefore \quad Z_{1}=j X_{1}, Z_{2}=j X_{2}, Z_{3}=j X_{3}$
Thus the loop gain becomes,

$$
\begin{aligned}
-A \beta & =-\frac{A_{v}\left(j X_{1}\right)\left(j X_{2}\right)}{R_{o} j\left(X_{1}+X_{2}+X_{3}\right)+j X_{2}\left(j X_{1}+j X_{3}\right)} \\
& =\frac{A_{v} X_{1} X_{2}}{-X_{2}\left(X_{1}+X_{3}\right)+j R_{0}\left(X_{1}+X_{2}+X_{3}\right)}
\end{aligned}
$$

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- To have $0^{\circ}$ phase shift for the loop gain, the imaginary part must be zero.

$$
\begin{array}{lr}
\therefore & \left(X_{1}+X_{2}+X_{3}\right)=0 \\
\therefore & -A \beta=\frac{-A_{v} X_{1} X_{2}}{X_{2}\left(X_{1}+X_{3}\right)} \text { but } X_{1}+X_{3}=-X_{2} \\
\therefore & -A \beta=A_{v}\left(\frac{X_{1}}{X_{2}}\right)
\end{array}
$$

- According to Barkhausen condition $-\mathrm{A} \beta$ must be positive and greater than equal to 1 . As $A_{v}$ is positive, $-A \beta$ will be positive only when $X_{1}$ and $X_{2}$ have same sign.
- Thus $X_{1}$ and $X_{2}$ must be of same type, either inductive or capacitive. And as $X_{1}+X_{3}=-X_{2}$ i.e. $X_{3}=-\left(X_{1}+X_{2}\right)$ the element $X_{3}$ must be a;posite type of reactance to $X_{1}$ and $X_{2}$.


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| Oscillator Type | Reactance elements in the tank circuit |  |  |
| :---: | :---: | :---: | :---: |
|  | x | $\mathrm{x}_{2}$ | $\mathrm{X}_{3}$ |
| Hartley oscillator | 1 | 1 | C |
| Colpits oscillator | C | C | L |

## (C) Hartlev Oscillator:

Explain the working of Hartley Oscillator. Derive the expression for frequency of oscillation and condition for maintenance of oscillation.


## Circuit diagram



## Construction:

- The Hartley oscillator circuit using BJT as an active device.
- The resistances $\mathrm{R}_{1}, \mathrm{R}_{2}$ and $\mathrm{R}_{\mathrm{E}}$ are biasing resistors
- The RFC is radio frequency chock whose reactance value is very high and high frequency and can be treated as open circuit. While for d.c operation, it is shorted hence does not cause problems for d.c operation.
- Due to RFC, the isolation between a.c and d.c operation is achieved. The $\mathrm{C}_{1}$ and $\mathrm{C}_{2}$ are coupling capacitors while $\mathrm{C}_{\mathrm{E}}$ is the emitter bypass capacitor. The CE amplifier provides phase shift of $180^{\circ}$.
- In the feedback circuit, as the centre of $L_{1}$ and $L_{2}$ is grounded, it provides additional phase shift of $180^{\circ}$. This satisfies Barkhausen condition. In this oscillator, $\mathrm{X}_{1}=\omega \mathrm{L}_{1}$, $X_{2}=\omega L_{2}, X_{3}=-1 / \omega C$


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## Analysis:

- For LC oscillator, $\mathrm{X}_{1}+\mathrm{X}_{2}+\mathrm{X}_{3}=0$

$$
\begin{aligned}
& \therefore \omega L_{1}+\omega L_{2}-\frac{1}{\omega C}=0 \\
& \text { i.e } \quad \omega\left(L_{1}+L_{2}\right)=\frac{1}{\omega c} \\
& \therefore \omega=\frac{1}{\substack{\sqrt{\left(L_{1}+\right.}}} \quad \text { i.e } f=\frac{1}{2 \pi \sqrt{\left(L_{1}+L_{2}\right) C}}
\end{aligned}
$$

- The inductance $L_{1}+L_{2}$ is equivalent inductance denoted as $L_{\text {eq }}$. To satisfy $|A \beta|=1$, then $\mathrm{h}_{\mathrm{fe}}$ of the BJT used must be $\mathrm{L}_{1} / \mathrm{L}_{2}$.

$$
h_{f e}=\frac{L_{1}}{L_{2}}
$$

- Practically L1 and L2 are wound on a single core and there exists a mutual inductance M between them.
In this case,

$$
f=\frac{1}{2 \pi \sqrt{L_{e q} C}} \quad \text { and } h_{f e}=\frac{L_{1}+M}{L_{2}+M}
$$

$$
L_{e q}=L_{1}+L_{2}+2 M
$$

- If capacitor C is kept variable, frequency can be varied over wide range.


## Derivation of frequency of Oscillations

- The output current is collector current which is $\mathrm{h}_{\mathrm{fe}} \mathrm{I}_{\mathrm{b}}$, where $\mathrm{I}_{\mathrm{b}}$ is base current. Assuming coupling capacitors shorted the capacitor C gets connected between collector and base.
- As emitter is grounded for a.c analysis, $L_{1}$ is between emitter and base while $L_{2}$ is between emitter and collector.
- $\mathrm{h}_{\mathrm{ie}}$ is the input impedance of the transistor. The output current is $\mathrm{I}_{\mathrm{b}}$ while input current is $\mathrm{h}_{\mathrm{fe}} \mathrm{I}_{\mathrm{b}}$. Convert current source to voltage source.
$V_{O}=h_{f e} I_{b} j X_{L 2}=h_{f e} I_{b} j \omega L_{2}$
- Total current I is,

$$
I=\frac{-V_{o}}{\left[X_{L 2}+X_{C}\right]+\left[X_{L 1}| | h_{i e}\right]}
$$

- Negative sign is because direction of I is opposite to the polarities of $\mathrm{V}_{\circ}$

$$
\begin{aligned}
& X_{L 2}+X_{C}=j \omega L_{2}+\frac{1}{j \omega C}=\frac{-\omega^{2} L_{2} C+1}{j \omega C} \\
& X_{L 1} \| h_{i e}=\frac{j \omega L_{1} h_{i e}}{j \omega L_{1}+h_{i e}}
\end{aligned}
$$

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$$
\therefore I=\frac{-h_{f e} I_{b} j \omega L_{2}}{\frac{-\omega^{2} L_{1} C+1}{j \omega C}+\frac{j \omega L_{1} h_{i e}}{j \omega L_{1}+h_{i e}}}
$$

- Using current division rule for parallel elements,

$$
\begin{aligned}
& I_{b}=I X \frac{j \omega L_{1}}{j \omega L_{1}+h_{i e}} \\
& I_{b}=\frac{-h_{f e} I_{b j} \omega L_{2}}{\frac{\omega^{2} L_{2} C+1}{j \omega C}+\frac{1 \omega L h}{j \omega L_{1}+h_{i e}}} X \underset{1}{j \omega L_{i e}} \\
& \therefore 1=\frac{j \omega^{3} h_{f e} C L_{1} L_{2}}{-j \omega^{3} L^{1} L_{2} C h_{i e}\left(L_{1}+L_{2}\right)+j \omega L_{1}+h_{i e}} \\
& \therefore 1=\frac{j \omega^{3} h_{f e} C L_{1} L_{2}}{\left[h_{i e}-\omega^{2} C h_{i e}\left(L_{1}+L_{2}\right)\right]+j \omega L_{1}\left(1-\omega^{2} L_{2} C\right)}
\end{aligned}
$$

- Rationalizing R.H.S of the above equation,

$$
1=\frac{\omega^{4} h_{f e} L_{1}^{2} L_{2} C\left(1-\omega^{2} L_{2} C\right)+j \omega^{3} h_{f e} L_{1} L_{2} C\left[h_{i e}-\omega^{2} C h_{i e}\left(L_{1}+L_{2}\right)\right]}{\left[h_{i e}-\omega^{2} C h_{i e}\left(L_{1}+L_{2}\right)\right]^{2}+\omega^{2} L_{1}^{2}\left(1-\omega^{2} L_{2} C\right)^{2}}
$$

- Imaginary part of R.H.S of above equation must be Zero

$$
\therefore 1-\omega^{3} C\left(L_{1}+L_{2}\right)=0 \quad \text { i.e } \omega=\frac{1}{\sqrt{C\left(L_{1}+L_{2}\right)}} \quad\left(\omega^{3} h_{f e} h_{i e} L_{1} L_{2} C \neq 0\right)
$$

$$
f=\frac{1}{2 \pi \sqrt{C\left(L_{1}+L_{2}\right)}}=\frac{1}{2 \pi \sqrt{C L_{e q}}}
$$

- Equating magnitude of both sides of the equation and using $\omega=\frac{1}{\sqrt{C\left(L_{1}+L_{2}\right)}}$ we get $h_{f e}=\frac{L_{1}}{L_{2}} \quad h_{f e}$ required for oscillation
- In practice, $L_{1}$ and $L_{2}$ may be wound on a single core so that there exists a mutual inductance between them denoted as M .
- In such a case, the mutual inductance is considered while determining the equivalent inductance $\mathrm{L}_{\text {eq }}, \quad \mathrm{L}_{\text {eq }}=\mathrm{L}_{1}+\mathrm{L}_{2}+2 \mathrm{M}$
- If $L_{1}$ and $L_{2}$ are assisting each other, then sign of $2 M$ is positive while if $L 1$ and $L 2$ are in series opposition then sign of 2 M is negative.


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## Advantage:

- The frequency can be easily varied by variable capacitor
- The output amplitude remains constant over the frequency range
- The feedback ratio of L1 and L2 remains constant
- It can be operated over wide range of frequency


## Disadvantage:

- The output is rich in harmonics hence not suitable for pure sine wave requirement
- Poor frequency stability


## Applications:

- Used as local oscillators in TV and radio receivers
- In function generators
- In radio frequency sources


## (D) COLPITTS OSCILLATOR:

Explain the working of Colpitts Oscillator. Derive the expression for frequency of oscillation and condition for maintenance of oscillation.

> (OR)

With a neat circuit diagram deduce the necessary condition for oscillations and expression for oscillation frequency in the case of Colpitts Oscillator.

## Construction:



## Transistorised Colpitts oscillator

- It uses two capacitive resistances and one inductive reactance in its feedback network.
- The amplifier stage uses BJT in common emitter configuration providing $180^{\circ}$ phase shift. The resistance $\mathrm{R}_{1}, \mathrm{R}_{2}$ and $\mathrm{R}_{\mathrm{E}}$ are the biasing resistors.
- The RFC is radio frequency choke providing insulation between AC and DC operations. The $\mathrm{C}_{\mathrm{C} 1}$ and $\mathrm{C}_{\mathrm{C} 2}$ are coupling capacitors. In the feedback circuit, as the center $\mathrm{C}_{1}$ and $\mathrm{C}_{2}$ are grounded, it provides additional phase shift of $180^{\circ}$, satisfying Barkhausen angle condition.


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- In this oscillator $X_{1}=\frac{-1}{\omega C_{1}} \quad X_{2}=\frac{-1}{\omega C_{2}} \quad X_{3}=\omega L$
- For LC oscillator, $\mathrm{X}_{1}+\mathrm{X}_{2}+\mathrm{X}_{3}=0$
$\therefore-\frac{1}{\omega C_{1}}-\frac{1}{\omega C_{2}}+\omega L=0$
i.e $\omega L=\frac{1}{\omega}\left[\frac{1}{C_{1}}+\frac{1}{C_{2}}\right]$
$\therefore \omega^{2}=\frac{1}{L\left[\frac{C_{1} \underline{C}}{C_{1}+C_{2}}\right]}$
where $\frac{C 1 C 2}{C_{1}+C_{2}}=C_{e q}$
$\therefore \omega=\frac{1}{\sqrt{L} C_{e q}}$ i.e $f=\frac{1}{2 \pi \sqrt{L C_{e q}}}$ and $C_{e q}=\frac{C_{1} C_{2}}{C_{1}+C_{2}}$
- To satisfy magnitude condition of Barkhausen criterion, the $\mathrm{h}_{\mathrm{fe}}$ of BJT used is given by

$$
h_{f e}=\frac{C_{2}}{C_{1}}
$$

## Derivation of Frequency of oscillations

- The equivalent circuit and simplified equivalent circuit.

(a) Equivalent circuit

$V_{0}=h_{f e} I_{b} X_{C 2}=\frac{-j h_{f e} \underline{\underline{\underline{b}}}}{\omega C_{2}} \quad \quad \ldots . . X_{C 2}=\frac{1}{j \omega C_{2}}=-\frac{j}{\omega C_{2}}$
- The total current drawn I is,

$$
\begin{aligned}
& I=\frac{-V_{0}}{\left[X C_{2}+X_{L}\right]+\left[X C_{1} \| h_{i e}\right]} \\
& X C_{2}+X_{L}=\frac{-j}{\omega C_{2}}+j \omega L=\frac{-j\left(1-\omega^{2} L C_{2}\right)}{\omega C_{2}} \\
& X_{C 1} \| h_{i e}=\frac{-\frac{\omega C_{1}}{-\frac{C_{1}}{\omega C_{1}}+h_{i e}}}{-\frac{-j h_{i e}}{}}=\frac{-\omega C_{1} h_{i e}}{} \\
& I=\frac{-\left[-\frac{j h_{f e} I_{b}}{\omega C_{2}}\right]}{\frac{-j\left(1-\omega^{2} L C_{2}\right)}{\omega C_{2}}-\frac{-j h_{i e}}{-j+\omega C_{1} h_{i e}}}
\end{aligned}
$$

- Using current division rule for parallel elements


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$I_{b}=I X \frac{\frac{-j}{\omega C_{1}}}{\frac{-j}{\omega C_{1}}+h_{i e}}=\frac{-j I}{-j+\omega C_{1} h_{i e}}$

$$
\begin{align*}
I_{b} & =-j\left[\frac{\frac{j h_{f e} I_{b}}{\omega C_{2}}}{\frac{-j\left(1-\omega^{2} L C_{2}\right)}{\omega C_{2}} \frac{-j h_{i e}}{-j+}}\right]\left[\frac{1}{-j+\omega C_{1} h_{i e}}\right] \\
1 & =\frac{-h_{f e}}{\omega C_{1} h_{i e}}  \tag{1}\\
\left(1-\omega^{2} L C_{2}\right)+j \omega h_{i e}\left[C_{1}+C_{2}-\omega^{2} L C_{1} C_{2}\right] & ---\cdots-----
\end{align*}
$$

- To have imaginary part of above equation zero
$\mathrm{C} 1+\mathrm{C} 2-\omega^{2} \mathrm{LC}_{1} \mathrm{C}_{2}=0 \quad$ i.e $\omega^{2}=\frac{C_{1}+C_{2}^{2}}{L C_{1} C_{2}}=\frac{1}{L\left[\frac{C_{1} \underline{C}_{2}}{C_{1}+C_{2}}\right]}$

$$
\omega=\frac{1}{\sqrt{L C_{e q}}} \text { and } f=\frac{1}{2 \pi \sqrt{L C_{e q}}} \text { where } C_{e q}=\frac{C_{1} C_{2}}{C_{1}+C_{2}}
$$

- Substituting $\omega$ in equation 1 and equating magnitudes of both sides

$$
h_{f e}=\frac{C_{2}}{C_{1}}
$$

## Advantages:

- Pure output waveform
- Good stability at high frequency
- Improved performance at high frequency
- Wide range of frequency
- Simple construction


## Disadvantages:

- Difficult to adjust the feedback
- Poor isolation


## Applications:

- Its main application is high frequency function generators.


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(E) CRYSTAL OSCILLATOR:

Describe and explain the operation of the crystal oscillator.
(OR)

## Can you use Piezo-Electric effect for electric oscillators? If so, explain a component with such characteristics. Also draw a circuit for the same.

- The crystals are either naturally occurring or synthetically manufactured, exhibiting the piezoelectric effect
- The piezoelectric effect means under the influence of mechanical pressure, the voltage gets generated across the opposite faces of the crystal
- If the mechanical force is applied in such a way to force the crystal to vibrate the a.c voltage gets generated across it.
- Every crystal has its own resonating frequency depending on its cut. So under the influence of the mechanical vibrations, the crystal generates an electrical signal of very constant frequency
- The crystal has a greater stability in holding the constant frequency. The crystal oscillators are preferred when greater frequency stability is stability
- Quartz is a compromise between the piezoelectric activity of Rochelle salt and the strength of the tourmaline.
- Quartz is inexpensive and easily available in nature hence very commonly used in the crystal oscillators.


## Constructional Details:

- The natural shape of quartz is a hexagonal prism. But for its practical use, it is cut to the rectangular slab. This slab is then mounted between the two metal plates.

- The metal plates are called holding plates, as they hold the crystal slab in between them.


## A.C. Equivalent circuit:


$\mathrm{C}_{\mathrm{M}}$ - Mounting Capacitance (due to two metal plates separated by dielectric like crystal slab).
R - Resistance (internal friction loss during vibration)
L - Inductance (indication of inertia of mass of crystal)
C - Capacitor (stiffness during vibrating)

- RLC forms a resonating circuit. The expression for the resonating frequency $f_{r}$ is,

$$
f_{r}=\frac{1}{2 \pi \sqrt{L C}} \sqrt{\frac{Q^{2}}{1+Q^{2}}} \text { where } \mathrm{Q}=\text { Quality factor of crystal }
$$

$$
Q=\frac{\omega L}{R}
$$

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- The Q factor of the crystal is very high, typically 20,000 . Value of Q up to $10^{6}$ also can be achieved. Hence $\sqrt{\sqrt{Q^{2}}}$ factor approaches to unity and we get the resonating frequency as $f_{r}=\frac{1}{2 \pi \sqrt{L C}}$
- The crystal frequency is in fact inversely proportional to the thickness of the crystal.
- $\mathrm{f} \alpha_{t}^{1}$ where $\mathrm{t}=$ Thickness
- So to have very frequencies, thickness of the crystal should be very small
- The crystal has two resonating frequencies, series resonant frequency and parallel resonant frequency.


## Applications

- Watches
- Communication transmitters and receivers


## Series and Parallel resonance:

## - Series Resonance frequency

$$
f_{s}=\frac{1}{2 \pi \sqrt{L C}}
$$

- Parallel Resonance frequency
- $\quad f_{P=\frac{1}{2 \pi \sqrt{L C_{e q}}}}$

- If we neglect the resistance $R$, the impedance of the crystal is a reactance $j X$ which depends on the frequency as,

$$
j X=-\frac{j \omega^{2}-\omega_{s}^{2}}{\omega C_{M} \omega^{2}-\omega_{p}^{2}}
$$

Where, $\omega_{\mathrm{s}}=$ Series resonant frequency

- Reactance against frequency is shown in fig.


## Crystal Stabilitv:

i. Temperature stability
ii. Long term stability
iii. Short term stability

## Types of Crystal Oscillator:

1. Pierce Crystal Oscillator:
2. Miller Crystal Oscillator:

## Pierce Crystal Oscillator:

Miller Crystal Oscillator:


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Comparison between Crystal and LC Oscillator:

| Sr. No. | LC oscillators | Crystal oscillators |
| :---: | :---: | :---: |
|  | The separate $L$ and $C$ components are necessary in the tuned circuit. | The single crystal serves the purpose of tuned circuit. |
| 2. | The Q value of LC tuned circuit is less as compared to the crystal. | The $Q$ value is much higher than LC tuned circuit. |
| 3. | The frequency stability is less. | Very high frequency stability. |
| 4. | The bandwidth is more. | The bandwidth is very small. |
| 5. | The effect of temperature on the frequency is more severe. | The effect of temperature on frequency is negligible. |
| 6. | The frequency range which can be generated is more. | There is limit to the frequency generated due to thickness of the crystal. |
| 7. | Used in general purpose applications like signal generators. | Used in specific applications which need high frequency stability like watches, computers, counters. |

## Solved Problems

1. In a Hartley oscillator, if $\mathrm{L}_{1}=0.2 \mathrm{mH}, \mathrm{L}_{2}=0.3 \mathrm{mH}$ and $\mathrm{C}=0.003 \mu \mathrm{~F}$. Calculate the frequency of oscillations. [MAY 2012]
Given: $\mathrm{L}_{1}=0.2 \mathrm{mH}, \mathrm{L}_{2}=0.3 \mathrm{mH}, \mathrm{C}=0.003 \mu \mathrm{~F}$
To find frequency of oscillations $f=\mathbf{1} /(\mathbf{2} \boldsymbol{\pi} \sqrt{ }[(\mathbf{L} 1+\mathbf{L} 2) \mathrm{C})]$ by substituting $\mathrm{f}=\mathbf{1 2 9 . 9 4 9 \mathrm { KHz }}$
2. In a $R C$ phase shift oscillator if $R_{1}=R_{2}=R_{3}=200 K \Omega$ and $C_{1}=C_{2}=C_{3}=100 P F$. Find the frequency of oscillation? (Apr/May 2018)

## Solution:

$$
\begin{aligned}
& \text { The frequency of an RC phase shift oscillator is given by } \\
& \mathrm{F}_{\mathrm{o}}=\frac{1}{2 \pi R C \sqrt{6}} \quad \mathrm{~F}_{\mathrm{o}}=\frac{1}{2 \pi \times 200 \times 10^{3} \times 100 \times 10^{-12} \times \sqrt{6}} \quad \mathbf{F}_{\mathbf{0}}=\mathbf{3 . 2 4 8 K H Z}
\end{aligned}
$$

3. In a phase shift oscillator, $R 1=R 2=R 3=1 \mathrm{M} \Omega$ and $\mathrm{C} 1=\mathrm{C} 2=\mathrm{C} 3=68 \mathrm{pF}$. At what frequency does the circuit oscillate. (Nov/Dec 2018)
Given that,
For a phase shift oscillator, $\quad$ Resistance, $\mathrm{R}_{1}=\mathrm{R}_{2}=\mathrm{R}_{3}=1 \mathrm{M} \Omega ; \quad$ Capacitor, $\mathrm{C}_{1}=\mathrm{C}_{2}=\mathrm{C}_{3}=68 \mathrm{pF}$
Frequency, $\mathbf{f}=$ ?
Frequency of phase shift oscillator is given by, $f=\frac{1}{2 \pi R C \sqrt{6}}$
Substituting corresponding values in above equation, $f=\frac{1}{2 \pi X 1 X 10^{6} X 68 X \sqrt{6}}=955.9 \mathrm{~Hz} \quad$ frequency, $\mathrm{f}=955.9 \mathrm{~Hz}$

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4. A wien bridge oscillator is used for operation at 10 KHz . If the value of the resistor $R$ is 100 Kohms , what is the value of $\mathbf{C}$ required?

Solution:
Given: $\quad \mathrm{F}=10 \mathrm{KHZ}, \mathrm{R}=100 \mathrm{~K} \Omega, \mathrm{C}=$ ?
The frequency of oscillation is

$$
\begin{array}{lll}
\mathrm{F}=\frac{1}{2 \pi R C} & \mathrm{C}=\frac{1}{2 \pi R F} & \mathrm{C}=\frac{1}{2 \pi \times 100 \times 10^{3} \times 10 \times 10^{3}} \\
\mathbf{C}=\mathbf{1 . 5 9 1} \times \mathbf{1 0}^{-\mathbf{1 0} \mathbf{F}} &
\end{array}
$$

5. An amplifier has a c urrent gain of 240 and input impedance of $15 \mathrm{k} \boldsymbol{\Omega}$ without feedback. If negative current feedback ( $\mathbf{m i}=\mathbf{0 . 0 1 5}$ ) is applied, what will be the input impedance of the amplifier? (Nov/Dec 2017)

$$
\begin{array}{ll}
\text { Solution. } & Z_{\text {in }}^{\prime}=\frac{Z_{\text {in }}}{1+m_{i} A_{i}} \\
\text { Here } & Z_{\text {in }}=15 \mathrm{k} \Omega ; A_{i}=240 ; \quad m_{i}=0.015 \\
\therefore & Z_{\text {in }}^{\prime}=\frac{15}{1+(0.015)(240)}=3.26 \mathrm{k} \Omega
\end{array}
$$

6. Design a Wien bridge oscillator circuit to oscillate at a frequency of 20 KHz . (Nov/Dec2015)

Solution:

$$
\begin{aligned}
& \mathrm{f}=\frac{1}{2 \pi R c} \mathrm{f}=20 \mathrm{kHz}, \quad \text { Let } \mathrm{C}=0.01 \mu F \\
& \mathrm{f}=\frac{1}{2 \pi R c}, \quad R=\frac{1}{2 \pi f C}=\frac{1 \mathrm{www} . \text { Eng }}{2 \times \pi \times 20000 \times 0.01 \times 10^{-6}}=80 \mathrm{ohms} .
\end{aligned}
$$

7. A $1 \mathbf{m H}$ inductor is available. Find the capacitor values of a colpitt's oscillator so that $f=1 \mathbf{M H z}$ and feedback fraction=0.25 (Nov/Dec 2018)

## Solution:

Given that,
For a Colpitts oscillator,
Inductance, $\mathrm{L}=1 \mathrm{mH}$
Resonant frequency, $\mathrm{f}_{0}=1 \mathrm{MHz}$
Feedback factor, $\beta=0.25$
The resonant frequency of Colpitts oscillator is given by,

$$
\begin{equation*}
f_{0}=\frac{1}{2 \pi \sqrt{L C_{e q}}} \tag{1}
\end{equation*}
$$

Where, $C_{e q}=\frac{C_{1} C_{2}}{C_{1}+C_{2}}$
From equation (1),

$$
\begin{equation*}
C_{e q}=\frac{1}{4 \pi^{2} f_{0}^{2} L} \tag{2}
\end{equation*}
$$

Given feedback factor, $\beta=\frac{C_{1}}{C_{2}}=0.25$

$$
\mathrm{C}_{2}=4 \mathrm{C}_{1}
$$

Substituting the given specifications in equation (2)

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$$
C_{e q}=\frac{1}{4 \pi^{2}\left(10^{6}\right)^{2} \times 10^{-3}}
$$

$$
\frac{C_{1} C_{2}}{C_{1}+C_{2}}=2.533 \times 10^{-11}
$$

$$
\frac{4 c_{1}^{2}}{-1}=2.53 \times 10^{-11}
$$

$$
5 C_{1}
$$

$$
\mathrm{C}_{1}=3.166 \times 10^{-11}=31.66 \mathrm{pF}
$$

From $\mathrm{C}_{2}=4 \mathrm{C}_{1}$,

$$
\mathrm{C}_{2}=4 \mathrm{X}\left(3.166 \times 10^{-11}\right)
$$

$$
\mathrm{C}_{2}=126.65 \mathrm{pF}
$$

8. The overall gain of a multistage amplifier is $\mathbf{1 4 0}$. When negative voltage feedback is applied the gain is reduced to $\mathbf{1 7 . 5}$ find the fraction of the output that is feedback to the input. (Nov/Dec 2018)
Given that,
For a multistage feedback amplifier,
Overall gain, $\mathrm{Av}_{\mathrm{v}}=140$
Feedback gain, $\mathrm{A}_{\mathrm{vf}}=17.5$
Feedback fraction, $\boldsymbol{\beta}=$ ?
Voltage gain of negative feedback amplifier is defined as,

$$
\begin{gathered}
A_{v f}=\frac{A_{v}}{1+A_{v} \beta} 17.5=\frac{40}{1+140 \beta} \\
17.5+2450 \beta=140 \\
\beta=\frac{1}{20}=0.05 \\
\boldsymbol{\beta}=\mathbf{0 . 0 5}
\end{gathered}
$$

9. In colpitts oscillator $\mathbf{C 1}=\mathbf{1 n F}$ and $\mathbf{C} \mathbf{2}=\mathbf{1 0 0 n F}$. If the frequency of oscillation is $\mathbf{1} \mathbf{k H z}$ find the value of inductor. Also find the minimum gain required for obtaining sustained oscillations. (May / Jun 2016) Given data:
$\mathrm{C} 1=1 \mathrm{nF}, \mathrm{C} 2=100 \mathrm{nF}$, Frequency of oscillation $\mathrm{f}=100 \mathrm{kHz}$.

## Formulae used:

$$
f=\frac{1}{2 n} \sqrt{\frac{C 1+C 2}{L 1 C 1 C 2^{2}}}, A_{V}=\frac{C 1}{C 2}
$$

Frequency of oscillations

$$
L=\frac{C 1+C 2}{4 n^{2} f_{r}^{2} C 1 C 2}=\frac{101 \times 10^{-6}}{4 n^{2} \times(10 \times 1000)^{2} \times 100 \times 10^{-12}}
$$

$$
=\frac{101 \times 10^{6}}{4 n^{2} \times(100000)^{2}}=\frac{101}{3.99} \times 10^{-5}=25.634 \times 10^{-5} \mathrm{H}=256.34 \mu \mathrm{~F}
$$

$$
A_{V}>\frac{C 1}{C 2}=\frac{1}{100}=0.01 \mathrm{nF}
$$

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10. Design a RC phase Shift Oscillator to generate 5 KHz sine wave with 20 V peak to Peak amplitude.

Assume $h_{\mathrm{fe}_{\mathrm{e}}}=\mathrm{Q}=150, C=1.5 n F$, hre=1.2K $\Omega$ (Nov.Dec 2016)

$$
\begin{gathered}
f=\frac{1}{2 \pi R c \sqrt{6}} ; \quad 5 \times 10^{3}=\frac{1}{2 \pi \times 1.5 \times 10^{-9} \sqrt{6} \times R} \quad R=\frac{1}{2 \pi \times 1.5 \times 10^{-9} \times \sqrt{6} \times 5 \times 10^{3}} \\
R=8.67 \mathrm{k} \Omega
\end{gathered}
$$

11. In Colpitts Oscillator, the desired frequency is 500 KHz . Find the value of L . Assume $\mathrm{C}=1000 \mathrm{pF}$. (Apr/May 2018)

$$
\therefore \quad \mathrm{C}_{\mathrm{eq}}=\frac{\mathrm{C}_{1} \mathrm{C}_{2}}{\mathrm{C}_{1}+\mathrm{C}_{2}}=500 \mathrm{pF}
$$

The frequency is given by,

$$
\begin{aligned}
& & \mathrm{f} & =\frac{1}{2 \pi \sqrt{\mathrm{LC} \mathrm{eq}}} \\
& \therefore & 500 \times 10^{3} & =\frac{1}{2 \pi \sqrt{\mathrm{~L} \times 500 \times 10^{-12}}} \\
& \therefore & \left(500 \times 10^{3}\right)^{2} & =\frac{1}{4 \pi^{2}\left[\mathrm{~L} \times 500 \times 10^{-12}\right]} \\
& \therefore & \mathrm{L} & =202.642 \mu \mathrm{H}
\end{aligned}
$$

12. When negative voltage feedback is applied to an amplifier of gain 100 , the overall gain falls to 50 .

Calculate the fraction of the output voltage fedback. If this fraction is maintained, calculate the value of the amplifier gain required if the overall stage gain is to be 75. (Nov/Dec 2017)
(i)

Gain without feedback, $A_{v}=100$ Gain with feedback, $A_{v f}=50$
Let $m_{v}$ be the fraction of the output voltage fedback.
Now
or
or
or
(ii)
or
or

$$
75+0.75 A_{v}=A_{v}
$$

$A_{v}=\frac{75}{1-0.75}=300$
13. In Colpitts oscillator, $\mathrm{C} 1=\mathrm{C} 2=\mathrm{C}$ and $\mathrm{L}=100 \times 10-6 \mathrm{H}$. The frequency of oscillation is 500 KHz . Determine the value of C. (Apr/May 2018)

Solution: The given values are,

$$
\begin{aligned}
& \mathrm{L}=100 \mu \mathrm{H}, \mathrm{C}_{1}=\mathrm{C}_{2}=\mathrm{C} \text { and } \mathrm{f}=500 \mathrm{kHz} \\
& \text { Now } \quad \mathrm{f}=\frac{1}{2 \pi \sqrt{\mathrm{LC}_{\text {eq }}}} \\
& \therefore \quad 500 \times 10^{3}=\frac{1}{2 \pi \sqrt{100 \times 10^{-6} \times \mathrm{C}_{\mathrm{eq}}}} \\
& \therefore \quad\left(500 \times 10^{3}\right)^{2}=\frac{1}{4 \pi^{2} \times 100 \times 10^{-6} \times \mathrm{C}_{\text {eq }}} \\
& \therefore \quad \mathrm{C}_{\mathrm{cq}}=1.0132 \times 10^{-9} \mathrm{~F} \\
& \text { but } \quad C_{\text {eq }}=\frac{C_{1} C_{2}}{C_{1}+C_{2}} \text { and } C_{1}=C_{2}=C \\
& \therefore \quad C_{\text {eq }}=\frac{C \times C}{C+C}=\frac{C}{2} \\
& \therefore \quad 1.0132 \times 10^{-9}=\frac{C}{2} \\
& \therefore \quad \mathrm{C}=2.026 \times 10^{-9} \mathrm{~F}=2.026 \mathrm{nF}
\end{aligned}
$$

14. An amplifier in required with a voltage gain of 100 which does not vary by more that $1 \%$. If it is to use negative feedback with a basic amplifier the voltage gain of which vary by $20 \%$, find the minimum voltage gain required and the feedback factor. (Nov/Dec 2018)

## Solution:

Closed loop voltage gain of amplifier, $\mathrm{A}_{\mathrm{f}}$ is defined as,

$$
\begin{align*}
& A_{f}=\frac{A_{m}}{1+A_{m} \beta}  \tag{1}\\
& \qquad 100=\frac{A_{m}}{1+A_{m} \beta} \\
& A_{m}=100+100 A_{m} \beta \tag{2}
\end{align*}
$$

Since, feedback voltage gain, $\mathrm{A}_{\mathrm{f}}$ does not vary more than $1 \%$ and amplifier gain varies by $20 \%$ equation (1) can be written as,

$$
\begin{align*}
& 99=\frac{0.8 A_{m}}{1+0.8 A_{m} \beta} \\
& 0.8 A_{m}=99+79.2 A_{m} \beta \quad-----(3)  \tag{3}\\
& \text { Multiplying equation (1) with } 0.792 \text { or both sides, } \\
& 0.792 A_{m}=79.2+79.2 A_{m} \beta \quad-----(4)
\end{align*}
$$

Subtracting equation (3) and (4),

$$
\begin{array}{lll}
0.008 \mathrm{~A}_{\mathrm{m}}=19.8 ; & =\frac{19.8}{0.008} & \mathbf{A}_{\mathrm{m}}=\mathbf{2 4 7 5} \\
A_{n} &
\end{array}
$$

Substituting $\mathrm{A}_{\mathrm{m}}$ in equation (2),

$$
\begin{aligned}
2475 & =100+100 \times 2475 \times \beta \\
\beta & =\frac{2475-100}{2475 \times 100}
\end{aligned}
$$

$$
\beta=0.0096
$$

$\therefore$ Feedback factor, $\beta=0.0096$ and minimum voltage gain $\mathrm{A}_{\mathrm{m}}=2475 \mathrm{~V}$.

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## Additional Important Ouestions:

6. Discuss the effect for the following negative feedback amplifiers and derive the expression for input resistance, output resistance and voltage gain for common emitter amplifier.
A. VOLTAGE SERIES FEEDBACK
B. VOLTAGE SHUNTFEEDBACK
C. CURRENT SERIES FEEDBACK
D. CURRENT SHUNT FEEDBACK

## (A) VOLTAGE SERIES FEEDBACK

Draw circuit of CE amplifier with Voltage Series feedback and obtain the expression for feedback ratio, voltage gain, input and output resistances.

Input is the feedback network is parallel with output of amplifier shunt connection to reduce output resistance $R_{o}$ series connection at the input increase the input resistance.

$$
\text { Voltage feedback factor } \beta=\frac{V_{f}}{V_{o}}
$$

## Gain

Amplifier Gain $A_{v}=\frac{V_{o}}{V_{i}}$

$$
V_{o}=A_{v} V_{i}---(1)
$$



Feedback is connected

$$
V_{s}=V_{i}+V_{f} \quad ;
$$

$$
V_{i}=V_{s}-V_{f}
$$

Now

$$
\begin{aligned}
V_{s}=V_{i}+\beta V_{o}= & V_{i}+\beta A_{v} V_{i} \\
& V_{s}=V_{i}(1+A \beta) \quad---(2) \\
& V_{i}=V_{s}-V_{f} \quad \& \quad V_{i}=I_{i} R_{i} \\
\therefore V_{s}= & V_{i}+V_{f}=I_{i} R_{i}+A \beta V_{i} \\
& =I_{i} R_{i}+A \beta R_{i} I_{i} \\
& V_{s}=R_{i} I_{i}(1+A \beta)
\end{aligned}
$$

Now, Input Impedance $Z_{i f}=\frac{V_{i}}{I_{i}}=\frac{I_{i} \underline{R_{i}}(1+A \beta)}{I_{i}}$

$$
\begin{gathered}
=\frac{V_{i}}{I_{i}}(1+A \beta) \\
Z_{i f}=Z_{i}(1+A \beta)
\end{gathered}
$$

Output impedance, $V_{o}=R_{o} I_{o}+A V_{i}, V_{i}=V_{s}-V_{P}$

$$
\begin{aligned}
& V_{s}=0 \\
& V_{i}=-V_{P}=\beta V_{o}
\end{aligned}
$$

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$$
\begin{gathered}
\therefore V_{o}=I_{o} R_{o}-A \beta V_{o} \\
V_{o}+A \beta V_{o}=I_{o} R_{o} \\
V_{o}(1+A \beta)=I_{o} R_{o} \\
\quad \underline{V}_{o}=\frac{R_{o}}{1+A \beta} \\
I_{o} \\
Z_{o}=\frac{R_{o}}{1+A \beta}
\end{gathered}
$$

$R_{o} \rightarrow$ output resistance of amplifier without feedback.

$$
\begin{aligned}
& A_{i}=\frac{I_{e}}{\hbar}=\frac{I_{b}+I_{c}}{I_{b}}=1+h \\
& R_{i}=h_{i e}+\left(1+h_{f e}\right) R_{E} \\
& A_{V}=\frac{A}{A_{f} \underline{R_{L}}} \\
& R_{o}=\frac{\left(1+h_{f e}\right) R_{L}}{h_{i e}+\left(1+h_{f e}\right) R_{L}}=1-\frac{h_{i e}}{R_{i}}+R_{V} \\
& 1+h_{f e} \\
& R_{o f}=R_{o} \| R_{c}
\end{aligned}
$$



## (B) VOLTAGE SHUNT FEEDBACK AMPLIFIER

Draw circuit of CE amplifier with Voltage Shunt feedback and obtain the expression for feedback ratio, voltage gain, input and output resistances. (April / May 2015 -R13)

Trans resistance Amplifier
Connection Diagram:

Gain: $A_{F}=\frac{V_{o}}{L}=\frac{V_{o}}{I_{i}}$

$$
\begin{aligned}
I_{s} & =I_{i}+I_{f} \\
& =I_{i}+\beta V_{o} \\
I_{s} & =I_{i}+A \beta I_{i}=I_{i}(1+A \beta)
\end{aligned}
$$

$A_{F}=\frac{\underline{V}_{Q}}{f}=\frac{A I_{i}}{I_{i}(1+A \beta)}=\frac{A}{1+A \beta}$ without feedback.

$\therefore$ The gain of the amplifier without feedback is reduced by a factor of $(1+A \beta)$

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Input Impedance:

$$
\begin{array}{lll}
Z_{i}=\frac{V_{i}}{I_{s}} ; \quad Z_{i}=\frac{V_{i}}{I_{i}+I_{f}} ; & Z_{i}=\frac{V_{i}}{} ; & Z_{i}=\frac{V_{i}}{} ; \quad Z_{i}=\frac{V_{i}}{I_{i}(1+A \beta)^{\prime}} \\
Z_{i}=\frac{Z_{i}}{(1+A \beta)} & & I_{i}+A \beta I_{o}
\end{array}
$$

Input impedance is reduced by the factor $(1+A \beta)$ for both series, shunt feedback connection.

## Output Impedance

$$
\begin{aligned}
& V_{o}=R_{o} I_{o}-A I_{i} \quad I_{i}=I_{S}-I_{F}, I_{f} I_{s} \text { transferred to output side } I_{s}=0 \\
& =R_{o} I_{o}-A I_{F} \quad \therefore \quad I_{i}=-I_{F} \\
& V_{o}+A \beta V_{o}=R_{o} I_{o} \quad V_{o}(1+A \beta)=R_{o} I_{o} \\
& \quad \frac{V_{o}}{I_{o}}=\frac{R_{o}}{1+A \beta} Z_{o}=\frac{V_{o}}{I_{o}}=\frac{R_{o}}{1+A \beta}
\end{aligned}
$$

## (C) CURRENT SHUNT FEEDBACK AMPLIFIER

Draw circuit of CE amplifier with Current Shunt feedback and obtain the expression for feedback ratio, voltage gain, input and output resistances. (April / May 2015 -R13)

## Connection Diagram



$$
\begin{array}{rr}
\text { Amplifier Gain, } A=\frac{V_{o}}{I_{i}} & I_{S}=l+I_{F} \\
\text { Feedback factor } \beta=\frac{\underline{F}}{F} & I_{F}=\beta I_{o} \\
I_{o} & \\
& I_{o}=A I_{i}
\end{array}
$$

Gain of the Amplifier

$$
\begin{aligned}
& A_{F}=\frac{I_{o}}{\frac{b}{j}}=\frac{A I_{i}}{I_{i}+I_{F}}=\frac{A I_{i}}{I_{i}+\beta I_{o}}=\frac{A I_{i}}{I_{i}+\beta A I_{i}} \\
& A_{F}=\frac{A}{1+\beta A}
\end{aligned}
$$

Input Impedance:


$$
\begin{aligned}
& I_{s}=I_{i}+I_{F} \\
& I=\frac{V_{i}}{R_{i}}+\beta I ; \quad{ }_{s}=\frac{V_{i}}{R_{i}}+A \beta I_{i} ; \quad I_{s}=\frac{V_{i}}{R_{i}}+\frac{A \beta V_{i}}{R_{i}} ; \quad I_{s}=\frac{V_{i}}{R_{i}}(1+A \beta)
\end{aligned}
$$

Input resistance of amplifier with feedback $R_{i f}$

$$
R_{i f}=\frac{V_{\underline{i}}}{I_{s}}=\frac{R_{i}}{1+A \beta}
$$

Output Impedance:
$I_{S}=I_{i}+I_{F} \quad I_{i}=I_{s}-I_{F}$
$I_{S}=0$, Source transferred to output side to calculate the output impedance.

$$
\begin{gathered}
I_{o}=A I+\frac{V_{\underline{o}}}{R_{o}} \\
\underline{V}_{\underline{o}}=(1+A \beta) \\
\text { wwh } R_{o}^{-} n g g \text { Tree.com } \\
R_{F}=\frac{V_{o}}{R_{o}}=R_{o}(1+A \beta)
\end{gathered}
$$

Thus, output impedance increased by $(1+A \beta)$

## (D) CURRENT SERIES FEEDBACK AMPLIFIER

Draw circuit of CE amplifier with Current Series feedback and obtain the expression for feedback ratio, voltage gain, input and output resistances. (April / May 2015 -R13)

Transconductance Amplifier:


Gain $=\frac{\underline{I}_{o}}{V_{o}}=\frac{\underline{I}_{0}}{V_{i}+V_{F}}$

$$
\begin{aligned}
& =\frac{A V_{i}}{V_{i}+\beta I_{o}} \Rightarrow \frac{A V_{i}}{V_{i}+A \beta V_{i}} \\
& A=\frac{A V_{i}}{V_{i}(1+A \beta)}=\frac{A}{1+A \beta}
\end{aligned}
$$

## Equivalent Circuit



Input Impedance:
$V_{s}=I_{i} R_{i}+V_{F}$
$=I_{i} R_{i}+\beta I_{o}$
$=I_{i} R_{i}+A \beta V_{i}$
$=I_{i} R_{i}+A \beta I_{i} R_{i}$
$=I_{i} R_{i}(1+A \beta)$
$Z_{i}=\frac{V_{s}}{I_{i}}=R(1+A \beta)$
$\therefore \quad$ Input impedance increased by factor $(1+A \beta)$
Output Impedance:
$V_{s}=0$
$V_{S}=V_{i}+V_{F}$
$V_{i}+V_{F}=0 ; \quad V_{i}=-V_{F}$
$I{ }_{o}=A V{ }_{i}+\frac{V_{o}}{Z_{o}}=-A V{ }_{i}+\frac{V_{o}}{Z_{o}}$
$=-A \beta I_{o}+\frac{V_{\underline{o}}}{Z_{o}}$
$I_{o}+A \boldsymbol{\beta}{ }_{o}=\frac{V_{o}}{Z_{o}}, \quad \quad I_{o}(1+A \beta)=\frac{V_{o}}{Z_{o}}$
$Z_{O F}=\frac{V_{o}}{I_{o}}=Z_{o}(1+A \beta)$
The output impedance is increased by factor $(1+A \beta)$

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7. Sketch the circuit diagram of a two-stage capacitor coupled BJT amplifier that uses series voltage negative feedback. Briefly explain $h_{\text {oe }}$ the feedback operates (Nov/Dec 2015)
It is a shunt or nodal sampling and series mixing. Also cascading means two or more amplifier are connected in series using coupling capacitor or coupling elements. This is shown in fig.


Above fig shows cascaded voltage series amplifier. This analysis of cascaded amplifiers is as follows.

## Step 1:

RF and RE1 acts as feedback. The,
i) $ß$ network is directly taken from $V_{0}$. Therefore, it is called voltage sampled.
ii) Also $\beta$ network is not directly connected to base hence it is not shunt mixing and therefore it is series feedback.

Therefore, the voltage series feedback $\mathrm{X}_{0}, \mathrm{X}_{\mathrm{s}}, \mathrm{X}_{\mathrm{i}}, \mathrm{X}_{\mathrm{f}}$ are voltages. Then its analysis is as followings.

## Step 2 :

$\beta=\frac{V_{f}}{V_{0}}$
WhereV $_{f}=\left(\underset{R_{f}+R_{E 1}}{V_{0}}\right) R_{E 1}$
Also, $\beta=\frac{\left(\frac{V_{0}}{R_{f}+R_{E 1}}\right) R_{E 1}}{V_{0}}$
$\therefore \beta=\frac{R_{E 1}}{R_{f}+R_{E 1}}$
Step 3 : Drawingbasicamplifier.=
(i)Fortheinputcircuitgotooutputandput $X_{0}=0$; i.e., $V_{0}=0$
(ii)Foroutputcircuitgotoinputandput $I_{i}=0$

$$
\begin{gathered}
\text { Anyhow, } \quad R_{E}=R_{E 1} \| R_{f} \text { (or) } \\
R_{E}=\frac{R_{E 1} R_{f}}{R_{E 1}+R_{f}}
\end{gathered}
$$

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Also, $R_{L 2}=R_{C 2} \|\left(R_{f}+R_{E 1}\right)$

$$
R_{L 2}=\frac{R_{C 2} \times\left(R_{f}+R_{E 1}\right)}{R_{C 2}+R_{f}+R_{E 1}}
$$

This is the basic amplifier equivalent circuit is as in figure 3.40


Here, the first stage is common emitter connection with feedback resistor $R_{f} a n d R_{E 1}$ is also called $\boldsymbol{g l o b a l f e e d b a c k}$.
Step 4 : Analysisgivesthefollowingresultsinshort,
i.e., $\quad D=1+A_{V} \beta$
$A_{v f}=\frac{A_{v}}{D}$ or $\frac{A_{V}}{\left(1+A_{v} \beta\right)}$
$R_{i f}=R_{i} \times \operatorname{DorR}_{i}\left(1+A_{V} \beta\right)$
$R_{o f}=\frac{R_{0}}{D}$ or $\frac{R_{0}}{\left(1+A_{V} \beta\right)}$


From the above analysis voltage gain with feedback $A_{V F}$ and output resistance $R_{0 f}$ is reduced by $(1+A \beta)$ times, and input resistance ( $R_{i f}$ ) with feedback is increased by ( $1+A \beta$ ) times.


[^0]:    Amplifier frequency response with and without negative feedback. Negative feedback oxtends the amplifier bandwidth.

